

# Package ‘stable’

March 2, 2022

**Version** 1.1.6

**Title** Probability Functions and Generalized Regression Models for Stable Distributions

**Depends** R (>= 1.4), rmutil

**Description** Density, distribution, quantile and hazard functions of a stable variate; generalized regression models for the parameters of a stable distribution. See the README for how to make equivalent calls to those of 'stabledist' (i.e., Nolan's 0-parameterization and 1-parameterization as detailed in Nolan (2020)). See github for Lambert and Lindsey 1999 JRSS-C journal article, which details the parameterization of the Buck (1995) stable. See the Details section of the `?dstable` help file for context and references.

**License** GPL (>= 2)

**URL** <https://www.commanster.eu/rcode.html>

**BugReports** <https://github.com/swihart/stable/issues>

**Encoding** UTF-8

**LazyLoad** true

**RoxygenNote** 7.1.2

**NeedsCompilation** yes

**Author** Bruce Swihart [cre, aut],  
Jim Lindsey [aut] (Jim created this package, Bruce is maintaining the CRAN version),  
Philippe Lambert [aut]

**Maintainer** Bruce Swihart <bruce.swihart@gmail.com>

**Repository** CRAN

**Date/Publication** 2022-03-02 00:50:02 UTC

## R topics documented:

dstable . . . . .	2
Links . . . . .	5
Parameter_Conversion . . . . .	6
Parameter_Conversion_Nolan_pm1_pm0 . . . . .	7
stable.mode . . . . .	9
stablereg . . . . .	10

<b>Index</b>	<b>16</b>
--------------	-----------

---

dstable	<i>Stable Distribution</i>
---------	----------------------------

---

### Description

These functions provide information about the stable distribution with the location, the dispersion, the skewness and the tail thickness respectively modelled by the parameters `loc`, `disp`, `skew` and `tail`. These differ from those of 'stabledist' (i.e., Nolan's 0-parameterization and 1-parameterization as detailed in Nolan (2020)). See the README for how to make equivalent calls to those of 'stabledist' (i.e., Nolan's 0-parameterization and 1-parameterization as detailed in Nolan (2020)).

### Usage

```
dstable(
  x,
  loc = 0,
  disp = 1/sqrt(2),
  skew = 0,
  tail = 2,
  npt = 501,
  up = 10,
  eps = 1e-06,
  integration = "Romberg"
)
```

```
pstable(q, loc = 0, disp = 1/sqrt(2), skew = 0, tail = 2, eps = 1e-06)
```

```
qstable(p, loc = 0, disp = 1/sqrt(2), skew = 0, tail = 2, eps = 1e-06)
```

```
rstable(n = 1, loc = 0, disp = 1/sqrt(2), skew = 0, tail = 2, eps = 1e-06)
```

```
hstable(x, loc = 0, disp = 1/sqrt(2), skew = 0, tail = 2, eps = 1e-06)
```

### Arguments

<code>x</code> , <code>q</code>	vector of quantiles.
<code>loc</code>	vector of (real) location parameters.

disp	vector of (positive) dispersion parameters.
skew	vector of skewness parameters (in [-1,1]).
tail	vector of parameters (in [0,2]) related to the tail thickness.
npt, up, integration	As detailed herein – only available when using dstable.
eps	scalar giving the required precision in computation.
p	vector of probabilities.
n	number of observations.

### Details

dstable, pstable, qstable and hstable compute the density, the distribution, the quantile and the hazard functions of a stable variate. rstable generates random deviates with the prescribed stable distribution.

loc is a location parameter in the same way as the mean in the normal distribution: it can take any real value.

disp is a dispersion parameter in the same way as the standard deviation in the normal distribution: it can take any positive value.

skew is a skewness parameter: it can take any value in  $(-1, 1)$ . The distribution is right-skewed, symmetric and left-skewed when skew is negative, null or positive respectively.

tail is a tail parameter (often named the characteristic exponent): it can take any value in  $(0, 2)$  (with tail=1 and tail=2 yielding the Cauchy and the normal distributions respectively when symmetry holds).

If loc, disp, skew, or tail are not specified they assume the default values of 0,  $1/\sqrt{2}$ , 0 and 2 respectively. This corresponds to a normal variate with mean= 0 and variance=  $1/2disp^2$ .

