

Package ‘mgwrsar’

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Type Package

Title GWR and MGWR with Spatial Autocorrelation

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Author Ghislain Geniaux and Davide Martinetti

Maintainer Ghislain Geniaux <ghislain.geniaux@inra.fr>

Description Functions for computing (Mixed) Geographically Weighted Regression with spatial autocorrelation, Geniaux and Martinetti (2017) <doi:10.1016/j.regsciurbeco.2017.04.001>.

License GPL (>= 2)

Depends Rcpp, sp, leaflet, Matrix

Imports spgwr, methods, doParallel, foreach, htmltools, nabor

Suggests knitr, rmarkdown

VignetteBuilder knitr

LinkingTo RcppEigen, Rcpp

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mgwrsar-package	<i>GWR and MGWR with Spatial Autocorrelation</i>
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Description

mgwrsar package proposes functions for estimating linear and local linear model with spatial autocorrelation. It allows to estimate linear and Spatial Autoregressive models with spatially varying coefficients. Models that mixed spatially varying and stationary coefficients can also be estimated.

```

Package:      mgwrsar
Type:         Package
Title:        GWR and MGWR with Spatial Autocorrelation
Version:      0.1-1
Date:         2021-04-26
Author:       Ghislain Geniaux and Davide Martinetti
Maintainer:   Ghislain Geniaux <ghislain.geniaux@inra.fr>
Description:  Functions for computing (Mixed) Geographically Weighted Regression with spatial autocorrelation, Ge
License:      GPL (>= 2)
Depends:      Rcpp, sp, leaflet, Matrix
Imports:      spgwr, methods, doParallel, foreach, htmltools, nabor
Suggests:    knitr, rmarkdown
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LinkingTo:    RcppEigen, Rcpp
RoxygenNote: 7.1.1
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LazyData:    true

```

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KNN	A function that returns a row normalized weight matrix based on k first neighbors, to be documented
MGWRSAR	Estimation of linear and local linear model with spatial autocorrelation model (mgwrsar).
bandwidths_mgwrsar	Select optimal kernel and bandwidth from a list

	of models, kernels and bandwidth candidates.
bisq	bisquare kernel
bisq_C	bisquare kernel, RcppEigen version
bisq_knn_C	Adaptive bisquare kernel
gauss_adapt	Adaptive gaussian kernel
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predict_mgwrsar	mgwrsar Model Predictions
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Details

The DESCRIPTION file: Functions for computing (Mixed) Geographycally Weighted Regression with spatial autocorrelation, Geniaux and Martinetti (2017) <doi:10.1016/j.regsciurbeco.2017.04.001>.

Author(s)

Ghislain Geniaux <ghislain.geniaux@hat.inra.fr> Davide Martinetti <davide.martinetti@hat.inra.fr>

References

Geniaux, G. and Martinetti, D.(2017). A new method for dealing simultaneously with spatial autocorrelation and spatial heterogeneity in regression models. *Regional Science and Urban Economics*. (<https://doi.org/10.1016/j.regsciurbeco.2017.04.001>)

See Also

[locfit](#)

Examples

```
library(mgwrsar)
## loading data example
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
## Creating a spatial weigth matrix (sparce dgCMatrix) of 8 nearest neighbors
```

```

W=KNN(coord,8)

ptm1<-proc.time()
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
fixed_vars=NULL,kernels=c('gauss'),H=0.13, Model = 'GWR',
control=list(SE=TRUE,doMC=FALSE))
(proc.time()-ptm1)[3]

summary_mgwrsar(model_GWR)
plot_mgwrsar(model_GWR,type='B_coef',var='X2')
plot_mgwrsar(model_GWR,type='t_coef',var='X2')

```

bandwidths_mgwrsar	<i>Select optimal kernel and bandwidth from a list of models, kernels and bandwidth candidates.</i>
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Description

Given a lm formula and a dataframe with coordinates, function `bandwidths_mgwrsar` optimizes the choice of a bandwidth value for each of the chosen models and kernel types using a leave-one-out cross validation criteria. A cross validated criteria is also used for selecting the best kernel type for a given model.

