

# Package ‘TestGardener’

November 24, 2022

**Version** 3.1.0

**Date** 2022-11-22

**Type** Package

**Title** Optimal Analysis of Test and Rating Scale Data

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**Depends** R (>= 3.5), fda, ggplot2, rgl

**Description** Develop, evaluate, and score multiple choice examinations, psychological scales, questionnaires, and similar types of data involving sequences of choices among one or more sets of answers.

This version of the package should be considered as brand new. Almost all of the functions have been changed, including their argument list.

See the file NEWS.Rd in the Inst folder for more information.

Using the package does not require any formal statistical knowledge beyond what would be provided by a first course in statistics in a social science department. There the user would encounter the concept of probability and how it is used to model data and make decisions, and would become familiar with basic mathematical and statistical notation. Most of the output is in graphical form.

**License** GPL (>= 2)

**LazyData** true

**Imports** dplyr, ggpubr, stringr, tidyr, pracma, utf8, knitr, rmarkdown

**VignetteBuilder** knitr

**BuildVignettes** yes

**Language** en-US

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2022-11-24 14:50:02 UTC

**R topics documented:**

|                               |    |
|-------------------------------|----|
| Analyze . . . . .             | 3  |
| ArcLength.plot . . . . .      | 5  |
| dataSimulation . . . . .      | 6  |
| density_plot . . . . .        | 8  |
| DHfun . . . . .               | 9  |
| entropies . . . . .           | 11 |
| Entropy.plot . . . . .        | 12 |
| Hcurve . . . . .              | 14 |
| Hfun . . . . .                | 16 |
| Hfuns.plot . . . . .          | 17 |
| ICC.fit . . . . .             | 18 |
| ICC.plot . . . . .            | 21 |
| keyshsort . . . . .           | 24 |
| make.dataList . . . . .       | 25 |
| mu.plot . . . . .             | 28 |
| Power.plot . . . . .          | 29 |
| Quantshort_dataList . . . . . | 31 |
| Quantshort_infoList . . . . . | 32 |
| Quantshort_key . . . . .      | 33 |
| Quantshort_parList . . . . .  | 33 |
| Quantshort_U . . . . .        | 34 |
| scoreDensity . . . . .        | 35 |
| scorePerformance . . . . .    | 36 |
| SDS . . . . .                 | 38 |
| SDS_dataList . . . . .        | 38 |
| SDS_infoList . . . . .        | 39 |
| SDS_key . . . . .             | 40 |
| SDS_parList . . . . .         | 41 |
| SDS_U . . . . .               | 42 |
| Sensitivity.plot . . . . .    | 43 |
| testscore . . . . .           | 45 |
| TG_density.fd . . . . .       | 47 |
| theta.distn . . . . .         | 49 |
| theta2arclen . . . . .        | 50 |
| thetafun . . . . .            | 53 |
| thetasearch . . . . .         | 54 |
| Ushort . . . . .              | 56 |
| Usimulate . . . . .           | 57 |
| Wbinsmth . . . . .            | 58 |
| Wpca.plot . . . . .           | 61 |

Analyze

*Analyze test or rating scale data defined in dataList.***Description**

The test or rating scale data have already been processed by function `make.dataList` or other code to produce the list object `dataList`. The user defines a list vector `ParameterList` which stores results from a set of cycles of estimating surprisal curves followed by estimating optimal score index values for each examinee or respondent. These score index values are within the interval [0,100]. The number of analysis cycles is the length of the `parList` list vector.

**Usage**

```
Analyze(theta, thetaQnt, dataList, ncycle=10, itdisp=FALSE, verbose=FALSE)
```

**Arguments**

|                       |  |
|-----------------------|--|
| <code>theta</code>    | A vector of N score index values for the examinees or respondents. These values are in the percent interval [0,100].   |
| <code>thetaQnt</code> | A vector of length $2 * nbin + 1$ where <code>nbin</code> is the number of bins containing score index values. The vector begins with the lower boundary 0 and ends with the upper boundary 100. In between it alternates between the bin center value and the boundary separating the next bin.   |
| <code>dataList</code> | <p>A list that contains the objects needed to analyse the test or rating scale with the following fields:</p> <p><b>U:</b> A matrix of response data with N rows and n columns where N is the number of examinees or respondents and n is the number of items. Entries in the matrices are the indices of the options chosen. Column i of U is expected to contain only the integers 1,...,noption.</p> <p><b>optList:</b> A list vector containing the numerical score values assigned to the options for this question.</p> <p><b>key:</b> If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length n containing the indices the right answers. Otherwise, it is NULL.</p> <p><b>WfdPar:</b> An <code>fdPar</code> object for the defining the surprisal curves.</p> <p><b>noption:</b> A numeric vector of length n containing the numbers of options for each item.</p> <p><b>nbin:</b> The number of bins for binning the data.</p> <p><b>scrrng:</b> A vector of length 2 containing the limits of observed sum scores.</p> <p><b>scrfine:</b> A fine mesh of test score values for plotting.</p> <p><b>scrvec:</b> A vector of length N containing the examinee or respondent sum scores.</p> <p><b>itemvec:</b> A vector of length n containing the question or item sum scores.</p> <p><b>percnrnk:</b> A vector length N containing the sum score percentile ranks.</p> <p><b>thetaQnt:</b> A numeric vector of length <math>2 * nbin + 1</math> containing the bin boundaries alternating with the bin centers. These are initially defined as <code>seq(0,100,len=2*nbin+1)</code>.</p> |

|                      |  |
|----------------------|--|
|                      | <b>Wdim:</b> The total dimension of the surprisal scores.                                    |
|                      | <b>PcntMarkers:</b> The marker percentages for plotting: 5, 25, 50, 75 and 95.               |
| <code>ncycle</code>  | The number of cycles executed by <code>Analyze</code> .                                      |
| <code>itdisp</code>  | If TRUE, the progress of the iterations within each cycle for estimating theta are reported. |
| <code>verbose</code> | If TRUE, the stages of analysis within each cycle for estimating theta are reported.         |

### Details

The cycling process is described in detail in the references, and displayed in R code in the vignette `SweSATQuantitativeAnalysis`.