The stable characteristic function is given by

$$greekphi(t) = ilocat - disp|t|^{tail} [1 + iskewsign(t)greekomega(t, tail)]$$

where

$$greekomega(t, tail) = \frac{2}{\pi} LOG(ABS(t))$$

when tail=1, and

$$greekomega(t, tail) = \tan\left(\frac{\pi tail}{2}\right)$$

otherwise.

The characteristic function is inverted using Fourier's transform to obtain the corresponding stable density. This inversion requires the numerical evaluation of an integral from 0 to  $\infty$ . Two algorithms are proposed for this. The default is Romberg's method (integration="Romberg") which is used to evaluate the integral with an error bounded by eps. The alternative method is Simpson's integration (integration="Simpson"): it approximates the integral from 0 to  $\infty$  by an integral from 0 to up with npt points subdividing  $(O, up)$ . These three extra arguments – integration, up and npt – are only available when using dstable. The other functions are all based on Romberg's algorithm.

[Swihart 2022 update:]

See the README for how to make equivalent calls to those of 'stabledist' (i.e., Nolan's 0-parameterization and 1-parameterization as detailed in Nolan (2020)). See github for Lambert and Lindsey 1999 JRSS-C journal article, which details the parameterization of the Buck (1995) stable distribution which allowed a Fourier inversion to arrive at a form similar to but not exactly the  $g_d$  function as detailed in Nolan (2020), Abdul-Hamid and Nolan (1998) and Nolan (1997). The Nolan (2020) reference is a textbook that provides an accessible and comprehensive summary of stable distributions in the 25 years or so since the core of this R package was made and put on CRAN. The Buck (1995) parameterization most closely resembles the Zolotarev B parameterization outlined in Definition 3.6 on page 93 of Nolan (2020) – except that Buck (1995) did not allow the scale parameter to multiply with the location parameter. This explains why the 'Zolotarev B' entry in Table 3.1 on page 97 of Nolan (2020) has the location parameter being multiplied by the scale parameter whereas in converting the Lindsey and Lambert (1999) to Nolan 1-parameterization the location parameter stays the same.

To be clear, `dstable` and `pstable` are evaluated by numerically integrating the inverse Fourier transform. The code works reasonably for small and moderate values of  $x$ , but will have numerical issues in some cases (such as values from `pstable` being greater than 1 or not being monotonic). The arguments `npt`, `up`, `integration`, and `eps` can be adjusted to improve accuracy at the cost of speed, but will still have limitations. Functions that better handle these problems are available in other packages (such as `stabledist` and `stable`) that use an alternative method (as detailed in Nolan 1997) distinct from directly numerically integrating the Fourier inverse transform. See last example in the README.

## Functions

- `dstable`: density
- `pstable`: cdf
- `qstable`: quantiles
- `rstable`: random deviates
- `hstable`: hazard

## Author(s)

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>)

Jim Lindsey

## References

- Lambert, P. and Lindsey, J.K. (1999) Analysing financial returns using regression models based on non-symmetric stable distributions. *Applied Statistics*, 48, 409-424.
- Nolan, John P. *Univariate stable distributions*. Berlin/Heidelberg, Germany: Springer, 2020.
- Nolan, John P. "Numerical calculation of stable densities and distribution functions." *Communications in statistics. Stochastic models* 13.4 (1997): 759-774.
- Abdul-Hamid, Husein, and John P. Nolan. "Multivariate stable densities as functions of one dimensional projections." *Journal of multivariate analysis* 67.1 (1998): 80-89.

**See Also**

[stablereg](#) to fit generalized nonlinear regression models for the stable distribution parameters. R packages `stabledist` and `libstableR` provide `[dpqr]` functions.

