

Package ‘hergm’

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Title Hierarchical Exponential-Family Random Graph Models

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Description Hierarchical exponential-family random graph models with local dependence.

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bali	<i>Bali terrorist network</i>
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Description

The network corresponds to the contacts between the 17 terrorists who carried out the bombing in Bali, Indonesia in 2002. The network is taken from Koschade (2006).

Usage

```
data(bali)
```

Value

Undirected network.

References

Koschade, S. (2006). A social network analysis of Jemaah Islamiyah: The applications to counter-terrorism and intelligence. *Studies in Conflict and Terrorism*, 29, 559–575.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(bali)
object <- hergm(bali ~ edges_ij + triangle_ijk, max_number=3, method="bayes")
summary(object)

## End(Not run)
```

bunt	<i>Van de Bunt friendship network</i>
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Description

Van de Bunt (1999) and Van de Bunt et al. (1999) collected data on friendships between 32 freshmen at a European university at 7 time points. Here, the last time point is used. A directed edge from student *i* to *j* indicates that student *i* considers student *j* to be a “friend” or “best friend”.

Usage

```
data(bunt)
```

Value

Directed network.

References

Van de Bunt, G. G. (1999). Friends by choice. An Actor-Oriented Statistical Network Model for Friendship Networks through Time. Thesis Publishers, Amsterdam.

Van de Bunt, G. G., Van Duijn, M. A. J., and T. A. B. Snijders (1999). Friendship Networks Through Time: An Actor-Oriented Statistical Network Model. Computational and Mathematical Organization Theory, 5, 167–192.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(bunt)
object <- hergm(bunt ~ edges_ij + mutual_ij + ttriple_ijk, max_number=32, method="bayes")
summary(object)

## End(Not run)
```

example

Example network

Description

Example data set: synthetic, undirected network with 15 nodes.

Usage

```
data(example)
```

Value

Undirected network.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_i, max_number=3)
summary(object)

## End(Not run)
```

gof.hergm

Goodness-of-fit

Description

The function `gof.hergm` accepts an object of class `hergm` as argument and assesses the goodness-of-fit of the model estimated by function `hergm`.

Usage

```
## S3 method for class 'hergm'
gof(object, sample_size = 1000, ...)
```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>sample_size</code>	number of samples to generate.
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

Value

The function `gof.hergm` returns a list with components:

<code>component.number</code>	number of components.
<code>max.component.size</code>	size of largest component.
<code>distance</code>	geodesic distance of pairs of nodes.
<code>degree</code>	degree of nodes.
<code>edges</code>	number of edges.
<code>stars</code>	number of 2-stars.
<code>triangle</code>	number of triangles.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm, simulate.hergm

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_i)
gof(object)

## End(Not run)
```

hergm	<i>Hierarchical exponential-family random graph models with local dependence</i>
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Description

The function `hergm` estimates and simulates three classes of hierarchical exponential-family random graph models:

1. The p_1 model of Holland and Leinhardt (1981) in exponential-family form and extensions by Vu, Hunter, and Schweinberger (2013) and Schweinberger, Petrescu-Prahova, and Vu (2014) to both directed and undirected random graphs with additional model terms, with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`).
2. The stochastic block model of Snijders and Nowicki (1997) and Nowicki and Snijders (2001) in exponential-family form and extensions by Vu, Hunter, and Schweinberger (2013) and Schweinberger, Petrescu-Prahova, and Vu (2014) with additional model terms, with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`).
3. The exponential-family random graph models with local dependence of Schweinberger and Handcock (2015), with and without covariates, and with parametric and nonparametric priors (see `arcs_i`, `arcs_j`, `edges_i`, `edges_ij`, `mutual_i`, `mutual_ij`, `twostar_ijk`, `triangle_ijk`, `ttriple_ijk`, `ctriple_ijk`). The exponential-family random graph models with local dependence replace the long-range dependence of conventional exponential-family random graph models by short-range dependence. Therefore, exponential-family random graph models with local dependence replace the strong dependence of conventional exponential-family random graph models by weak dependence, reducing the problem of model degeneracy (Handcock, 2003; Schweinberger, 2011) and improving goodness-of-fit (Schweinberger and Handcock, 2015). In addition, exponential-family random graph models with local dependence satisfy a weak form of self-consistency in the sense that these models are self-consistent under neighborhood sampling (Schweinberger and Handcock, 2015), which enables consistent estimation of neighborhood-dependent parameters (Schweinberger and Stewart, 2017; Schweinberger, 2017).