Usage

```
bandwidths_mgwrsar(formula, data,coord,
fixed_vars='Intercept',Models='GWR',Kernels='bisq',control=list(),control_search=list())
```

Arguments

<code>formula</code>	a formula.
<code>data</code>	a dataframe or a spatial dataframe (sp package).
<code>coord</code>	a dataframe or a matrix with coordinates, not required if data is a spatial dataframe, default NULL.
<code>fixed_vars</code>	a vector with the names of spatially constant coefficient. For mixed model, if NULL, the default # is set to 'Intercept'.
<code>Models</code>	character containing the type of model: Possible values are "OLS", "SAR", "GWR" (default), "MGWR" , "MGWRSAR_0_0_kv", "MGWRSAR_1_0_kv", "MGWRSAR_0_kc_kv", "MGWRSAR_1_kc_kv", "MGWRSAR_1_kc_0".
<code>Kernels</code>	a vector with the names of kernel type.
<code>control</code>	list of extra control arguments for MGWRSAR wrapper - see MGWRSAR help.
<code>control_search</code>	list of extra control arguments for bandwidth/kernel search - see section below. @details <ul style="list-style-type: none"> • <code>search_Wif TRUE</code> select an optimal spatial weight matrix using a moment estimator, default FALSE.

- kernels_wif search_W is TRUE, kernels_w is a vector of candidated kernels types, default NULL.
- lower_c lower bound for bandwidth search (default, the approximate first decile of distances).
- upper_c upper bound for bandwidth search (default, the approximate last decile of distances).
- lower_d lower bound for discrete kernels, default $2*k+1$.
- lower_dW lower bound for discrete kernels for finding optimal spatial weight matrix, default 2.
- lower_cW lower bound for bandwidth search for finding optimal spatial weight matrix (default approximate 0.005 quantile of distances).

Details

Given a lm formula and a dataframe with coordinates, for each model in Models for wich a bandwidth is required, this function optimizes the choice of a bandwidth value for each of the chosen models and kernel types using a leave one out cross validation criteria. A cross validated criteria is also used for selecting the best kernel type for a given model.

Value

bandwidths_MGWRSAR returns a list with:

config_model	a vector with information about model, optimal kernel and bandwidth for local regression, and optimal kernel and bandwith for spatial weight matrix W.
SSR	The sum of square residuals.
CV	The CV criteria.
model	objects of class mgwrsar estimated using config_model

References

- Geniaux, G. and Martinetti, D. (2017). A new method for dealing simultaneously with spatial auto-correlation and spatial heterogeneity in regression models. *Regional Science and Urban Economics*. (<https://doi.org/10.1016/j.regsciurbeco.2017.04.001>)
- McMillen, D. and Soppelsa, M. E. (2015). A conditionally parametric probit model of microdata land use in chicago. *Journal of Regional Science*, 55(3):391-415.
- Loader, C. (1999). *Local regression and likelihood*, volume 47. Springer New York.
- Franke, R. and Nielson, G. (1980). Smooth interpolation of large sets of scattered data. *International journal for numerical methods in engineering*, 15(11):1691-1704.

See Also

MGWRSAR, summary_mgwrsar, plot_mgwrsar, predict_mgwrsar, kernelW_C

Examples

```

library(mgwrsar)
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
W=KNN(coord,8)
#####
#### Finding bandwith by hand
#####

### kernel only space
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
fixed_vars=NULL,kernels=c('bisq_knn'),H=50,
Model = 'GWR', control=list(isgcv=FALSE,minv=1))
cat('SSR =')
summary_mgwrsar(model_GWR)

myCV<-function(H){model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,
coord=coord, fixed_vars=NULL,kernels=c('gauss_adapt'),H,
Model = 'GWR',control=list(isgcv=TRUE))
model_GWR$SSR
}

res=optimize(myCV,upper=500,lower=10)
res

## model with optimal bandwith with adaptative gaussian kernel

model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
fixed_vars=NULL,kernels=c ('gauss_adapt'),H=ceiling(res$minimum),
Model = 'GWR',control=list(isgcv=FALSE))
summary_mgwrsar(model_GWR)

#####
#### finding the bandwidths using bandwidths_mgwrsar
#####

mytab<-bandwidths_mgwrsar(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
fixed_vars='Intercept',Models=c('GWR','MGWR'),Kernels=c('bisq_knn','gauss_adapt','gauss'),
control=list(),control_search=list(lower_d=8,lower_c=0.03,upper_c=0.65))

names(mytab)
names(mytab[['GWR']])

mytab[['GWR']]$config_model
mytab[['GWR']]$CV
summary(mytab[['GWR']]$model$Betav)

mytab[['GWR_2']]$config_model
mytab[['GWR_2']]$CV