**Examples**

```
par(mfrow=c(2,2))
x <- seq(-5,5,by=0.1)

# Influence of loc (location)
plot(x,dstable(x,loc=-2,disp=1/sqrt(2),skew=-0.8,tail=1.5),
     type="l",ylab="",main="Varying LOCation")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=-0.8,tail=1.5))
lines(x,dstable(x,loc=2,disp=1/sqrt(2),skew=-0.8,tail=1.5))

# Influence of disp (dispersion)
plot(x,dstable(x,loc=0,disp=0.5,skew=0,tail=1.5),
     type="l",ylab="",main="Varying DISPersion")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=0.9,skew=0,tail=1.5))

# Influence of skew (skewness)
plot(x,dstable(x,loc=0,disp=1/sqrt(2),skew=-0.8,tail=1.5),
     type="l",ylab="",main="Varying SKEWness")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0.8,tail=1.5))

# Influence of tail (tail)
plot(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=0.8),
     type="l",ylab="",main="Varying TAIL thickness")
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=1.5))
lines(x,dstable(x,loc=0,disp=1/sqrt(2),skew=0,tail=2))
```

---

Links

*Links*

---

**Description**

Link and inverse functions for use in `stablereg`

**Usage**

```
loc_g(x)

loc_h(x)

disp_g(x)
```

disp\_h(x)

skew\_g(x)

skew\_h(x)

tail\_g(x)

tail\_h(x)

### Arguments

x                    the function argument

---

Parameter\_Conversion    *Easy conversion of parameters between stabledist (Nolan 1-parameterization) and stable (Lambert and Lindsey 1999)*

---

### Description

sd2s has stabledist parameter (Nolan 1-parameterization) inputs and returns stable parameters as put forth in Lambert and Lindsey (1999) and used in this package. s2sd has stable parameter (Lambert and Lindsey (1999)) inputs and returns stabledist parameters (Nolan 1-parameterization). See examples and the readme. There's also more context and references in '?stable::dstable'.

### Usage

```
sd2s(alpha, beta, gamma, delta, pm = 1)
```

```
s2sd(tail, skew, disp, loc, pm = 1)
```

### Arguments

alpha	the stabledist 'alpha'
beta	the stabledist 'beta'
gamma	the stabledist 'gamma'
delta	the stabledist 'delta'
pm	default 1; currently only value supported. the stabledist parameterization 'pm'
tail	the stable 'tail' analogous to 'alpha'
skew	the stable 'skew' analogous to 'beta'
disp	the stable 'disp' analogous to 'gamma'
loc	the stable 'loc' analogous to 'delta'

## Details

[Swihart 2022 update:] See the examples and README for how to make equivalent calls to those of 'stabledist' (i.e., Nolan's 1-parameterization as detailed in Nolan (2020)) using these functions and this package. See github for Lambert and Lindsey 1999 JRSS-C journal article, which details the parameterization of the Buck (1995) stable distribution which allowed a Fourier inversion to arrive at a form of the  $g_d$  function as detailed in Nolan (2020), The Buck (1995) parameterization most closely resembles the Zolotarev B parameterization outlined in Definition 3.6 on page 93 of Nolan (2020) – except that Buck (1995) did not allow the scale parameter to multiply with the location parameter. This explains why the 'Zolotarev B' entry in Table 3.1 on page 97 of Nolan (2020) has the location parameter being multiplied by the scale parameter whereas in converting the Lindsey and Lambert (1999) to Nolan 1-parameterization the location parameter stays the same.

## Value

sd2s returns stable parameters as put forth in Lambert and Lindsey (1999) and used in this package.  
s2sd returns stabledist parameters (Nolan 1-parameterization).

## References

Lambert, P. and Lindsey, J.K. (1999) Analysing financial returns using regression models based on non-symmetric stable distributions. Applied Statistics, 48, 409-424.

Nolan, John P. Univariate stable distributions. Berlin/Heidelberg, Germany: Springer, 2020.

## Examples

```
## Not run:
q <- -1
# nolan pm=1 parameters:
a <- 1.3
b <- -0.4
c <- 2
d <- 0.75
s <- sd2s(alpha=a, beta=b, gamma=c, delta=d)
stable::pstable(q, tail = s$tail, skew=s$skew, disp = s$disp, loc = s$loc)
stabledist::pstable(q, alpha=a, beta=b, gamma=c, delta=d, pm=1)
sd <- s2sd(tail = s$tail, skew=s$skew, disp = s$disp, loc = s$loc)
stabledist::pstable(q, alpha=sd$alpha, beta=sd$beta, gamma=sd$gamma, delta=sd$delta, pm=1)
## End(Not run)
```

---

Parameter\_Conversion\_Nolan\_pm1\_pm0

*Easy conversion of parameters between stabledist Nolan 1-parameterization and 0-parameterization*

---

## Description

pm0\_to\_pm1 has stabledist parameter inputs for pm=0 and returns pm=1 equivalent parameterization. pm1\_to\_pm0 has stabledist parameter inputs for pm=1 and returns pm=0 equivalent parameterization.