### Value

The list vector `parList` where each member is a named list object containing the results of an analysis cycle. These results are:

- theta:** The optimal estimates of the score index values for the examinees/respondents. This is a vector of length `N`.
- thetaQnt:** A vector of length `2*nbin+1` containing bin boundaries alternating with bin edges.
- WfdList:** A list vector containing results from the estimation of surprisal curves. The list vector is of length `n`, the number of questions or items in the test of rating scale. For details concerning these results, see function `Wbinsmth()`.
- logdensfd:** A functional data object defining the estimate of the log of the probability density function for the distribution of the score index values.
- C:** The normalizing value for probability density functions. A density value is computed by dividing the exponential of the log density value by this constant.
- densfine:** The value of the probability density function over a fine mesh of 101 equally spaced score index values.
- denscdf:** The values over a fine mesh of the cumulative probability distribution function. These values start at 0 and end with 1 and are increasing. Ties are often found at the upper boundary, so that using these values for interpolation purposes may require using the vector `unique(denscdf)`.
- binctr:** A vector of length `nbin` containing the bin centers within the interval `[0,100]`.
- bdry:** A vector of length `nbin+1` containing the bin boundaries.
- freq:** A vector of length `nbin` containing the number of score index values in the bins. An score index value is within a bin if it is less than or equal to the upper boundary and greater than the lower boundary. The first boundary also contains zero values.
- Hval:** A vector of length `N` containing the values of the negative log likelihood fitting criterion.
- DHval:** A vector of length `N` containing the values of the first derivative of the negative log likelihood fitting criterion.
- D2Hval:** A vector of length `N` containing the values of the second derivative of the negative log likelihood fitting criterion.
- active:** A vector of length `N` of the activity status of the values of theta. If convergence was not achieved, the value is TRUE, otherwise FALSE.

**arclength:** The length of the space curve defined by the surprisal curves.

**alfine:** A vector of length 101 of arclengths corresponding to equally spaced values of theta.

**theta\_al:** A vector of length N of arclengths corresponding to estimated values of theta.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

### See Also

[make.dataList](#), [dataSimulation](#), [Power.plot](#), [scoreDensity](#), [Sensitivity.plot](#), [testscore](#), [theta.distn](#), [theta2arclen](#), [thetafun](#), [Wbinsmth](#), [ICC.plot](#), [Wpca.plot](#)

---

ArcLength.plot

*Plot the score index theta as a function of arc length.*

---

### Description

Arc length is the distance along the space curved traced out as score index theta increases from 0 to 100. It is measured in bits and is remains unchanged if the score index continuum is modified.

### Usage

```
ArcLength.plot(arclength, arclengthvec, titlestr=NULL)
```

### Arguments

|              |   |
|--------------|---|
| arclength    | This is a positive real number indicating the total length of the space curve. It is expressed in terms of numbers of bits. |
| arclengthvec | A vector of length 101 containing equally-spaced arc-length distances along the test information curve.                     |
| titlestr     | A string for the title of the data.   |

### Value

A gg or ggplot object defining the plot of arclength along the test information curve as a function of the score index theta. This is displayed by the print command. The plot is automatically displayed as a side value even if no return object is specified in the calling statement.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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**See Also**

[theta2arclen](#)

**Examples**

```
# Example 1. Display the arc length curve for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
indfine      <- seq(0,100,len=101)
WfdList      <- Quantshort_parList$WfdList
theta        <- Quantshort_parList$theta
Qvec         <- Quantshort_parList$Qvec
binctr       <- Quantshort_parList$binctr
arclenList   <- theta2arclen(theta, Qvec, WfdList, binctr)
names(arclenList)
arclength    <- arclenList$arclength
arclengthvec <- arclenList$arclengthvec
oldpar <- par(no.readonly=TRUE)
on.exit(oldpar)
ArcLength.plot(arclength, arclengthvec)
# Example 2. Display the arc length curve for the
# Symptom Distress Scale with 13 items and 473 respondents
indfine      <- seq(0,100,len=101)
WfdList      <- SDS_parList$WfdList
theta        <- SDS_parList$theta
Qvec         <- SDS_parList$Qvec
binctr       <- SDS_parList$binctr
arclenList   <- theta2arclen(theta, Qvec, WfdList, binctr)
arclength    <- arclenList$arclength
arclengthvec <- arclenList$arclengthvec
ArcLength.plot(arclength, arclengthvec)
```

**Description**

Estimate sum score, score index values theta and test information values bias and mean squared errors using simulated data.

**Usage**

```
dataSimulation(dataList, parList, theta.pop = seq(0, 100, len = 101),  
              nsample = 1000)
```

**Arguments**

|           |  |
|-----------|--|
| dataList  | The list object set up by function make_dataList.                              |
| parList   | The list object containing objects computed by function Analyze.               |
| theta.pop | A vector containing true values of theta to be estimated using simulated data. |
| nsample   | The number of simulated samples.   |

**Value**

A named list object containing objects produced from analyzing the simulations, one set for each simulation:

**sumscr:** Sum score estimates  
**theta:** Score index estimates  
**mu:** Expected sum score estimates  
**al:** Total arc length estimates  
**thepop:** True or population score index values  
**mupop:** Expected sum score population values  
**alpop:** Total test length population values  
**n:** Number of items  
**ntheta:** Number of theta values  
**indfine:** Fine mesh over score index range  
**Qvec:** Five marker percentages: 5, 25, 50, 75 and 95

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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**See Also**

[scorePerformance](#)

---

density\_plot

*Plot the probability density function for a set of test scores*

---

**Description**

Plots the probability density function of a set of score values that are not at the score boundaries as a smooth curve, and also plots the proportions of score values at both boundaries as points. The score values are typically either the values of the score index values theta or the arclength or information score values.

**Usage**

```
density_plot(scrvec, scrrng, Qvec, xlabstr=NULL, titlestr=NULL,
             scrnbasis=15, nfine=101)
```

**Arguments**

|           |  |
|-----------|--|
| scrvec    | A vector of N score values   |
| scrrng    | A vector of length 2 containing boundary values  |
| Qvec      | A vector of length 5 containing the score values corresponding to the marker percentages 5, 25, 50, 75 and 95. |
| xlabstr   | Label for abscissa   |
| titlestr  | Label for plot   |
| scrnbasis | The number of spline basis functions used for representing the smooth density function                         |
| nfine     | Number of plotting points  |

**Value**

A plot object.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[scoreDensity](#)

**Examples**

```
# Example 1. Display probability density curve for the
# score index values for the short SweSAT multiple choice test with
# 24 items and 1000 examinees
theta <- Quantshort_parList$theta
Qvec <- Quantshort_parList$Qvec
# plot the density for the score indices within interval c(0,100)
oldpar <- par(no.readonly=TRUE)
on.exit(oldpar)
density_plot(theta, c(0,100), Qvec, xlabstr="Score index",
             titlestr="SweSAT 13B Theta Density",
             scrnbasis=11, nfine=101)

# Example 2. Display probability density curve for the
# arc length or information values
theta_al <- Quantshort_infoList$theta_al
Qvec_al <- Quantshort_infoList$Qvec_al
arclength <- Quantshort_infoList$arclength
# plot the density for the score indices within interval c(0,arclength)
density_plot(theta_al, c(0,arclength), Qvec_al, xlabstr="Score index",
             titlestr="SweSAT 13B Theta Density",
             scrnbasis=11, nfine=101)
```

---

DHfun

*Compute the first and second derivatives of the negative log likelihoods*

---

**Description**

DHfun computes the first and second derivatives of the negative log likelihoods for a set of examinees. Items can be either binary or multi-option. The analysis is within the closed interval  $[0,100]$ .