Usage

```
hergm(formula,  
      max_number = 2,  
      hierarchical = TRUE,  
      parametric = FALSE,  
      parameterization = "offset",  
      initialize = FALSE,  
      initialization_method = 1,  
      estimate_parameters = TRUE,  
      initial_estimate = NULL,  
      n_em_step_max = 100,  
      max_iter = 4,  
      perturb = FALSE,  
      scaling = NULL,  
      alpha = NULL,  
      alpha_shape = NULL,  
      alpha_rate = NULL,  
      eta = NULL,  
      eta_mean = NULL,  
      eta_sd = NULL,  
      eta_mean_mean = NULL,  
      eta_mean_sd = NULL,  
      eta_precision_shape = NULL,  
      eta_precision_rate = NULL,  
      mean_between = NULL,  
      indicator = NULL,  
      parallel = 1,  
      simulate = FALSE,  
      method = "ml",  
      seeds = NULL,  
      sample_size = NULL,  
      sample_size_multiplier_blocks = 20,  
      NR_max_iter = 200,  
      NR_step_len = NULL,  
      NR_step_len_multiplier = 0.2,  
      interval = 1024,  
      burnin = 16*interval,  
      mh.scale = 0.25,  
      variational = FALSE,  
      temperature = c(1,100),  
      predictions = FALSE,  
      posterior.burnin = 2000,  
      posterior.thinning = 1,  
      relabel = 1,  
      number_runs = 1,  
      verbose = 0,  
      ...)
```

Arguments

formula	formula of the form $\text{network} \sim \text{terms}$. <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> . Possible terms can be found in <code>ergm.terms</code> and <code>hergm.terms</code> .
max_number	maximum number of blocks.
hierarchical	hierarchical prior; if <code>hierarchical = TRUE</code> , prior is hierarchical (i.e., the means and variances of block parameters are governed by a hyper-prior), otherwise non-hierarchical (i.e., the means and variances of block parameters are fixed).
parametric	parametric prior; if <code>parametric = FALSE</code> , prior is truncated Dirichlet process prior, otherwise parametric Dirichlet prior.
parameterization	<p>There are three possible parameterizations of within-block terms when using <code>method == "ml"</code>. Please note that between-block terms do not use these parameterizations, and <code>method == "bayes"</code> allows the parameters of all within-block terms to vary across blocks and hence does not use them either.</p> <ul style="list-style-type: none"> • <code>standard</code>: The parameters of all within-block terms are constant across blocks. • <code>offset</code>: The offset $\log(n[k])$ is subtracted from the parameters of the within-block edge terms and is added to the parameters of the within-block mutual edge terms along the lines of Krivitsky, Handcock, and Morris (2011), Krivitsky and Kolaczyk (2015), and Stewart, Schweinberger, Bojanowski, and Morris (2019), where $n[k]$ is the number of nodes in block k. The parameters of all other within-block terms are constant across blocks. • <code>size</code>: The parameters of all within-block terms are multiplied by $\log(n[k])$ along the lines of Babkin and Schweinberger (2019), where $n[k]$ is the number of nodes in block k.
initialize	if <code>initialize = TRUE</code> , initialize block memberships of nodes.
initialization_method	if <code>initialization_method = 1</code> , block memberships of nodes are initialized by walk trap; if <code>initialization_method = 2</code> , block memberships of nodes are initialized by spectral clustering.
estimate_parameters	if <code>method = "ml"</code> and <code>estimate_parameters = TRUE</code> , estimate parameters.
initial_estimate	if <code>method = "ml"</code> and <code>estimate_parameters = TRUE</code> , specifies starting point.
n_em_step_max	if <code>method = "ml"</code> , maximum number of iterations of Generalized Expectation Maximization algorithm estimating the block structure.
max_iter	if <code>method = "ml"</code> , maximum number of iterations of Monte Carlo maximization algorithm estimating parameters given block structure.
perturb	if <code>initialize = TRUE</code> and <code>perturb = TRUE</code> , initialize block memberships of nodes by spectral clustering and perturb.