```

```

summary(mytab[['GWR_2']]$model$Betav)

mytab[['GWR_3']]$config_model
mytab[['GWR_3']]$CV
summary(mytab[['GWR_3']]$model$Betav)

mytab[['MGWR']]$config_model
mytab[['MGWR']]$CV
mytab[['MGWR']]$model$Betac
summary(mytab[['MGWR']]$model$Betav)

mytab[['MGWR_2']]$config_model
mytab[['MGWR_2']]$CV
mytab[['MGWR_2']]$model$Betac
summary(mytab[['MGWR_2']]$model$Betav)

mytab[['MGWR_3']]$config_model
mytab[['MGWR_3']]$CV
mytab[['MGWR_3']]$model$Betac
summary(mytab[['MGWR_3']]$model$Betav)

mytab2<-bandwidths_mgwsar(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
  fixed_vars='Intercept',Models=c('MGWRSAR_0_kc_kv'),Kernels=c('gauss_adapt'),
  control=list(),control_search=list(search_W=TRUE,kernels_w=c('bisq','gauss_adapt')))

mytab2[['MGWRSAR_0_kc_kv']]$config_model
mytab2[['MGWRSAR_0_kc_kv']]$CV
mytab2[['MGWRSAR_0_kc_kv']]$model$Betac
summary(mytab2[['MGWRSAR_0_kc_kv']]$model$Betav)

```

bisq

bisquare kernel

Description

bisquare kernel

Usage

```
bisq(d, h)
```

Arguments

d	a vector of distance
h	a distance bandwidth

Value

a vector of weight

Examples

```
w=bisq(-30:30, 20)
plot(-30:30,w,type='l')
abline(v=-20)
abline(v=20)
```

bisq_C

bisquare kernel, RcppEigen version

Description

bisquare kernel, RcppEigen version

Usage

```
bisq_C(d, h, Minv)
```

Arguments

d	a vector of distance
h	a distance bandwidth
Minv	Minimal number of non null weight (neighbor)

Value

a vector of weight

Examples

```
w=bisq_C(1:100,20,0)
plot(1:100,w,type='l')
```

bisq_knn_C	<i>Adaptive bisquare kernel</i>
------------	---------------------------------

Description

Adaptive bisquare kernel

Usage

```
bisq_knn_C(d,h)
```

Arguments

d	a vector of distance
h	bandwidth size expressed in number of neighbors

Value

a vector of weight

Examples

```
w=bisq_knn_C(-30:30,20)
plot(-30:30,w,type='l')
abline(v=-10)
abline(v=10)
```

gauss_adapt	<i>Adaptive gaussian kernel</i>
-------------	---------------------------------

Description

Adaptive gaussian kernel

Usage

```
gauss_adapt(d, h)
```

Arguments

d	a vector of distance
h	bandwidth size expressed in number of neighbors

Value

a vector of weight

Examples

```
w=gauss_adapt(-30:30,20)
plot(-30:30,w,type='l')
abline(v=-10)
abline(v=10)
```

gauss_adapt_C

Adaptive gaussian kernel, RcppEigen version

Description

Adaptive gaussian kernel, RcppEigen version

Usage

```
gauss_adapt_C(d, h)
```

Arguments

d a vector of distance
h bandwidth size expressed in number of neighbors

Value

a vector of weight

Examples

```
w=gauss_adapt_C(-30:30,20)
plot(-30:30,w,type='l')
abline(v=-10)
abline(v=10)
```

kernelW_C	<i>Computes weight matrix for a given kernel and bandwidth</i>
-----------	--

Description

kernelW_C is a function that computes weight matrix for a given kernel and bandwidth

Usage

```
kernelW_C(XX, hh, MykernelS, isgcv_, Type, Minv, maxknn_,
          NmaxDist_, TIME, Decay, DDiagNull)
```