**Usage**

```
DHfun(theta, WfdList, Umat)
```

**Arguments**

**theta** Initial values for score indices in  $[0,n]/[0,100]$ . Vector of size  $N$ .

**WfdList** A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of `WfdList` is a named list containing information computed during the analysis. These named lists contain these objects:

**Wfd**: A functional data object containing the  $M$  surprisal curves for a question.

**M**: The number of options.

**Pbin:** A matrix containing proportions at each bin.  
**Wbin:** A matrix containing surprisal values at each bin.  
**Pmatfine:** A matrix of probabilities over a fine mesh.  
**Wmatfine:** A matrix of surprisal values over a fine mesh.  
**DWmatfine:** A matrix of the values of the first derivative of surprisal curves over fine mesh.  
**D2Wmatfine:** A matrix of the values of the second derivative of surprisal curves over fine mesh.

Umat            An N by n matrix of responses. If N = 1, it can be a vector of length n.

### Value

A named list for results DH and D2H:

**DH:** First derivatives of the negative log likelihood values, vector of size N

**D2H:** Second derivatives of the negative log likelihood values, vector of size N

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

### See Also

[make.dataList](#), [Hfun](#), [Hfuns.plot](#)

### Examples

```
# Example 1:
# Compute the first and second derivative values of the objective function for
# locating each examinee for the 24-item short form of the SweSAT quantitative
# test on the percentile score index continuum.
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
U <- Quantshort_dataList$U
DHfunResult <- DHfun(theta, WfdList, U)
DHval <- DHfunResult$DH
D2Hval <- DHfunResult$D2H
print(paste("Mean of objective gradient =",round(mean(DHval),4)))
print(paste("Standard deviation of objective gradient =",round(sqrt(var(DHval)),4)))
print(paste("Mean of objective Hessian =",round(mean(D2Hval),4)))
print(paste("Standard deviation of objective Hessian =",round(sqrt(var(D2Hval)),6)))
```

```
# Example 2:
# Compute the first and second derivative values of the objective function for
# locating each examinee for the 13-item Symptom Distress scale
# on the percentile score index continuum.
# Proceed as above changing "Quant" for "SDS".
```

---

entropies

*Entropy measures of inter-item dependency*


---

### Description

Entropy  $I_1$  is a scalar measure of how much information is required to predict the outcome of a choice number 1 exactly, and consequently is a measure of item effectiveness suitable for multiple choice tests and rating scales. Joint entropy  $J_{1,2}$  is a scalar measure of the cross-product of multinomial vectors 1 and 2. Mutual entropy  $I_{1,2} = I_1 + I_2 - J_{1,2}$  is a measure of the co-dependency of items 1 and 2, and thus the analogue of the negative log of a squared correlation  $R^2$ . this function computes all four types of entropies for two specified items.

### Usage

```
entropies(theta, m, n, U, noption)
```

### Arguments

|         |  |
|---------|--|
| theta   | A vector of length N containing score index values for each test taker.        |
| m       | The index of the first choice.   |
| n       | The index of the second choice.  |
| U       | The data matrix containing the indices of choisen options for each test taker. |
| noption | A vector containing the number of options for all items.                       |

### Value

A named list object containing objects produced from analyzing the simulations, one set for each simulation:

**I\_m:** The entropy of item m.

**I\_n:** The entropy of item n.

**J\_nm:** The joint entropy of items m and n.

**I\_nm:** The mutual entropy of items m and n.

### Author(s)

Juan Li and James Ramsay

## References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

## See Also

[Entropy.plot](#)

## Examples

```
# Load needed objects
U      <- Quantshort_dataList$U
theta  <- Quantshort_parList$theta
noption <- matrix(5,24,1)
# compute mutual entropies for all pairs of the first 6 items
Mvec   <- 1:6
Mlen   <- length(Mvec)
Hmutual <- matrix(0,Mlen,Mlen)
for (i1 in 1:Mlen) {
  for (i2 in 1:i1) {
    Result <- entropies(theta, Mvec[i1], Mvec[i2], U, noption)
    Hmutual[i1,i2] = Result$Hmutual
    Hmutual[i2,i1] = Result$Hmutual
  }
}
print("Matrix of mutual entries (off-digagonal) and self-entropies (diagonal)")
print(round(Hmutual,3))
```

---

Entropy.plot

*Plot item entropy curves for selected items or questions.*

---

## Description

Item the value of the entropy curve at a point theta is the expected value of the surprisal curve values. Entropy is a measure of the randomness of the surprisal value, which is maximized when all the surprisal curves have the same value and has a minimum of zero if all but a single curve has probability zero. This is unattainable in the calculation, but can be arbitrarily close to this state.

## Usage

```
Entropy.plot(scrfine, WfdList, Qvec, dataList, plotindex=1:n,
             plorange=c(min(scrfine),max(scrfine)), height=1.0, value=0,
             ttlsz=NULL, axisttl=NULL, axistxt=NULL)
```

**Arguments**

|           |   |
|-----------|---|
| scrfine   | A vector of length <code>nfine</code> (usually 101) containing equally spaced points spanning the <code>plotrange</code> . Used for plotting.   |
| WfdList   | A numbered list object produced by a <code>TestGardener</code> analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <code>WfdList</code> is a named list containing information computed during the analysis. These named lists contain these objects:<br><br><b>Wfd:</b> A functional data object containing the <code>M</code> surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| Qvec      | The five marker percentile values.  |
| dataList  | A list vector containing objects essential to an analysis.  |
| plotindex | A set of integers specifying the numbers of the items or questions to be displayed.   |
| plotrange | A vector of length 2 containing the plot boundaries within or over the score index interval <code>c(0,100)</code> .   |
| height    | A positive real number defining the upper limit on the ordinate for the plots.  |
| value     | Number required by <code>ggplot2</code> . Defaults to 0.  |
| ttlsz     | Title font size.  |
| axisttl   | Axis title font size.   |
| axistxt   | Axis text(tick label) font size.  |

**Details**

An entropy curve for each question indexed in the `index` argument. A request for a keystroke is made for each question. The answer to question strongly defines the optimal position of an estimated score index value where the curve is high value. Values of entropy curves typically range over `[0,1]`.

**Value**

The plots of the entropy curves specified in `plotindex` are produced as a side effect. If `saveplot` is `TRUE`, the plots of item entropy curves specified in `plotindex` are bundled into a single postscript or `.pdf` file and the file name is defined by `paste(dataList$titlestr, i, '-entropy.pdf', sep="")`. The file is then output as a returned value.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[Sensitivity.plot](#), [Power.plot](#), [Hfuncs.plot](#), [ICC.plot](#)

**Examples**

```
# Example 1. Display the item entropy curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# plot the entropy curve for the first item
WfdList <- Quantshort_parList$WfdList
Qvec <- Quantshort_parList$Qvec
scrfine <- seq(0,100,len=101)
oldpar <- par(no.readonly=TRUE)
Entropy.plot(scrfine, WfdList, Qvec, Quantshort_dataList, plotindex=1)
par(oldpar)
# Example 2. Display the item entropy curves for the
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".
```

---

Hcurve

*Construct grid of 101 values of the fitting function*

---

**Description**

A fast grid of values of the fitting function or one of its first two derivatives is constructed for use in function `thetasearch`.