**Usage**

```
pm0_to_pm1(a0, b0, c0, d0)
```

```
pm1_to_pm0(a1, b1, c1, d1)
```

**Arguments**

a0	the stabledist 'alpha' for pm=0 in 'stabledist'
b0	the stabledist 'beta' for pm=0 in 'stabledist'
c0	the stabledist 'gamma' for pm=0 in 'stabledist'
d0	the stabledist 'delta' for pm=0 in 'stabledist'
a1	the stabledist 'alpha' for pm=1 in 'stabledist'
b1	the stabledist 'beta' for pm=1 in 'stabledist'
c1	the stabledist 'gamma' for pm=1 in 'stabledist'
d1	the stabledist 'delta' for pm=1 in 'stabledist'

**Details**

See table Table 3.1 on page 97 of Nolan (2020).

**Value**

pm0\_to\_pm1 has stabledist parameter inputs for pm=0 and returns pm=1 equivalent parameterization. pm1\_to\_pm0 has stabledist parameter inputs for pm=1 and returns pm=0 equivalent parameterization.

**References**

Nolan, John P. Univariate stable distributions. Berlin/Heidelberg, Germany: Springer, 2020.

**Examples**

```
## Not run: q <- -1
# nolan pm=1 parameters:
a1 <- 1.3
b1 <- -0.4
c1 <- 2
d1 <- 0.75
# Convert to nolan pm=0 parameters:
pm0 <- pm1_to_pm0(a1,b1,c1,d1)
a0 <- pm0$a0
b0 <- pm0$b0
c0 <- pm0$c0
d0 <- pm0$d0
# check:
stabledist::pstable(q, alpha=a1, beta=b1 , gamma=c1 , delta=d1, pm=1)
#> [1] 0.1965513
# only change delta=d0 for pm=0
```

```

stabledist::pstable(q, alpha=a1, beta=b1 , gamma=c1 , delta=d0, pm=0)
stabledist::pstable(q, alpha=a0, beta=b0 , gamma=c0 , delta=d0, pm=0)
#> [1] 0.1965513
stabledist::dstable(q, alpha=a1, beta=b1 , gamma=c1 , delta=d1, pm=1)
#> [1] 0.0572133
# only change delta=d0 for pm=0
stabledist::dstable(q, alpha=a1, beta=b1 , gamma=c1 , delta=d0, pm=0)
stabledist::dstable(q, alpha=a0, beta=b0 , gamma=c0 , delta=d0, pm=0)
#> [1] 0.0572133
## End(Not run)

```

---

stable.mode

*Mode of a Stable Distribution*


---

## Description

This function gives a reliable approximation to the mode of a stable distribution with location, dispersion, skewness and tail thickness specified by the parameters `loc`, `disp`, `skew` and `tail`. `tail` must be in (1,2).

## Usage

```
stable.mode(loc, disp, skew, tail)
```

## Arguments

<code>loc</code>	vector of (real) location parameters.
<code>disp</code>	vector of (positive) dispersion parameters.
<code>skew</code>	vector of skewness parameters (in [-1,1]).
<code>tail</code>	vector of parameters (in [1,2]) related to the tail thickness.

## Details

`loc` is a location parameter in the same way as the mean in the normal distribution: it can take any real value.

`disp` is a dispersion parameter in the same way as the standard deviation in the normal distribution: it can take any positive value.

`skew` is a skewness parameter: it can take any value in  $(-1, 1)$ . The distribution is right-skewed, symmetric and left-skewed when `skew` is negative, null or positive respectively.

`tail` is a tail parameter (often named the characteristic exponent): it can take any value in  $(0, 2)$  (with `tail=1` and `tail=2` yielding the Cauchy and the normal distributions respectively when symmetry holds).