Arguments

XX	a matrix with coordinates.
hh	a bandwidth value
MykernelS	a kernel type between ('bin','bisq','gauss','gauss_adapt', 'knn','bisq_knn')
isgcv_	default FALSE for computing CV criteria (for example for selecting optimal bandwidth).
Type	Kernel type.
Minv,	minimum number of neighbors when using distance kernels.
maxknn_	default 500, when n>NmaxDist only maxknn first neighbours are used for computation distance
NmaxDist_	default 5000, when n>NmaxDist only maxknn first neighbours are used for computing distance
TIME	default FALSE, time is used for computing weights if TIME is TRUE weight for future observation are set to zero
Decay	time decay when time is used for computing weights.
DDiagNull	default FALSE, if TRUE diagonal has zero weights.

Value

kernelW_C returns a sparse weight matrix

See Also

MGWRSAR, bandwidths_mgwrsar, summary_mgwrsar, plot_mgwrsar, predict_mgwrsar

Examples

```
data(mydata); coord=as.matrix(mydata[,c("x_lat", "y_lon")]);
W=kernelW_C(coord,100, 'bisq_knn', FALSE, 'GD', 1, 500, 5000, FALSE, 0, FALSE)
plot(D_dense_C(coord[1,1], coord[1,2], coord[,1], coord[,2]), W[1,])
```

KNN	<i>A function that returns a row normalized weight matrix based on k first neighbors, to be documented</i>
-----	--

Description

A function that returns a row normalized weight matrix based on k first neighbors, to be documented

Usage

```
KNN(coord,h,diagnull=TRUE,kerne1='knn',query=NULL)
```

Arguments

coord	matrix of coordinates
h	a bandwidth
diagnull	0 on diagonal, default TRUE
kernel	kernel type ('bisq','bisq_knn','gauss','gauss_adapt','knn')
query	an index of neighbors to consider, if NULL all observation are used.

Value

a row nomralized weight dgCmatrix

Examples

```
data(mydata)
coord=as.matrix(mydata[,c("x_lat","y_lon")])
W=KNN(coord,8)
which(W[1,]>0)
W[1,W[1,]>0]
```

MGWRSAR	<i>Estimation of linear and local linear model with spatial autocorrelation model (mgwrsar).</i>
---------	--

Description

MGWRSAR is is a wrapper function for estimating linear and local linear models with spatial autocorrelation (SAR models with spatially varying coefficients).

Usage

```
MGWRSAR(formula, data, coord, fixed_vars=NULL, kernels, H,
Model='GWR', control=list())
```

Arguments

formula	a formula.
data	a dataframe or a spatial dataframe (sp package).
coord	default NULL, a dataframe or a matrix with coordinates, not required if data is a spatial dataframe.
fixed_vars	a vector with the names of spatially constant coefficient for mixed model. All other variables present in formula are supposed to be spatially varying. If empty or NULL (default), all variables in formula are supposed to be spatially varying.
kernels	vector containing the kernel types. Possible types: k nearest neighbors ("knn"), bisquare ("bisq"), adaptative bisquare ("bisq_knn"), gaussian ("gauss"), adaptative gaussian ("gauss_adapt").
H	vector containing the bandwidth parameters for the kernel functions.
Model	character containing the type of model: Possible values are "OLS", "SAR", "GWR" (default), "MGWR" , "MGWRSAR_0_0_kv", "MGWRSAR_1_0_kv", "MGWRSAR_0_kc_kv", "MGWRSAR_1_kc_kv", "MGWRSAR_1_kc_0". See Details for more explanation.
control	list of extra control arguments for MGWRSAR wrapper - see Details below

Details

- Z a matrix of variables for generalized kernel product, default NULL.
- W a row-standardized spatial weight matrix for Spatial Aurocorrelation, default NULL.
- type verbose mode, default FALSE.
- kernel_w the type of kernel for computing W, default NULL.
- h_w the bandwidth value for computing W, default 0.
- Method estimation technique for computing the models with Spatial Dependence. '2SLS' or 'B2SLS', default '2SLS'.
- isgcv computing CV criteria (for example for selecting optimal bandwidth), default FALSE.
- isfgev if TRUE, simplify the computation of CV criteria (remove or not i when using local instruments for model with lambda spatially varying), default TRUE.
- maxknn when $n > N_{\maxDist}$, only the maxknn first neighbours are used for distance computation, default 500.
- NmaxDist when $n > N_{\maxDist}$ only the maxknn first neighbours are used for distance computation, default 5000
- verbose verbose mode, default FALSE.