**Usage**

```
Hcurve(WfdList, U, nderiv=0)
```

**Arguments**

|         |  |
|---------|--|
| WfdList | A list vector containing specifications of surprisal curves for each item. |
| U       | A N by n matrix containing indices of chosen items for each test taker.    |
| nderiv  | Integer 0, 1 or 2 to indicate which level of derivative to use.            |

**Value**

A vector of length 101 containing grid values of a derivative of the fitting function

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[thetasearch](#)

**Examples**

```
# Compute a grid of values of the objective function for locating each
# examinee or respondent for the 24-item short form of the SweSAT quantitative
# test on the percentile score index continuum [0,100].
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
U <- Quantshort_dataList$U
n <- ncol(U)
# Fitting function for the first examinee
j <- 1
Umat <- matrix(U[j,],1,n)
Hcurve1 <- Hcurve(WfdList, Umat, 0)
# First derivative of the fitting function for the first examinee
DHcurve1 <- Hcurve(WfdList, Umat, 1)
# Second derivative of the fitting function for the first examinee
D2Hcurve1 <- Hcurve(WfdList, Umat, 2)
oldpar <- par(no.readonly=TRUE)
par(mfrow=c(3,1))
indfine <- seq(0,100,len=101)
plot(indfine, Hcurve1, type="l", xlab="", ylab="Fitting curve",
     main="Examinee 1")
plot(indfine, DHcurve1, type="l", xlab="", ylab="First derivative")
points(theta[1], 0, pch="o")
abline(0,0,lty=2)
plot(indfine, D2Hcurve1, type="l", xlab="Score index", ylab="Second derivative")
abline(0,0,lty=2)
points(theta[1], 0, pch="o")
par(oldpar)
```

---

|      |   |
|------|---|
| Hfun | <i>Compute the negative log likelihoods associated with a vector of score index values.</i> |
|------|---|

---

### Description

Hfun computes the negative log likelihoods for a set of examinees, each at a single value theta.

### Usage

```
Hfun(theta, WfdList, Umat)
```

### Arguments

|         |  |
|---------|--|
| theta   | A vector of size N containing values for score indices in the interval [0,100].  |
| WfdList | A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of WfdList is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd:</b> A functional data object containing the M surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| Umat    | An N by n matrix of responses or, for a single examinee, a vector of length n.   |

### Value

A vector of length N of negative log likelihood values.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[make.dataList](#), [Hfun](#), [Hfuns.plot](#)

**Examples**

```
# Example 1: Compute the values of the objective function for locating each
# examinee or respondent for the 24-item short form of the SweSAT quantitative
# test on the percentile score index continuum [0,100].
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
U <- Quantshort_dataList$U
Hval <- Hfun(theta, WfdList, U)
print(paste("Mean          of objective function =",round(mean(Hval),2)))
print(paste("Standard deviation of objective function =",round(sqrt(var(Hval)),2)))
# Example 2: Compute the values of the objective function for locating each
# examinee or respondent for the 13-item Symptom Distress Scale
# on the percentile score index continuum [0,100].
# Proceed as above changing "Quant" for "SDS".
```

---

|            |   |
|------------|---|
| Hfuns.plot | <i>Plot a selection of fit criterion H functions and their first two derivatives.</i> |
|------------|---|

---

**Description**

These plots indicate whether an appropriate minimum of the fitting criterion was found. The value of theta should be at the function minimum, the first derivative be close to zero there, and the second derivative should be positive. If these conditions are not met, it may be worthwhile to use function `thetafun` initialized with an approximate minimum value of score index theta to re-estimate the value of theta.

**Usage**

```
Hfuns.plot(theta, WfdList, U, plotindex=1)
```

**Arguments**

|           |  |
|-----------|--|
| theta     | The entire vector of estimated values of theta.                        |
| WfdList   | The list vector of length n containing the estimated surprisal curves. |
| U         | The entire N by n matrix of choice indices.                            |
| plotindex | A subset of the integers 1:N.  |

**Details**

The curves are displayed in three vertically organized panels along with values of theta and the values and first two derivative values of the fit criterion. If more than one index value is used, a press of the Enter or Return key moves to the next index value.

**Value**

A list vector is returned which is of the length of argument `plotindex`. Each member of the vector is a `gg` or `ggplot` object for the associated `plotindex` value. Each plot can be displayed using the `print` command. The plots of item power are produced as a side value even if no output object is specified in the call to the function.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[thetafun](#), [Hfun](#), [DHfun](#)

**Examples**

```
# Example 1. Display fit criterion values and derivatives for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
index <- 1
theta <- Quantshort_parList$theta
WfdList <- Quantshort_parList$WfdList
U <- Quantshort_dataList$U
Hval <- Hfun(theta[index], WfdList, U[index,])
DHResult <- DHfun(theta[index], WfdList, U[index,])
DHval <- DHResult$DH
D2Hval <- DHResult$D2H
Hfuns.plot(theta, WfdList, U, plotindex=index)
# Example 2. Compute score index values theta for the
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".
```

---

ICC.fit

*Estimate the option probability and surprisal curves.*

---

**Description**

The surprisal curves for each item are fit to the surprisal transforms of choice probabilities for each of a set of bins of current performance values `theta`. The error sums of squares are minimized by the surprisal optimization `smooth.surp` in the `fda` package. The output is a list vector of length `n` containing the functional data objects defining the curves.

**Usage**

```
ICC.fit(theta, dataList, WfdList=dataList$WfdList,
        thetaQnt=seq(0,100, len=2*nbin+1), wtvec=matrix(1,n,1),
        iterlim=20, conv=1e-4, dbglev=0)
```