<code>scaling</code>	if <code>scaling = TRUE</code> , use size-dependent parameterizations which ensure that the scaling of between- and within-block terms is consistent with sparse edge terms.
<code>alpha</code>	concentration parameter of truncated Dirichlet process prior of natural parameters of exponential-family model.
<code>alpha_shape, alpha_rate</code>	shape and rate parameter of Gamma prior of concentration parameter.
<code>eta</code>	the parameters of <code>ergm</code> . terms and <code>hergm</code> . terms; the parameters of <code>hergm</code> . terms must consist of <code>max_number</code> within-block parameters and one between-block parameter.
<code>eta_mean, eta_sd</code>	means and standard deviations of Gaussian baseline distribution of Dirichlet process prior of natural parameters.
<code>eta_mean_mean, eta_mean_sd</code>	means and standard deviations of Gaussian prior of mean of Gaussian baseline distribution of Dirichlet process prior.
<code>eta_precision_shape, eta_precision_rate</code>	shape and rate (inverse scale) parameter of Gamma prior of precision parameter of Gaussian baseline distribution of Dirichlet process prior.
<code>mean_between</code>	if <code>simulate = TRUE</code> and <code>eta = NULL</code> , then <code>mean_between</code> specifies the mean-value parameter of edges between blocks.
<code>indicator</code>	if the indicators of block memberships of nodes are specified as integers between 1 and <code>max_number</code> , the specified indicators are fixed, which is useful when indicators of block memberships are observed (e.g., in multilevel networks).
<code>parallel</code>	number of computing nodes; if <code>parallel > 1</code> , <code>hergm</code> is run on <code>parallel</code> computing nodes.
<code>simulate</code>	if <code>simulate = TRUE</code> , simulate networks from model, otherwise estimate model given observed network.
<code>method</code>	if <code>method = "bayes"</code> , Bayesian methods along the lines of Schweinberger and Handcock (2015) and Schweinberger and Luna (2018) are used; otherwise, if <code>method = "ml"</code> , then approximate maximum likelihood methods along the lines of Babkin and Schweinberger (2019) are used; note that Bayesian methods are the gold standard but are too time-consuming to be applied to networks with more than 100 nodes, whereas the approximate maximum likelihood methods can be applied to networks with thousands of nodes.
<code>seeds</code>	seed of pseudo-random number generator; if <code>parallel > 1</code> , number of seeds must equal number of computing nodes.
<code>sample_size</code>	if <code>simulate = TRUE</code> , number of network draws, otherwise number of posterior draws; if <code>parallel > 1</code> , number of draws on each computing node.
<code>sample_size_multiplier_blocks</code>	if <code>method = "ml"</code> , multiplier of the number of network draws from within-block subgraphs; the total number of network draws from within-block subgraphs is <code>sample_size_multiplier_blocks * number of possible edges of largest within-block subgraph</code> ; if <code>sample_size_multiplier_blocks = NULL</code> , then total number of network draws from within-block subgraphs is <code>sample_size</code> .

NR_max_iter	if method = "ml", the maximum number of iterations to be used in the estimation of parameters.
NR_step_len	if method = "ml", the step-length to be used for increments in the estimation of parameters. If set to NULL (default), then an adaptive step length procedure is used.
NR_step_len_multiplier	if method = "ml", multiplier for adjusting the step-length in the estimation procedure after a divergent increment.
interval	if simulate = TRUE, number of proposals between sampled networks.
burnin	if simulate = TRUE, number of burn-in iterations.
mh.scale	if simulate = FALSE, scale factor of candidate-generating distribution of Metropolis-Hastings algorithm.
variational	if simulate = FALSE and variational = TRUE, variational methods are used to construct the proposal distributions of block memberships of nodes; limited to selected models.
temperature	if simulate = FALSE and variational = TRUE, minimum and maximum temperature; the temperature is used to melt down the proposal distributions of indicators, which are based on the full conditional distributions of indicators but can have low entropy, resulting in slow mixing of the Markov chain; the temperature is a function of the entropy of the full conditional distributions and is designed to increase the entropy of the proposal distributions, and the minimum and maximum temperature are user-defined lower and upper bounds on the temperature.
predictions	if predictions = TRUE and simulate = FALSE, returns posterior predictions of statistics in the model.
posterior.burnin	number of posterior burn-in iterations; if computing is parallel, posterior.burnin is applied to the sample generated by each processor; please note that hergm returns $\min(\text{sample_size}, 10000)$ sample points and the burn-in is applied to the sample of size $\min(\text{sample_size}, 10000)$, therefore posterior.burnin should be smaller than $\min(\text{sample_size}, 10000)$.
posterior.thinning	if posterior.thinning > 1, every posterior.thinning-th sample point is used while all others discarded; if computing is parallel, posterior.thinning is applied to the sample generated by each processor; please note that hergm returns $\min(\text{sample_size}, 10000)$ sample points and the thinning is applied to the sample of size $\min(\text{sample_size}, 10000) - \text{posterior.burnin}$, therefore posterior.thinning should be smaller than $\min(\text{sample_size}, 10000) - \text{posterior.burnin}$.
relabel	if relabel > 0, relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) (relabel = 1) or Peng and Carvalho (2016) (relabel = 2).
number_runs	if relabel = 1, number of runs of relabeling algorithm.
verbose	if verbose = -1, no console output; if verbose = 0, short console output; if verbose = +1, long console output. If, e.g., simulate = FALSE and verbose = 1, then hergm reports the following console output:

```

Progress: 50.00% of 1000000
...
means of block parameters: -0.2838 1.3323
precisions of block parameters: 0.9234 1.4682
block parameters:
-0.2544 -0.2560 -0.1176 -0.0310 -0.1915 -1.9626
0.4022 1.8887 1.9719 0.6499 1.7265 0.0000
block indicators: 1 3 1 1 1 1 3 1 1 2 2 2 2 1 1 1
block sizes: 10 5 2 0 0
block probabilities: 0.5396 0.2742 0.1419 0.0423 0.0020
block probabilities prior parameter: 0.4256
posterior prediction of statistics: 66 123
where ... indicates additional information about the Markov chain Monte Carlo
algorithm that is omitted here. The console output corresponds to:
- "means of block parameters" correspond to the mean parameters of the Gaus-
sian base distribution of parameters of hergm-terms.
- "precisions of block parameters" correspond to the precision parameters of the
Gaussian base distribution of parameters of hergm-terms.
- "block parameters" correspond to the parameters of hergm-terms.
- "block indicators" correspond to the indicators of block memberships of nodes.
- "block sizes" correspond to the block sizes.
- "block probabilities" correspond to the prior probabilities of block member-
ships of nodes.
- "block probabilities prior parameter" corresponds to the concentration param-
eter of truncated Dirichlet process prior of parameters of hergm-terms.
- if predictions = TRUE, "posterior prediction of statistics" correspond to pos-
terior predictions of sufficient statistics.
...
additional arguments, to be passed to lower-level functions in the future.