The simplest empirical formula found to give a satisfactory approximation to the mode for values of `tail` in (1,2) is

$$loc + disp * a * skew * exp(-b * abs(skew))$$

with

$$a = 1.7665114 + 1.8417675 * tail - 2.2954390 * tail^2 + 0.4666749 * tail^3$$

and

$$b = -0.003142967 + 632.4715 * tail * \exp(-7.106035 * tail)$$

.

### Value

A list of size 3 giving the mode,  $a$  and  $b$ .

### Author(s)

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>) and Jim Lindsey.

### References

Lambert, P. and Lindsey, J.K. (1999) Analysing financial returns using regression models based on non-symmetric stable distributions. *Applied Statistics*, 48, 409-424.

### See Also

`stable` for more details on the stable distribution.

`stablereg` to fit generalized linear models for the stable distribution parameters.

### Examples

```
x <- seq(-5,5,by=0.1)
plot(x,dstable(x,loc=0,disp=1,skew=-1,tail=1.5),type="l",ylab="f(x)")
xhat <- stable.mode(loc=0,disp=1,skew=-1,tail=1.5)$ytilde
fxhat <- dstable(xhat,loc=0,disp=1,skew=-1,tail=1.5)
lines(c(xhat,xhat),c(0,fxhat),lty="dotted")
```

---

stablereg

*Stable Generalized Regression Models*

---

### Description

`stablereg` fits user specified generalized linear and nonlinear regression models based on the stable distribution to (uncensored, right and/or left censored) data. This allows the location, the dispersion, the skewness and the tails of the fitted stable distribution to vary with explanatory variables.

**Usage**

```
stablereg(  
  y = NULL,  
  loc = 0,  
  disp = 1,  
  skew = 0,  
  tail = 1.5,  
  oloc = TRUE,  
  odisp = TRUE,  
  oskew = TRUE,  
  otail = TRUE,  
  noopt = FALSE,  
  iloc = NULL,  
  idisp = NULL,  
  iskew = NULL,  
  itail = NULL,  
  loc_h = NULL,  
  disp_h = NULL,  
  skew_h = NULL,  
  tail_h = NULL,  
  weights = 1,  
  exact = FALSE,  
  delta = 1,  
  envir = parent.frame(),  
  integration = "Romberg",  
  eps = 1e-06,  
  up = 10,  
  npoint = 501,  
  hessian = TRUE,  
  llik.output = FALSE,  
  print.level = 0,  
  ndigit = 10,  
  steptol = 1e-05,  
  gradtol = 1e-05,  
  fscale = 1,  
  tysize = abs(p0),  
  stepmax = sqrt(p0 %*% p0),  
  iterlim = 100  
)
```

**Arguments**

**y** The response vector or a repeated data object. If the repeated data object contains more than one response variable, give that object in `envir` and give the name of the response variable to be used here.

For censored data, two columns with the second being the censoring indicator (1: uncensored, 0: right censored, -1: left censored.)

`loc`, `loc_h`, `oloc`, `iloc`

Describe the regression model fitted for the location parameter of the stable distribution, perhaps after transformation by the link function `loc_g` (set to the identity by default. The inverse link function is denoted by `loc_h`. Note that these functions cannot contain unknown parameters).

Two specifications are possible:

(1) `loc` is a linear or nonlinear language expression beginning with `~` or an R function, describing the regression function for the location parameter (after transformation by `loc_g`, the link function).

`iloc` is a vector of initial conditions for the parameters in the regression for this parameter.

`oloc` is a boolean indicating if an optimization of the likelihood has to be carried out on these parameters. If `oloc` is set to `TRUE`, a default zero value is considered for the starting values `iloc`. But if no optimization is desired on the location parameters, i.e. when the likelihood has to be evaluated or optimized at a fixed location, then `iloc` has to be explicitly specified.

(2) `loc` is a numeric expression (i.e. a scalar or a vector of the same size as the data vector `y`, or `y[, 1]` when censoring is considered).