**Arguments**

|          |  |
|----------|--|
| theta    | A vector of length N containing current values of score index percentile values.   |
| dataList | A list that contains the objects needed to analyse the test or rating scale with the following fields:<br><b>U:</b> A matrix of response data with N rows and n columns where N is the number of examinees or respondents and n is the number of items. Entries in the matrices are the indices of the options chosen. Column i of U is expected to contain only the integers 1, . . . , noption.<br><b>optList:</b> A list vector containing the numerical score values assigned to the options for this question.<br><b>key:</b> If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length n containing the indices the right answers. Otherwise, it is NULL.<br><b>WfdPar:</b> An fdPar object for the defining the surprisal curves.<br><b>noption:</b> A numeric vector of length n containing the numbers of options for each item.<br><b>nbin:</b> The number of bins for binning the data.<br><b>srrng:</b> A vector of length 2 containing the limits of observed sum scores.<br><b>scrfine:</b> A fine mesh of test score values for plotting.<br><b>scrvec:</b> A vector of length N containing the examinee or respondent sum scores.<br><b>itemvec:</b> A vector of length n containing the question or item sum scores.<br><b>percntrnk:</b> A vector length N containing the sum score percentile ranks.<br><b>thetaQnt:</b> A numeric vector of length 2*nbin + 1 containing the bin boundaries alternating with the bin centers. These are initially defined as seq(0, 100, len=2*nbin+1).<br><b>Wdim:</b> The total dimension of the surprisal scores.<br><b>PentMarkers:</b> The marker percentages for plotting: 5, 25, 50, 75 and 95. |
| WfdList  | A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of WfdList is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd:</b> A functional data object containing the M surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>indfine:</b> A vector of length 101 containing equally spaced plotting points.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.  |

|                       |   |
|-----------------------|---|
|                       | <b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.  |
|                       | <b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh.  |
|                       | By default <code>ICC.fit</code> uses the <code>WfdList</code> member of <code>dataList</code> , which is generated by the initialization with <code>ICC.fit.init</code> within <code>make.dataList</code> . Usually this is what is required. However, <code>WfdList</code> may occasionally need to be entered from another source, and so included here as a separate argument. |
| <code>thetaQnt</code> | A vector of length $2*n+1$ containing the sequence of bin boundary and bin centre values.   |
| <code>wtvec</code>    | A vector of length <code>n</code> of weights on observations. Defaults to all ones.   |
| <code>iterlim</code>  | The maximum number of iterations used in optimizing surprisal curves. Defaults to 20.   |
| <code>conv</code>     | Convergence tolerance. Defaults to 0.0001.  |
| <code>dbglev</code>   | Level of output within <code>ICC.fit</code> . If 0, no output, if 1 the error sum of squares and slope on each iterations, and if 2 or higher, results for each line search iteration with function <code>lnsrch</code> .   |

## Details

The function first bins the data in order to achieve rapid estimation of the option surprisal curves. The argument `thetaQnt` contains the sequence of bin boundaries separated by the bin centers, so that it is of length  $2*nbin + 1$  where `nbin` is the number of bins. These bin values are distributed over the percentile interval  $[0,100]$  so that the lowest boundary is 0 and highest 100. Prior to the call to `ICC.fit` these boundaries are computed so that the numbers of values of `theta` falling in the bins are roughly equal. It is important that the number of bins be chosen so that the bins contain at least about 25 values.

After the values of `theta` are binned, the proportions that the bins are chosen for each question and each option are computed. Proportions of zero are given NA values.

The positive proportions are then converted to surprisal values where  $surprisal = -\log_M(\text{proportion})$  where  $\log_M$  is the logarithm with base `M`, the number of options associated with a question. Bins with zero proportions are assigned a surprisal that is appropriately large in the sense of being in the range of the larger surprisal values associated with small but positive proportions.

The next step is to fit the surprisal values for each question by a functional data object that is smooth, passes as closely as possible to an option's surprisal values, and has values consistent with being a surprisal value. The function `smooth.surp()` is used for this purpose.

Finally the curves and other results for each question are saved in object `WfdList`, a list vector of length `n`, and the list vector is returned.

## Value

The optimized numbered list object produced by `ICC.fit`. See above for its description.

## Author(s)

Juan Li and James Ramsay

## References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

## See Also

[ICC.plot](#), [thetafun](#)

## Examples

```
# Example 1. Display the item probability and surprisal curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# estimate the initial surprisal curves
theta    <- Quantshort_dataList$percncrnk
thetaQnt <- Quantshort_parList$thetaQnt
Qvec     <- Quantshort_parList$Qvec
Result   <- ICC.fit(theta, Quantshort_dataList)
WfdList  <- Result$WfdList
# plot the curves for the first question
binctr   <- Quantshort_parList$binctr
scrfine  <- seq(0,100,len=101)
ICC.plot(scrfine, WfdList, Quantshort_dataList, Qvec, binctr,
         plotindex=1, plotrange=c(0,100))
# estimate the final surprisal curves
theta    <- Quantshort_parList$theta
thetaQnt <- Quantshort_parList$thetaQnt
Qvec     <- Quantshort_parList$Qvec
WfdList  <- Quantshort_parList$WfdList
# plot the curves for the first question
ICC.plot(scrfine, WfdList, Quantshort_dataList, Qvec, binctr,
         plotindex=1, plotrange=c(0,100))
# Example 2. Display the item probability and surprisal curves for the
# Symptom Distress Scale with 13 items and 473 respondents.
# Proceed as above changing "Quant" to "SDS"
```

---

ICC.plot

*Plot probability and surprisal curves for a selection of test or scale items.*

---

## Description

ICC.plots plots each item in argument `plotindex` in turn after function `Wbinsmth()` has used spline smoothing to estimate item and option characteristic curves.

**Usage**

```
ICC.plot(scrfine, WfdList, dataList, Qvec, binctr, plotType = "P",
        plotindex=1:n, plotrange=c(min(scrfine),max(scrfine)),
        shaderrange = NULL, Wrng=c(0,5), DWrng=c(-0.2, 0.2),
        data_point = FALSE, ci = FALSE,
        titlestr = NULL, autoplot = FALSE, ttlsz = NULL,
        axisttl = NULL, axistxt = NULL, lgdlab = NULL)
```

**Arguments**

- |          |   |
|----------|---|
| scrfine  | A vector of 101 plotting points.  |
| WfdList  | <p>A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of WfdList is a named list containing information computed during the analysis. These named lists contain these objects:</p> <p><b>scrfine:</b> A vector of length 101 containing plotting points.</p> <p><b>Wfd:</b> A functional data object containing the M surprisal curves for a question.</p> <p><b>M:</b> The number of options.</p> <p><b>Pbin:</b> A matrix containing proportions at each bin.</p> <p><b>Wbin:</b> A matrix containing surprisal values at each bin.</p> <p><b>indfine:</b> A vector of length 101 with equally spaced score values used for plotting.</p> <p><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.</p> <p><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.</p> <p><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.</p> <p><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh.</p> <p><b>PStdErr:</b> A matrix of the values of the standard error of probability curves at each bin.</p> <p><b>WStdErr:</b> A matrix of the values of the standard error of surprisal curves at each bin.</p> |
| dataList | <p>A list that contains the objects needed to analyse the test or rating scale with the following fields:</p> <p><b>U:</b> A matrix of response data with N rows and n columns where N is the number of examinees or respondents and n is the number of items. Entries in the matrices are the indices of the options chosen. Column i of U is expected to contain only the integers 1, . . . , noption.</p> <p><b>optList:</b> A list vector containing the numerical score values assigned to the options for this question.</p> <p><b>key:</b> If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length n containing the indices the right answers. Otherwise, it is NULL.</p> <p><b>WfdPar:</b> An fdPar object for the defining the surprisal curves.</p>   |