```

Value

The function `hergm` returns an object of class `hergm` with components:

<code>network</code>	network is an object of class <code>network</code> and can be created by calling the function <code>network</code> .
<code>formula</code>	formula of the form <code>network ~ terms</code> . <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> . Possible terms can be found in <code>erm.terms</code> and <code>hergm.terms</code> .
<code>n</code>	number of nodes.
<code>hyper_prior</code>	indicator of whether hyper prior has been specified, i.e., whether the parameters <code>alpha</code> , <code>eta_mean</code> , and <code>eta_precision</code> are estimated.
<code>alpha</code>	concentration parameter of truncated Dirichlet process prior of parameters of <code>hergm-terms</code> .
<code>ergm_theta</code>	parameters of <code>ergm-terms</code> .

<code>eta_mean</code>	mean parameters of Gaussian base distribution of parameters of hergm-terms.
<code>eta_precision</code>	precision parameters of Gaussian base distribution of parameters of hergm-terms.
<code>d1</code>	total number of parameters of ergm terms.
<code>d2</code>	total number of parameters of hergm terms.
<code>hergm_theta</code>	parameters of hergm-terms.
<code>relabelled.hergm_theta</code>	relabelled parameters of hergm-terms by using <code>relabel = 1</code> or <code>relabel = 2</code> .
<code>number_fixed</code>	number of fixed indicators of block memberships of nodes.
<code>indicator</code>	indicators of block memberships of nodes.
<code>relabel</code>	if <code>relabel > 0</code> , relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) (<code>relabel = 1</code>) or Peng and Carvalho (2016) (<code>relabel = 2</code>).
<code>relabelled.indicator</code>	relabelled indicators of block memberships of nodes by using <code>relabel = 1</code> or <code>relabel = 2</code> .
<code>size</code>	the size of the blocks, i.e., the number of nodes of blocks.
<code>parallel</code>	number of computing nodes; if <code>parallel > 1</code> , hergm is run on parallel computing nodes.
<code>p_i_k</code>	posterior probabilities of block membership of nodes.
<code>p_k</code>	probabilities of block memberships of nodes.
<code>predictions</code>	if <code>predictions = TRUE</code> and <code>simulate = FALSE</code> , returns posterior predictions of statistics in the model.
<code>simulate</code>	if <code>simulate = TRUE</code> , simulation of networks, otherwise Bayesian inference.
<code>prediction</code>	posterior predictions of statistics.
<code>edgelist</code>	edge list of simulated network.
<code>sample_size</code>	if <code>simulate = TRUE</code> , number of network draws, otherwise number of posterior draws minus number of burn-in iterations; if <code>parallel > 1</code> , number of draws on each computing node.
<code>extract</code>	indicator of whether function <code>hergm.postprocess</code> has postprocessed the object of class <code>hergm</code> generated by function <code>hergm</code> and thus whether the MCMC sample generated by function <code>hergm</code> has been extracted from the object of class <code>hergm</code> .
<code>convergence.diagnostics</code>	MCMC diagnostics generated by function <code>mcmc.diagnostics</code> , which in turn relies on function <code>mcgibbsit</code> in R package <code>mcgibbsit</code> ; see <code>?mcgibbsit</code> .
<code>verbose</code>	if <code>verbose = -1</code> , no console output; if <code>verbose = 0</code> , short console output; if <code>verbose = +1</code> , long console output.