Value

MGWRSAR returns an object of class `mgwrsar` with at least the following components:

<code>Betav</code>	matrix of coefficients of $\dim(n, k_v) \times k_v$.
<code>Betac</code>	vector of coefficients of length k_c .
<code>Model</code>	The sum of square residuals.
<code>Y</code>	The dependent variable.
<code>XC</code>	The explanatory variables with constant coefficients.
<code>XV</code>	The explanatory variables with varying coefficients.
<code>X</code>	The explanatory variables.
<code>W</code>	The spatial weight matrix for spatial dependence.
<code>isgcv</code>	if <code>gcv</code> has been computed.
<code>edf</code>	The estimated degrees of freedom.
<code>formula</code>	The formula.
<code>data</code>	The dataframe used for computation.
<code>Method</code>	The type of model.
<code>coord</code>	The spatial coordinates of observations.
<code>H</code>	The bandwidth vector.
<code>fixed_vars</code>	The names of constant coefficients.
<code>kernels</code>	The kernel vector.
<code>SSR</code>	The sum of square residuals.
<code>residuals</code>	The vector of residuals.
<code>fit</code>	the vector of fitted values.
<code>sev</code>	local standard error of parameters.

MGWRSAR is a wrapper function for estimating linear and local linear model with spatial autocorrelation that allows to estimate the following models : $y = \beta_c X_c + \epsilon_i$ (OLS)

$$y = \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (GWR)}$$

$$y = \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR)}$$

$$y = \lambda W y + \beta_c X_c + \epsilon_i \text{ (MGWR-SAR(0,k,0))}$$

$$y = \lambda W y + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(0,0,k))}$$

$$y = \lambda W y + \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(0,k_c,k_v))}$$

$$y = \lambda(u_i, v_i)W y + \beta_c X_c + \epsilon_i \text{ (MGWR-SAR(1,k,0))}$$

$$y = \lambda(u_i, v_i)W y + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(1,0,k))}$$

$$y = \lambda(u_i, v_i)W y + \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(1,k_c,k_v))}$$

When model imply spatial autocorrelation, a row normalized spatial weight matrix must be provided. 2SLS and Best 2SLS method can be used. When model imply local regression, a bandwidth and a kernel type must be provided. Optimal bandwidth can be estimated using `bandwidths_mgwrsar` function. When model imply mixed local regression, the names of stationary covariates must be provided.

#' In addition to the ability of considering spatial autocorrelation in GWR/MGWR like models, MGWRSAR function introduces several useful technics for estimating local regression with space coordinates:

- it uses RCCP and RCCPeigen code that speed up computation and allows parallel computing via doMC package;
- it allows to drop out variables with not enough local variance in local regression, which allows to consider dummies in GWR/MGWR framework without trouble.
- it allows to drop out local outliers in local regression.
- it allows to consider additional variable for kernel, including time (asymetric kernel) and categorical variables (see Li and Racine 2010). Experimental version.

References

Geniaux, G. and Martinetti, D. (2017). A new method for dealing simultaneously with spatial autocorrelation and spatial heterogeneity in regression models. *Regional Science and Urban Economics*. (<https://doi.org/10.1016/j.regsciurbeco.2017.04.001>)

McMillen, D. and Soppelsa, M. E. (2015). A conditionally parametric probit model of microdata land use in chicago. *Journal of Regional Science*, 55(3):391-415.

Loader, C. (1999). *Local regression and likelihood*, volume 47. springer New York.

Franke, R. and Nielson, G. (1980). Smooth interpolation of large sets of scattered data. *International journal for numerical methods in engineering*, 15(11):1691-1704.