If `oloc` is set to `TRUE`, i.e. when an optimization of the likelihood has to be carried out on the location parameter, then the location parameter (after transformation by the link function `loc_g`) is set to an unknown parameter with initial value equal to `iloc[1]` or `loc[1]` when `iloc` is not specified.

But when `oloc` is set to `FALSE`, i.e. when the likelihood has to be evaluated or optimized at a fixed location, then the transformed location is assumed to be equal to `loc` when it is of the same length as the data vector `y` (or `y[, 1]` when censoring is considered), and to `loc[1]` otherwise.

Specification (1) is especially useful in ANOVA-like situations where the location is assumed to change with the levels of some factor variable.

`disp`, `disp_h`, `odisp`, `idisp`

describe the regression model for the dispersion parameter of the fitted stable distribution, after transformation by the link function `disp_g` (set to the log function by default). The inverse link function is denoted by `disp_h`. Again these functions cannot contain unknown parameters. The same rules as above apply when specifying the generalized regression model for the dispersion parameter.

`skew`, `skew_h`, `oskew`, `iskew`

describe the regression model for the skewness parameter of the fitted stable distribution, after transformation by the link function `skew_g` (set to  $\log\{(1 + [.])/(1 - [.])\}$  by default). The inverse link function is denoted by `skew_h`. Again these functions cannot contain unknown parameters. The same rules as above apply when specifying the generalized regression model for the skewness parameter.

`tail`, `tail_h`, `otail`, `itail`

describe the regression model considered for the tail parameter of the fitted stable distribution, after transformation by the link function `tail_g` (set to  $\log\{([.] - 1)/(2 - [.])\}$  by default). The inverse link function is denoted by `tail_h`. Again these functions cannot contain unknown parameters). The same rules as

	above apply when specifying the generalized regression model for the tail parameter.
noopt	When set to TRUE, it forces oloc, odisp, oskew and otail to FALSE, whatever the user choice for these last three arguments. It is especially useful when looking for appropriate initial values for the regression model parameters, before undertaking the optimization of the likelihood.
weights	Weight vector.
exact	If TRUE, fits the exact likelihood function for continuous data by integration over intervals of observation, i.e. interval censoring.
delta	Scalar or vector giving the unit of measurement for each response value, set to unity by default. For example, if a response is measured to two decimals, $\text{delta}=0.01$ . If the response is transformed, this must be multiplied by the Jacobian. For example, with a log transformation, $\text{delta}=1/y$ . (The delta values for the censored response are ignored.) The transformation cannot contain unknown parameters.
envir	Environment in which model formulae are to be interpreted or a data object of class, repeated, tccov, or tvcov; the name of the response variable should be given in y. If y has class repeated, it is used as the environment.
integration, eps, up, npoint	integration indicates which algorithm must be used to evaluate the stable density when the likelihood is computed with exact set to FALSE. See the man page on stable for extra information.
hessian	Arguments controlling the optimization procedure <a href="#">nlm</a> .
llik.output	is TRUE when the likelihood has to be displayed at each iteration of the optimization.
print.level	Arguments controlling the optimization procedure <a href="#">nlm</a> .
ndigit	Arguments controlling the optimization procedure <a href="#">nlm</a> .
steptol	Arguments controlling the optimization procedure <a href="#">nlm</a> .
gradtol	Arguments controlling the optimization procedure <a href="#">nlm</a> .
fscale	Arguments controlling the optimization procedure <a href="#">nlm</a> .
typsize	Arguments controlling the optimization procedure <a href="#">nlm</a> .
stepmax	Arguments controlling the optimization procedure <a href="#">nlm</a> .
iterlim	Arguments controlling the optimization procedure <a href="#">nlm</a> .

### Value

A list of class `stable` is returned. The printed output includes the  $-\log$ -likelihood, the corresponding AIC, the maximum likelihood estimates, standard errors, and correlations. It also include all the relevant information calculated, including error codes.

### Warning

Because of the numerical integrations involved, convergence can be very sensitive to the initial parameter values supplied and to the settings of the arguments controlling [nlm](#). If `nlm` feeds extreme parameter values in the tails of the distribution to the likelihood function, the integration may hang for a long time.

**Author(s)**

Philippe Lambert (Catholic University of Louvain, Belgium, <phlambert@stat.ucl.ac.be>) and Jim Lindsey.