References

- Babkin, S. and M. Schweinberger (2019). Large-scale estimation of random graph models with local dependence. <https://arxiv.org/abs/1703.09301>.
- Cao, M., Chen, Y., Fujimoto, K., and M. Schweinberger (2018). A two-stage working model strategy for network analysis under hierarchical exponential random graph models. Proceedings

of the 2018 IEEE/ACM International Conference on Advances in Social Networks Analysis and Mining, 290–298.

Handcock, M. S. (2003). Assessing degeneracy in statistical models of social networks. Technical report, Center for Statistics and the Social Sciences, University of Washington, Seattle. <http://www.csss.washington.edu/Paper>

Holland, P. W. and S. Leinhardt (1981). An exponential family of probability distributions for directed graphs. *Journal of the American Statistical Association, Theory & Methods*, 76, 33–65.

Krivitsky, P. N., Handcock, M. S., & Morris, M. (2011). Adjusting for network size and composition effects in exponential-family random graph models. *Statistical methodology*, 8(4), 319-339.

Krivitsky, P.N, and Kolaczyk, E. D. (2015). On the question of effective sample size in network modeling: An asymptotic inquiry. *Statistical science: a review journal of the Institute of Mathematical Statistics*, 30(2), 184.

Nowicki, K. and T. A. B. Snijders (2001). Estimation and prediction for stochastic blockstructures. *Journal of the American Statistical Association, Theory & Methods*, 96, 1077–1087.

Peng, L. and L. Carvalho (2016). Bayesian degree-corrected stochastic block models for community detection. *Electronic Journal of Statistics* 10, 2746–2779.

Schweinberger, M. (2011). Instability, sensitivity, and degeneracy of discrete exponential families. *Journal of the American Statistical Association, Theory & Methods*, 106, 1361–1370.

Schweinberger, M. (2019). Consistent structure estimation of exponential-family random graph models with block structure. *Bernoulli*, to appear.

Schweinberger, M. and M. S. Handcock (2015). Local dependence in random graph models: characterization, properties, and statistical inference. *Journal of the Royal Statistical Society, Series B (Statistical Methodology)*, 7, 647-676.

Schweinberger, M., Krivitsky, P. N., Butts, C.T. and J. Stewart (2019). Exponential-family models of random graphs: Inference in finite-, super-, and infinite-population scenarios. *Statistical Science*, to appear.

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

Schweinberger, M., Petrescu-Prahova, M. and D. Q. Vu (2014). Disaster response on September 11, 2001 through the lens of statistical network analysis. *Social Networks*, 37, 42–55.

Schweinberger, M. and J. Stewart (2019). Concentration and consistency results for canonical and curved exponential-family random graphs. *The Annals of Statistics*, to appear.

Snijders, T. A. B. and K. Nowicki (1997). Estimation and prediction for stochastic blockmodels for graphs with latent block structure. *Journal of Classification*, 14, 75–100.

Stewart, J., Schweinberger, M., Bojanowski, M., and M. Morris (2019). Multilevel network data facilitate statistical inference for curved ERGMs with geometrically weighted terms. *Social Networks*, 59, 98–119.

Vu, D. Q., Hunter, D. R. and M. Schweinberger (2013). Model-based clustering of large networks. *Annals of Applied Statistics*, 7, 1010–1039.