|            |  |
|------------|--|
|            | <b>noption:</b> A numeric vector of length $n$ containing the numbers of options for each item.  |
|            | <b>nbin:</b> The number of bins for binning the data.  |
|            | <b>scrrng:</b> A vector of length 2 containing the limits of observed sum scores.  |
|            | <b>scrfine:</b> A fine mesh of test score values for plotting.   |
|            | <b>scrvec:</b> A vector of length $N$ containing the examinee or respondent sum scores.  |
|            | <b>itemvec:</b> A vector of length $n$ containing the question or item sum scores.   |
|            | <b>percentrnk:</b> A vector length $N$ containing the sum score percentile ranks.  |
|            | <b>thetaQnt:</b> A numeric vector of length $2*nbin + 1$ containing the bin boundaries alternating with the bin centers. These are initially defined as <code>seq(0, 100, len=2*nbin+1)</code> .   |
|            | <b>Wdim:</b> The total dimension of the surprisal scores.  |
|            | <b>PcntMarkers:</b> The marker percentages for plotting: 5, 25, 50, 75 and 95.   |
| Qvec       | A vector of five marker percentile values. For plotting over information, this is replaced by <code>Qvec_al</code> returned as <code>parList\$Qvec_al</code> .   |
| binctr     | A vector of bin center values. If the plot is over arc length or information, <code>binctr</code> is modified before calling <code>Wbinsth.plot</code> by the command <code>binctr_al = pracma::interp1(indfine, alfine, binctr)</code> , and argument <code>binctr</code> is replaced by <code>binctr_al</code> . |
| plotType   | Type(s) of plot, default as "P" for probability, can also be "W" for surprisal, "DW" for sensitivity, and any combination of the three   |
| plotindex  | A vector of indices of items to be plotted.  |
| plotrange  | A vector of length 2 containing the plot boundaries of the score index interval.   |
| shaderange | a list of length 2 vector(s); set if users want to gray out specific score range(s)  |
| Wrng       | A vector of length 2 specifying the plotting range for surprisal values.   |
| DWrng      | A vector of length 2 specifying the plotting range for sensitivity values.   |
| titlestr   | plot title   |
| autoplot   | in Vignette, plot all items in a batch   |
| data_point | A logical value indicating whether to plot the data points.  |
| ci         | A logical value indicating whether to plot the confidence limits.  |
| ttlsz      | Title font size.   |
| axisttl    | Axis title font size.  |
| axistxt    | Axis text(tick label) font size.   |
| lgdlab     | Legend label font size.  |

### Value

A list vector is returned which is of the length of argument `plotindex`. Each member of the vector is a `gg` or `ggplot` object for the associated `plotindex` value. Each plot can be displayed using the `print` command. The plots of item power are produced as a side value even if no output object is specified in the call to the function.

### Author(s)

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[Sensitivity.plot](#), [Power.plot](#), [Entropy.plot](#), [Wbinsmth](#),

**Examples**

```
# Example 1. Display the item surprisal curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
WfdList <- Quantshort_parList$WfdList
Qvec <- Quantshort_parList$Qvec
binctr <- Quantshort_parList$binctr
titlestr <- NULL
# plot the curves for the first question
scrfine <- seq(0,100,len=101)
oldpar <- par(no.readonly=TRUE)
ICC.plot(scrfine, WfdList, Quantshort_dataList, Qvec, binctr, plotindex=1:2)
par(oldpar)
# Example 2. Display the item probability and surprisal curves for the
# Symptom Distress Scale with 13 items and 473 respondents.
# Proceed as above changing "Quant" to "SDS"
```

---

keyshort

*Option information for the short form of the SweSAT Quantitative test.*

---

**Description**

The file has two rows, each with 24 integers in string format. The first row contains the indices of the right answers among the options for the 24 questions. The second row contains the number of options for each question.

**Usage**

keyshort

**Details**

The code above inputs the contents of the file using the scan function into a single character vector of length 48. The strings are converted to integers by the second command, and the integer vector is then reformatted into a 2 by 24 matrix. The subsequent analysis of these data is described in detail in the vignette `SweSATQuantitativeShort`.

---

|               |  |
|---------------|--|
| make.dataList | <i>Make a list object containing information required for analysis of choice data.</i> |
|---------------|--|

---

### Description

The returned named list object contains 11 named members, which are described in the value section below.

### Usage

```
make.dataList(U, key, optList, grbg=rep(0,n), scrrng=NULL, titlestr=NULL,
             nbin=nbinDefault(N), NumBasis=NULL, WfdPar=NULL,
             jitterwr=TRUE, PcntMarkers=c( 5, 25, 50, 75, 95),
             quadwr=FALSE, verbose=FALSE)
```

### Arguments

|             |   |
|-------------|---|
| U           | A matrix with rows corresponding to examinees or respondents, and columns to questions or items.  |
| key         | If the data are a multiple choice test with only weights 0 and 1, a vector of length n containing the indices of the right answers. Otherwise, NULL.  |
| optList     | A list vector of length number of questions. A member contains a vector of score values assigned to each answer or option by the test designer.   |
| grbg        | A vector of length indicating which option for each item contains missing or illegal choice values. If 0, there is no such option.  |
| scrrng      | A vector of length two containing the initial and final values for the interval over which test scores are to be plotted. Default is minimum and maximum sum score.   |
| titlestr    | A string to be used as a title in plots and other displays.   |
| nbin        | The number of bins for containing proportions of examinees choosing options. The default is computed by a function that uses the number of examinees.   |
| NumBasis    | The number of spline basis functions used to represent surprisal curves. The default is computed by a function that uses the number of examinees.   |
| WfdPar      | A functional parameter object specifying a basis, a linear differential operator, a smoothing parameter, a boolean constant indicating estimation, and a penalty matrix. The default object defines an order 5 spline with operator $Lfd = 3$ and smoothing parameter $1e4$ . The number of basis functions depends on the size of N. |
| jitterwr    | A boolean constant: TRUE implies adding a small random value to each sum score value prior to computing percent rank values.  |
| PcntMarkers | Used in plots of curves to display marker or reference percentage points for abscissa values in plots.  |

|         |   |
|---------|---|
| quadwrd | If TRUE a default order 5 basis is constructed. If FALSE the order and number of of basis functions are 3 so as to support the use of the second derivative in function thetafun. |
| verbose | If TRUE details of calculations are displayed.  |

### Details

The score range defined `scrrng` should contain all of the sum score values, but can go beyond them if desired. For example, it may be that no examinee gets a zero sum score, but for reporting and display purposes using zero as the lower limit seems desirable.

The number of bins is chosen so that a minimum of at least about 25 initial percentage ranks fall within a bin. For larger samples, the number per bin is also larger, making the proportions of choice more accurate. The number bins can be set by the user, or by a simple algorithm used to adjust the number of bins to the number `N` or examinees.