See Also

bandwidths_mgwrsar, summary_mgwrsar, plot_mgwrsar, predict_mgwrsar, kernelW_C

Examples

```
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata, coord=coord,
fixed_vars=NULL, kernels=c('gauss_knn'),
H=120, Model = 'GWR', control=list())
summary_mgwrsar(model_GWR)

W=KNN(coord,8)
model_MGWRSAR_0_kc_kv<-MGWRSAR(formula = 'Y_mgwrsar_0_kc_kv~X1+X2+X3', data = mydata,
coord=coord, fixed_vars='Intercept', kernels=c('gauss_adapt'),
H=120, Model = 'MGWRSAR_0_kc_kv', control=list(W=W))
summary_mgwrsar(model_MGWRSAR_0_kc_kv)
```

mgwrsar_bootstrap_test

A bootstrap test for Betas for mgwrsar class model.

Description

A bootstrap test for Betas for mgwrsar class model.

Usage

```
mgwrsar_bootstrap_test(x0,x1,B=100,domc=FALSE,ncore=1,
  type='standard',eps='H1',df='H1',focal='median',D=NULL)
```

Arguments

x0	The H0 mgwrsar model
x1	The H1 mgwrsar model
B	number of bootstrap repetitions, default 100
domc	If TRUE, doParallel parallelization
ncore	number of cores
type	type of bootstap : 'wild','Rademacher','spatial' or 'standard' (default)
eps	Hypothesis under wich residuals are simulated, 'H0' or 'H1' (default)
df	Hypothesis under wich degree of freedom is estimated.
focal	see sample_stat help
D	A matrix of distance

Value

The value of the statistics test and a p ratio.

See Also

mgwrsar_bootstrap_test_all

Examples

```
data(mydata)
coord=as.matrix(mydata[,c("x_lat","y_lon")])
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata, coord=coord,
  fixed_vars=NULL,kernels=c('gauss_adapt'), H=20,
  Model = 'GWR',control=list(SE=TRUE))

model_MGWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata, coord=coord,
  fixed_vars='Intercept',kernels=c('gauss_adapt'), H=20,
```



```
Model = 'MGWR',control=list(SE=TRUE))
mgwrsar_bootstrap_test(model_MGWR,model_GWR,domc=FALSE,B=30)
```

mgwrsar_bootstrap_test_all

A bootstrap test for testing nullity of all Betas for mgwrsar class model,

Description

A bootstrap test for testing nullity of all Betas for mgwrsar class model,

Usage

```
mgwrsar_bootstrap_test_all(model,B=100,domc=NULL)
```

Arguments

model	A mgwrsar model
B	number of bootstrap replications, default 100
domc	If TRUE, doMC parallelization

Value

a matrix with statistical test values and p ratios

See Also

mgwrsar_bootstrap_test

mydata

mydata is a simulated data set of a mgwrsar model

Description

mydata is a simulated data set of a mgwrsar model

Usage

```
mydata
```

Format

An object of class data.frame with 1000 rows and 22 columns.

Author(s)

Ghislain Geniaux and Davide Martinetti <ghislain.geniaux@inra.fr>

References

<https://www.sciencedirect.com/science/article/pii/S0166046216302381>

plot_mgwrsar	<i>plot_mgwrsar plots the value of local paramaters of a mgwrsar models using a leaflet map.</i>
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Description

plot_mgwrsar plots the value of local paramaters of a mgwrsar models using a leaflet map.

Usage

```
plot_mgwrsar(model, type='coef', var=NULL, SP=NULL, SP_id=NULL,
proj=NULL, mypalette= "RdYlGn", opacity=1, fopacity=1, radius=1500)
```

Arguments

model	a mgwsar model.
type	default 'coef', for plotting the value of the coefficients. Local t-Student could also be plot using 't_coef'.
var	Names of variable to plot.
SP	A spdf object.
SP_id	Id regions for spdf object.
proj	A CRS projection.
mypalette	A leaflet palette.
opacity	Opacity of border color.
fopacity	Opacity of fill color.
radius	radius of circle for plot of points.

Value

A Interactive Web Maps with local parameters plot and Open Street Map layer.