See Also

network, ergm.terms, hergm.terms, hergm.postprocess, mcmc.diagnostics, summary, print, plot, gof, simulate

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij, max_number=3)
summary(object)

data(sampson)
object <- hergm(samplike ~ edges_ij + transitivities_ijk, max_number=3)
summary(object)

## End(Not run)
```

hergm-terms

*Model terms***Description**

Hierarchical exponential-family random graph models with local dependence can be specified by calling the function `hergm(formula)`, where `formula` is a formula of the form `network ~ terms`. By specifying suitable terms, it is possible to specify a wide range of models: see `hergm.terms`. `hergm.terms` can be found here. In addition, `ergm.terms` can be used to include covariates.

Arguments

`edges_i` (undirected network)
adding the term `edges_i` to the model adds node-dependent edge terms to the model; please note: the term `edges_i` can be used with `method = "bayes"` but cannot be used with the default `method = "ml"`.

`arcs_i` (directed network)
adding the term `arcs_i` to the model adds node-dependent outdegree terms to the model; please note: the term `arcs_i` can be used with `method = "bayes"` but cannot be used with the default `method = "ml"`.

`arcs_j` (directed network)
adding the term `arcs_j` to the model adds node-dependent indegree terms to the model; please note: the term `arcs_j` can be used with `method = "bayes"` but cannot be used with the default `method = "ml"`.

`edges_ij` (undirected, directed network)
adding the term `edges_ij` to the model adds block-dependent edge terms to the model.

`mutual_i` (directed network)
adding the term `mutual_i` to the model adds additive, block-dependent mutual edge terms to the model.

`mutual_ij` (directed network)
adding the term `mutual_ij` to the model adds block-dependent mutual edge terms to the model.

`twostar_ijk` (undirected network)
adding the term `twostar_ijk` to the model adds block-dependent two-star terms to the model;

`transitivities_ijk` (directed network)
 adding the term `transitivities_ijk` to the model adds block-dependent transitive ties terms to the model.

`triangle_ijk` (undirected, directed network)
 adding the term `triangle_ijk` to the model adds block-dependent triangle terms to the model.

`ttriple_ijk` (directed network)
 adding the term `ttriple_ijk` to the model adds block-dependent transitive triple terms to the model; please note: the term `ttriple_ijk` can be used with `method = "bayes"` but cannot be used with the default `method = "ml"`.

`ctriple_ijk` (directed network)
 adding the term `ctriple_ijk` to the model adds block-dependent cyclic triple terms to the model; please note: the term `ctriple_ijk` can be used with `method = "bayes"` but cannot be used with the default `method = "ml"`.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `ergm.terms`

Examples

```
## Not run: data(sampson)
hergm(samplike ~ edges + transitivities_ijk)

## End(Not run)
```

`hergm.mcmc.diagnostics`

MCMC diagnostics of objects of class hergm

Description

The function `mcmc.diagnostics.hergm` helps detect non-convergence of the auxiliary-variable MCMC algorithm implemented in function `hergm`. It reports Markov chain Monte Carlo convergence diagnostics by using the function `mcgibbsit` of R package `mcgibbsit` along with trace plots. The help function of the function `mcgibbsit` provides additional details about the output of the function `mcgibbsit`.

Usage

```
## S3 method for class 'hergm'
mcmc.diagnostics(object, ...)
```

Arguments

`object` object of class `hergm`; objects of class `hergm` can be generated by function `hergm`.
`...` additional arguments, to be passed to lower-level functions in the future.

Value

The function `mcmc.diagnostics` returns a list with the following components:

`mcmc.alpha` MCMC diagnostics for the concentration parameter of truncated Dirichlet process prior of parameters of `hergm`-terms.
`mcmc.eta_mean` MCMC diagnostics for the mean parameters of Gaussian base distribution of parameters of `hergm`-terms.
`mcmc.eta_precision` MCMC diagnostics for the precision parameters of Gaussian base distribution of parameters of `hergm`-terms.
`mcmc.ergm_theta` MCMC diagnostics for the parameters of `ergm`-terms.
`mcmc.hergm_theta` MCMC diagnostics for the parameters of `hergm`-terms.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk, method="bayes")
mcmc.diagnostics(object)

## End(Not run)
```

`hergm.postprocess` *Postprocess object of class hergm*

Description

The function `hergm.postprocess` postprocesses an object of class `hergm`. Please note that the function `hergm` calls the function `hergm.postprocess` with `relabel = 0` by default or with other values of `relabel` specified by the user, therefore users do not need to call the function `hergm.postprocess` unless it is desired to postprocess an object of class `hergm` with a value of `relabel` that was not used by function `hergm`.

If `hergm.postprocess` is called with `relabel > 0`, it solves the so-called label-switching problem. The label-switching problem is rooted in the invariance of the likelihood function to permutations of the labels of blocks, and implies that raw MCMC samples from the posterior cannot be used to infer to block-dependent entities. The label-switching problem can be solved in a Bayesian decision-theoretic framework: by choosing a loss function and minimizing the posterior expected loss. Two loss functions are implemented in `hergm.postprocess`, the loss function of Schweinberger and Handcock (2015) (`relabel == 1`) and the loss function of Peng and Carvalho (2016) (`relabel == 2`). The first loss function seems to be superior in terms of the reported clustering probabilities, but is more expensive in terms of computing time. A rule of thumb is to use the first loss function when `max_number < 15` and use the second loss function otherwise.