**References**

Lambert, P. and Lindsey, J.K. (1999) Analysing financial returns using regression models based on non-symmetric stable distributions. *Applied Statistics* 48, 409-424.

**See Also**

[lm](#), [glm](#), [stable](#) and [stable.mode](#).

**Examples**

```
## Share return over a 50 day period (see reference above)
# shares
y <- c(296,296,300,302,300,304,303,299,293,294,294,293,295,287,288,297,
305,307,307,304,303,304,304,309,309,309,307,306,304,300,296,301,298,
295,295,293,292,297,294,293,306,303,301,303,308,305,302,301,297,299)

# returns
ret <- (y[2:50]-y[1:49])/y[1:49]
# hist(ret, breaks=seq(-0.035,0.045,0.01))

day <- seq(0,0.48,by=0.01) # time measured in days/100
x <- seq(1,length(ret))-1

# Classic stationary normal model tail=2
print(z1 <- stablereg(y = ret, delta = 1/y[1:49],
loc = ~1, disp= ~1, skew = ~1, tail = tail_g(1.9999999),
iloc = 0, idisp = -3, iskew = 0, oskew = FALSE, otail = FALSE))

# Normal model (tail=2) with dispersion=disp_h(b0+b1*day)
print(z2 <- stablereg(y = ret, delta = 1/y[1:49], loc = ~day,
disp = ~1, skew = ~1, tail = tail_g(1.9999999), iloc = c(0.003,0),
idisp = -4.5, iskew = 0, oskew = FALSE, otail = FALSE))

# Stable model with loc(ation)=loc_h(b0+b1*day)
print(z3 <- stablereg(y = ret, delta = 1/y[1:49],
loc = ~day, disp = ~1, skew = ~1, tail = ~1,
iloc = c(0.001,-0.004), idisp = -4.8, iskew = 0, itail = 0.6))

# Stable model with disp(ersion)=disp_h(b0+b1*day)
print(z4 <- stablereg(y = ret, delta = 1/y[1:49],
loc = ~1, disp = ~day, skew = ~1, tail = ~1,
iloc = 0.003, idisp = c(-4.8,0), iskew = -0.03, itail = 1.6))

# Stable model with skew(ness)=skew_h(b0+b1*day)
# Evaluation at fixed parameter values (because noopt is set to TRUE)
print(z5 <- stablereg(y = ret, delta = 1/y[1:49],
```

```
loc = ~1, disp = ~1, skew = ~day, tail = ~1,  
iloc = 5.557e-04, idisp = -4.957, iskew = c(2.811,-2.158),  
itail = 1.57, noopt=TRUE))  
  
# Stable model with tail=tail_h(b0+b1*day)  
print(z6 <- stablereg(y = ret, delta = 1/y[1:49], loc = ret ~ 1,  
disp = ~1, skew = ~1, tail = ~day, iloc = 0.002,  
idisp = -4.8, iskew = -2, itail = c(2.4,-4), hessian=FALSE))
```

# Index

- \* **distribution**
  - stable.mode, 9
- \* **models**
  - stablereg, 10

aic.stable (stablereg), 10

deviance.stable (stablereg), 10

df.residual.stable (stablereg), 10

disp\_g (Links), 5

disp\_h (Links), 5

dstable, 2

fitted.stable (stablereg), 10

glm, 14

hstable (dstable), 2

Links, 5

lm, 14

loc\_g (Links), 5

loc\_h (Links), 5

nlm, 13

Parameter\_Conversion, 6

Parameter\_Conversion\_Nolan\_pm1\_pm0, 7

pm0\_to\_pm1

- (Parameter\_Conversion\_Nolan\_pm1\_pm0), 7

pm1\_to\_pm0

- (Parameter\_Conversion\_Nolan\_pm1\_pm0), 7

pstable (dstable), 2

qstable (dstable), 2

rstable (dstable), 2

s2sd (Parameter\_Conversion), 6

sd2s (Parameter\_Conversion), 6

skew\_g (Links), 5

skew\_h (Links), 5

stable.mode, 9

stablereg, 5, 10

tail\_g (Links), 5

tail\_h (Links), 5