See Also

MGWRSAR, bandwidths_mgwrsar, summary_mgwrsar, predict_mgwrsar, kernelW_C

Examples

```

library(mgwrsar)
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
W=KNN(coord,4)
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata, coord=coord,
fixed_vars=NULL,kernels=c('gauss'),H=0.13,
Model = 'GWR', control=list(SE=TRUE))
summary_mgwrsar(model_GWR)
plot_mgwrsar(model_GWR,type='t_coef',var='X1')

```

predict_mgwrsar	<i>mgwrsar Model Predictions</i>
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Description

predict_mgwrsar is a function for computing predictions of a mgwrsar models. It uses Best Linear Unbiased Predictor for mgwrsar models with spatial autocorrelation.

Usage

```

predict_mgwrsar(model, newdata, newdata_coord, W = NULL,
type = "BPN", h_w = 100, kernel_w = "knn", k_extra = 12,
kernel_extra = "sheppard")

```

Arguments

model	a model of mgwrsar class.
newdata	a matrix or data.frame of new data.
newdata_coord	a matrix of new coordinates.
W	the spatial weight matrix for models with spatial autocorrelation.
type	Type for BLUP estimator, default "BPN". If NULL use predictions without spatial bias correction.
h_w	bandwidth for constructing W, if W is NULL.
kernel_w	kernel for constructing W, if W is NULL.
k_extra	number of neighbors for local parameter extrapolation, default 12.
kernel_extra	kernel for local parameter extrapolation, default sheppard kernel.

Value

A vector of predictions.

See Also

MGWRSAR, bandwidths_mgwrsar, summary_mgwrsar, plot_mgwrsar, kernelW_C

Examples

```
library(mgwrsar)
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
W=KNN(coord,2)
model_GWR_insample<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata[1:800,],
  coord=coord[1:800,], fixed_vars=NULL, kernels=c('gauss_adapt'), H=50,
  Model = 'GWR', control=list())
Y_pred=predict_mgwrsar(model_GWR_insample, newdata=mydata[801:1000,],
  newdata_coord=coord[801:1000,], k_extra = 8, kernel_extra = "sheppard")
head(Y_pred)
head(mydata$Y_gwr[801:1000])
sqrt(mean((mydata$Y_gwr[801:1000]-Y_pred)^2))

## predict with spatial autocorrelation
model_MGWRSAR_1_0_kv_insample<-MGWRSAR(formula = 'Y_mgwrsar_1_0_kv~X1+X2+X3', data = mydata[1:800,],
  coord=coord[1:800,], fixed_vars=NULL, kernels=c('gauss_adapt'), H=50,
  Model = 'MGWRSAR_1_0_kv', control=list(W=W[1:800,1:800], Lambdacor=TRUE, SE=TRUE))
summary_mgwrsar(model_MGWRSAR_1_0_kv_insample)

## with BLUP
Y_pred=predict_mgwrsar(model_MGWRSAR_1_0_kv_insample, newdata=mydata[801:1000,],
  newdata_coord=coord[801:1000,], k_extra = 12, W = W,
  type = "BPN", kernel_extra = "sheppard")
head(Y_pred)
head(mydata$Y_gwr[801:1000])
sqrt(mean((mydata$Y_gwr[801:1000]-Y_pred)^2))

## without BLUP
Y_pred=predict_mgwrsar(model_MGWRSAR_1_0_kv_insample, newdata=mydata[801:1000,],
  newdata_coord=coord[801:1000,], k_extra = 12, W = W,
  type = "TC", kernel_extra = "sheppard")
head(Y_pred)
head(mydata$Y_mgwrsar_1_0_kv[801:1000])
sqrt(mean((mydata$Y_mgwrsar_1_0_kv[801:1000]-Y_pred)^2))
```

summary_mgwrsar

Print a summary of mgwrsar models

Description

Print a summary of mgwrsar models

Usage

```
summary_mgwrsar(model)
```

Arguments

model a model of class mgwrsar

Value

a summary of mgwrsar models

See Also

MGWRSAR, bandwidths_mgwrsar, plot_mgwrsar, predict_mgwrsar, kernelW_C

Examples

```
## Not run:
library(mgwrsar)
data(mydata)
coord=as.matrix(mydata[,c("x_lat", "y_lon")])
W=KNN(coord,8)
model_GWR<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,coord=coord,
  fixed_vars=NULL,kernels=c('gauss'),H=0.13, Model = 'GWR',
  control=list(SE=TRUE))
summary_mgwrsar(model_GWR)

## End(Not run)
```

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