Usage

```
hergm.postprocess(object,
                  burnin = 2000,
                  thinning = 1,
                  relabel = 1,
                  number_runs = 1,
                  ...)
```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>burnin</code>	number of posterior burn-in iterations; if computing is parallel, <code>burnin</code> is applied to the sample generated by each processor; please note that <code>hergm</code> returns <code>min(sample_size, 10000)</code> sample points and the burn-in is applied to the sample of size <code>min(sample_size, 10000)</code> , therefore <code>burnin</code> should be smaller than <code>min(sample_size, 10000)</code> .
<code>thinning</code>	if <code>thinning > 1</code> , every <code>thinning</code> -th sample point is used while all others discarded; if computing is parallel, <code>thinning</code> is applied to the sample generated by each processor; please note that <code>hergm</code> returns <code>min(sample_size, 10000)</code> sample points and the thinning is applied to the sample of size <code>min(sample_size, 10000) - burnin</code> , therefore <code>thinning</code> should be smaller than <code>min(sample_size, 10000) - burnin</code> .
<code>relabel</code>	if <code>relabel > 0</code> , relabel MCMC sample by minimizing the posterior expected loss of Schweinberger and Handcock (2015) (<code>relabel == 1</code>) or Peng and Carvalho (2016) (<code>relabel == 2</code>).
<code>number_runs</code>	if <code>relabel == 1</code> , number of runs of relabeling algorithm.

... additional arguments, to be passed to lower-level functions in the future.

Value

ergm_theta	parameters of ergm-terms.
alpha	concentration parameter of truncated Dirichlet process prior of parameters of hergm-terms.
eta_mean	mean parameters of Gaussian base distribution of parameters of hergm-terms.
eta_precision	precision parameters of Gaussian base distribution of parameters of hergm-terms.
hergm_theta	parameters of hergm-terms.
loss	if relabel == TRUE, local minimum of loss function.
p_k	probabilities of block memberships of nodes.
indicator	indicators of block memberships of nodes.
p_i_k	posterior probabilities of block memberships of nodes.
prediction	posterior predictions of statistics.

References

Peng, L. and L. Carvalho (2016). Bayesian degree-corrected stochastic block models for community detection. *Electronic Journal of Statistics* 10, 2746–2779.

Schweinberger, M. and M. S. Handcock (2015). Local dependence in random graph models: characterization, properties, and statistical Inference. *Journal of the Royal Statistical Society, Series B (Statistical Methodology)*, 7, 647-676.

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm

Examples

```
## Not run: data(example)
object <- hergm(d ~ edges_ij + triangle_ijk)
hergm.postprocess(object)

## End(Not run)
```

 kapferer

Kapferer collaboration network

Description

The network corresponds to collaborations between 39 workers in a tailor shop in Africa: an undirected edge between workers i and j indicates that the workers collaborated. The network is taken from Kapferer (1972).

Usage

```
data(kapferer)
```

Value

Undirected network.

References

Kapferer, B. (1972). Strategy and Transaction in an African Factory. Manchester University Press, Manchester, U.K.

See Also

network, hergm, ergm.terms, hergm.terms

Examples

```
## Not run: data(kapferer)
object <- hergm(kapferer ~ edges_ij + transitivities_ijk, max_number=3)
summary(object)

## End(Not run)
```

 plot.hergm

Plot summary of object of class hergm

Description

The function `plot.hergm` accepts an object of class `hergm` as argument and plots a summary of a sample of block memberships of nodes from the posterior. Please note that the function `hergm` should have been called with `relabel > 0` to solve the so-called label-switching problem, which is done by default. If the function `hergm` has not been called with option `relabel > 0`, call the function `hergm.postprocess` with `relabel > 0`.

Usage

```
## S3 method for class 'hergm'  
plot(x, threshold = c(.7, .8, .9), ...)
```

Arguments

x	object of class hergm; objects of class hergm can be generated by function hergm.
threshold	if the component relabel of the object of class hergm is relabel = 3, then threshold is a vector of thresholds between 0 and 1, indicating the thresholds at which the same-block-membership posterior probabilities of nodes are to be thresholded to construct the same-block graphs.
...	additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

hergm, hergm.postprocess, print.hergm, summary.hergm

Examples

```
## Not run: data(example)  
object <- hergm(d ~ edges_ij)  
plot(object)  
  
## End(Not run)
```

print.hergm

Print summary of object of class hergm

Description

The function `print.hergm` accepts an object of class `hergm` as argument and prints a summary of parameters from the posterior. Please note that the function `hergm` should have been called with `relabel > 0` to solve the so-called label-switching problem, which is done by default. If the function `hergm` has not been called with option `relabel > 0`, call the function `hergm.postprocess` with `relabel > 0`.