The number of spline basis functions used to represent a surprisal curve should be small for small sample sizes, but can be larger when larger samples are involved. A minimum of 7 and maximum of 24 basis functions is assigned by default. The number of basis function can be set by the user or otherwise by a simple algorithm used to adjust the number of bins to the number `N` of examinees.

Adding a small value to discrete values before computing ranks is considered a useful way of avoiding any biases that might arise from the way the data are stored. The small values used leave the rounded jittered values fixed, but break up ties for sum scores.

It can be helpful to see in a plot where special marker percentages 5, 25, 50, 75 and 95 percent of the interval  $[0,100]$  are located. The median abscissa value is at 50 per cent for initial percent rank values, for example, but may not be located at the center of the interval after iterations of the analysis cycle.

### Value

A named list with named members as follows:

**U:** A matrix of response data with `N` rows and `n` columns where `N` is the number of examinees or respondents and `n` is the number of items. Entries in the matrices are the indices of the options chosen. Column `i` of `U` is expected to contain only the integers  $1, \dots, \text{noption}$ .

**optList:** A list vector containing the numerical score values assigned to the options for this question.

**key:** If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length `n` containing the indices the right answers. Otherwise, it is `NULL`.

**WfdPar:** An `fdPar` object for the defining the surprisal curves.

**noption:** A numeric vector of length `n` containing the numbers of options for each item.

**nbin:** The number of bins for binning the data.

**scrng:** A vector of length 2 containing the limits of observed sum scores.

**scrfine:** A fine mesh of test score values for plotting.

**scrvec:** A vector of length `N` containing the examinee or respondent sum scores.

**itemvec:** A vector of length `n` containing the question or item sum scores.

**percentrnk:** A vector length N containing the sum score percentile ranks.

**thetaQnt:** A numeric vector of length  $2 \cdot \text{nbin} + 1$  containing the bin boundaries alternating with the bin centers. These are initially defined as `seq(0, 100, len=2*nbin+1)`.

**Wdim:** The total dimension of the surprisal scores.

**PcntMarkers:** The marker percentages for plotting: 5, 25, 50, 75 and 95.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

### See Also

[Analyze](#)

### Examples

```
# Example 1: Input choice data and key for the short version of the
# SweSAT quantitative multiple choice test with 24 items and 1000 examinees
# input the choice data as 1000 strings of length 24
N <- dim(Quantshort_U)[1]
n <- dim(Quantshort_U)[2]

optList <- list()
grbg = matrix(0,n,1)
for (item in 1:n){
  noptioni <- length(unique(Quantshort_U[,item]))
  scorei <- rep(0,noptioni)
  scorei[Quantshort_key[item]] <- 1
  optList[[item]] <- scorei
  grbg[item] <- length(scorei)
}
optList <- list(itemLab=NULL, optLab=NULL, optScr=optList)

# Set up the dataList object containing the objects necessary
# for further display and analyses

Quantshort_dataList <- make.dataList(Quantshort_U, Quantshort_key, optList, grbg)

# Example 2: Input choice data and key for the Symptom Distress Scale
# with 13 items and 473 examinees.
# input the choice data as 473 strings of length 13
N <- dim(SDS_U)[1]
```

```

n <- dim(SDS_U)[2]
# ----- Define the option score values for each item -----
optList <- list()
grbg <- matrix(0,n,1)
for (item in 1:n){
  scorei <- c(0:4,0)
  optList[[item]] <- scorei
  grbg[item] <- length(scorei)
}
optList <- list(itemLab=NULL, optLab=NULL, optScr=optList)
# largest observed sum score is 37
srrng <- c(0,37)
SDS_dataList <- make.dataList(SDS_U, SDS_key, optList, grbg, srrng)

```

---

mu.plot

*Plot expected test score as a function of score index*


---

### Description

The expected score  $\mu(\theta)$  is a function of the score index  $\theta$ . A diagonal dashed line is displayed to show the linear relationship to the score range interval.

### Usage

```
mu.plot(mufine, srrng, titlestr)
```

### Arguments

|          |  |
|----------|--|
| mufine   | A mesh of 101 equally spaced values of $\mu$ as a function of $\theta$ . |
| srrng    | A vector of length 2 containing the score range.                         |
| titlestr | A string containing the title of the data.                               |

### Value

A gg or ggplot object defining the plot of the expected test score  $\mu$  as a function of the score index  $\theta$ . This is displayed by the `print` command. The plot is automatically displayed as a side value even if no return object is specified in the calling statement.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[scoreDensity](#), [testscore](#)

---

 Power.plot

---

*Plot item power curves for selected items or questions.*


---

**Description**

Item surprisal power curves are the square root of the sum over options of the squared surprisal sensitivity curves.

**Usage**

```
Power.plot(scrfine, WfdList, Qvec, dataList, plotindex=1:n,
           plotrange=c(min(scrfine),max(scrfine)), height=0.5,
           value=0, ttsiz=NULL, axisttl=NULL, axistxt=NULL)
```

**Arguments**

|           |  |
|-----------|--|
| scrfine   | A vector of length <i>n</i> fine (usually 101) containing equally spaced points spanning the plotrange. Used for plotting.   |
| WfdList   | A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <i>WfdList</i> is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd</b> : A functional data object containing the <i>M</i> surprisal curves for a question.<br><b>M</b> : The number of options.<br><b>Pbin</b> : A matrix containing proportions at each bin.<br><b>Wbin</b> : A matrix containing surprisal values at each bin.<br><b>Pmatfine</b> : A matrix of probabilities over a fine mesh.<br><b>Wmatfine</b> : A matrix of surprisal values over a fine mesh.<br><b>DWmatfine</b> : A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine</b> : A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| Qvec      | The five marker percentile values.   |
| dataList  | A list vector containing objects essential to an analysis.   |
| plotindex | A set of integers specifying the numbers of the items or questions to be displayed.  |
| plotrange | A vector of length 2 containing the plot boundaries within or over the score index interval <i>c</i> (0,100).  |
| height    | A positive real number defining the upper limit on the ordinate for the plots.   |
| value     | Number required by ggplot2. Defaults to 0.   |

|         |                                  |
|---------|----------------------------------|
| ttlsz   | Title font size.                 |
| axisttl | Axis title font size.            |
| axistxt | Axis text(tick label) font size. |

### Details

A surprisal power curve for each question indexed in the `index` argument. A request for a keystroke is made for each question. The answer to question strongly defines the optimal position of an estimated score index value where the curve is high value. Values of power curves typically range over [0,0.5].