Usage

```
## S3 method for class 'hergm'  
print(x, ...)
```

Arguments

`x` object of class `hergm`; objects of class `hergm` can be generated by function `hergm`.

`...` additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `hergm.postprocess`, `plot.hergm`, `summary.hergm`

Examples

```
## Not run: data(example)  
object <- hergm(d ~ edges_ij)  
print(object)  
  
## End(Not run)
```

<code>simulate.hergm</code>	<i>Simulate network</i>
-----------------------------	-------------------------

Description

The function `simulate.hergm` accepts an object of class `hergm` as argument and simulates networks.

Usage

```
## S3 method for class 'hergm'  
simulate(object,  
          nsim = 1,  
          seed = NULL,  
          max_number = NULL,  
          indicator = NULL,  
          eta = NULL,
```

```
sample_size = 1,
verbose = 0,
...)
```

Arguments

object	either object of class <code>hergm</code> or formula of the form <code>network ~ terms</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> ; <code>network</code> is an object of class <code>network</code> and can be created by calling the function <code>network</code> ; possible terms can be found in <code>ergm.terms</code> and <code>hergm.terms</code> .
nsim	redundant, but ensures that the <code>simulate</code> method is compatible with the <code>simulate</code> method of R package <code>stats</code> .
seed	redundant, but ensures that the <code>simulate</code> method is compatible with the <code>simulate</code> method of R package <code>stats</code> .
max_number	maximum number of blocks.
indicator	indicators of block memberships of nodes.
eta	<code>ergm.terms</code> and <code>hergm.terms</code> parameters.
sample_size	number of networks to be simulated.
verbose	if <code>verbose == -1</code> , no console output; if <code>verbose == 0</code> , short console output; if <code>verbose == +1</code> , long console output.
...	additional arguments, to be passed to lower-level functions in the future.

Value

The function `simulate.hergm` returns the simulated networks in the form of edge lists.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `ergm.terms`, `hergm.terms`, `gof.hergm`

Examples

```
## Not run: set.seed(123456789)

# Simulate 100 networks from model:
d <- matrix(rbinom(n=45*45, size=1, prob=.1), 45, 45)
d <- as.network(d, directed=TRUE, loops = FALSE)
N <- 100
indicator <- c(rep.int(1, 10), rep.int(2, 15), rep.int(3, 20))
eta <- c(-1.5, -2, -2.5, -4, .5, .5, .5, 0)
edgelists <- simulate.hergm(d ~ edges_ij + transitivities_ijk,
  max_number=3, indicator=indicator, eta=eta, sample_size=N)
d <- lapply(as.network, X=edgelists$edgelist)
```

```

coord <- plot(d[[1]], vertex.col=indicator, edge.col=same_clusters(indicator))
for (i in 1:N) plot(d[[i]], vertex.col=indicator, edge.col=same_clusters(indicator), coord=coord)

# Estimate model from first simulated network:
network <- d[[1]]
object <- hergm(network ~ edges_ij + transitivities_ijk, max_number=3)
# Plot network with estimated block structure:
plot(object)

## End(Not run)

```

summary.hergm

Summary of object of class hergm

Description

The function `summary.hergm` generates a summary of an object of class `hergm` by using the functions `print.hergm` and `plot.hergm`. The function `print.hergm` prints a summary of a sample of parameters from the posterior, whereas the function `plot.hergm` plots a summary of a sample of block memberships of nodes from the posterior.

Usage

```

## S3 method for class 'hergm'
summary(object, ...)

```

Arguments

<code>object</code>	object of class <code>hergm</code> ; objects of class <code>hergm</code> can be generated by function <code>hergm</code> .
<code>...</code>	additional arguments, to be passed to lower-level functions in the future.

References

Schweinberger, M. and P. Luna (2018). HERGM: Hierarchical exponential-family random graph models. *Journal of Statistical Software*, 85, 1–39.

See Also

`hergm`, `hergm.postprocess`, `print.hergm`, `plot.hergm`

Examples

```

## Not run: data(example)
object <- hergm(d ~ edges_ij)
summary(object)

## End(Not run)

```

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