### Value

The plots of the power curves specified in `plotindex` are produced as a side effect. If `saveplot` is TRUE, the plots of item power curves specified in `plotindex` are bundled into a single postscript or .pdf file and the file name is defined by `paste(dataList$titlestr, i, '-power.pdf', sep="")`. The file is then output as a returned value.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

### See Also

[Sensitivity.plot](#), [Entropy.plot](#), [Hfuncs.plot](#), [ICC.plot](#)

### Examples

```
# Example 1. Display the item power curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# plot the power curve for the first item
WfdList <- Quantshort_parList$WfdList
Qvec <- Quantshort_parList$Qvec
scrfine <- seq(0,100,len=101)
oldpar <- par(no.readonly=TRUE)
Power.plot(scrfine, WfdList, Qvec, Quantshort_dataList, plotindex=1)
par(oldpar)
# Example 2. Display the item power curves for the
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".
```

---

Quantshort\_dataList     *List of objects essential for an analysis of the abbreviated SweSAT Quantitative multiple choice test.*

---

### Description

The data are for 1000 randomly selected examinees taking 24 math analysis multiple choice questions.

### Usage

Quantshort\_dataList

### Format

A named list.

### Details

A named list with 15 members:

**U:** A matrix of response data with  $N$  rows and  $n$  columns where  $N$  is the number of examinees or respondents and  $n$  is the number of items. Entries in the matrices are the indices of the options chosen. Column  $i$  of  $U$  is expected to contain only the integers  $1, \dots, \text{noption}$ .

**optList:** A list vector containing the numerical score values assigned to the options for this question.

**key:** If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length  $n$  containing the indices the right answers. Otherwise, it is NULL.

**grbg:** A vector of length indicating which option for each item contains missing or illegal choice values. If 0, there is no such option.

**WfdPar:** An fdPar object for the defining the surprisal curves.

**noption:** A numeric vector of length  $n$  containing the numbers of options for each item.

**nbin:** The number of bins for binning the data.

**scrng:** A vector of length 2 containing the limits of observed sum scores.

**scrfine:** A fine mesh of test score values for plotting.

**scrvec:** A vector of length  $N$  containing the examinee or respondent sum scores.

**itemvec:** A vector of length  $n$  containing the question or item sum scores.

**percnrnk:** A vector length  $N$  containing the sum score percentile ranks.

**thetaQnt:** A numeric vector of length  $2*nbin + 1$  containing the bin boundaries alternating with the bin centers. These are initially defined as `seq(0, 100, len=2*nbin+1)`.

**Wdim:** The total dimension of the surprisal scores.

**PcntMarkers:** The marker percentages for plotting: 5, 25, 50, 75 and 95.

**titlestr:** A string containing a title for the analysis.

---

Quantshort\_infoList     *Arc length or information arameter list for 24 items from the quantitative SweSAT subtest.*

---

### Description

The data are for 1000 examinees randomly selected from those who took the 2013 quantitative subtest of the SweSAT university entrance exam. The questions are only the 24 math analysis questions, and each question has four options. The analysis results are after 10 cycles of alternating between estimating surprisal curves and estimating percentile score index values. The objects in list object Quantshort\_infoList are required for plotting results over the arc length or information domain rather the score index domain. This domain is preferred because such plots are invariant with respect to changes in the score index domain. It also has a metric structure so that differences are comparable no matter where they fall within the information domain.

### Usage

Quantshort\_infoList

### Format

A named list containing eight objects.

### Value

The object Quantshort\_parList is a named list with these members:

**arclength:** The total length of the information domain measured in M-bits, where M is the number of options for a question.

**Wfd.theta:** The log derivative functional data object defining a strictly increasing set of arc length values corresponding to set of score index values.

**arclengthvec:** A mesh of equally-spaced values of indefinite integrals of sum of norms of surprisal derivatives.

**theta\_al** The N arc length values corresponding to the N estimated score index values assigned to N examinees.

**Qvec\_al:** The arc length positions corresponding to the marker percentages 5, 25, 50, 75 and 95.

**Wfd.info:** The log derivative functional data object defining a strictly increasing set of score index values corresponding to a set of arc length values.

**thetavec:** A vector of score index values resulting from using function monfd with equally spaced arc length values and Wfd.info.

**Wdim:** The dimension of the over space containing the surprisal pcurves.

---

Quantshort\_key      *Option information for the short form of the SweSAT Quantitative test.*

---

### Description

A vector that contains the indices of the right answers among the options for the 24 questions

### Usage

Quantshort\_key

---

Quantshort\_parList      *Parameter list for 24 items from the quantitative SweSAT subtest.*

---

### Description

The data are for 1000 examinees randomly selected from those who took the 2013 quantitative subtest of the SweSAT university entrance exam. The questions are only the 24 math analysis questions, and each question has four options. The analysis results are after 10 cycles of alternating between estimating surprisal curves and estimating percentile score index values.

### Usage

Quantshort\_parList

### Format

A named list.

### Value

The object `Quantshort_parList` is a named list with these members:

**theta:** A vector of length  $N$  of estimated values of the percentile rank score index.

**thetaQnt:** A vector of length  $2*nbin + 1$  containing bin boundaries alternating with bin centres.

**WfdList:** A list vector of length equal to the number of questions. Each member contains the following eight results for the surprisal curves associated with a question:

**Wfd:** A functional data object representing the  $M$  surprisal curves defined over the percentile rank range, where  $M$  is the number of options for that question.

**M:** The number of option choices for the question.

**type:** The type of question: 1 for multiple choice, 0 for rating scale.

**Pbin:** A  $nbin$  by  $M$  matrix of proportions of examinees choosing each option for each bin,.

**Wbin:** A  $nbin$  by  $M$  matrix of surprisal values of examinees choosing each option for each bin.

- Pmatfine:** A  $n_{\text{fine}}$  by  $M$  matrix of proportions over a fine mesh of proportions of examinees choosing each option.
- Wmatfine:** A  $n_{\text{fine}}$  by  $M$  matrix of surprisal values over a fine mesh of values of examinees choosing each option.
- DWmatfine:** A  $n_{\text{fine}}$  by  $M$  matrix of the first derivative of surprisal values over a fine mesh of values of examinees choosing each option. These are referred to as the sensitivity values.
- logdensfd:** A functional data object representing the logarithm of the density of the percentile rank score index values.
- C:** The norming constant: the density function is  $\exp(\logdensfd)/C$ .
- densfine:** A fine mesh of probability density values of the percentile rank score index.
- denscdf:** A fine mesh of cumulative probability distribution values used for interpolating values.
- Qvec:** The score index values associated with the five marker percentages 5, 25, 50, 75 and 95.
- binctr:** A vector of length  $n_{\text{bin}}$  containing the centres of the bins.
- bdry:** A vector of length  $n_{\text{bin}}+1$  containing the boundaries of the bins.
- freq:** An  $n_{\text{bin}}$  by  $M$  matrix of frequencies with which options are chosen.
- Wmax:** A maximum surprisal value used for plotting purposes.
- Hval:** The value of the fitting criterion  $H$  for a single examinee or respondent.
- DHval:** The value of the first derivative of the fitting criterion  $H$  for a single examinee or respondent.
- D2Hval:** The value of the second derivative of the fitting criterion  $H$  for a single examinee or respondent.
- active:** A logical vector of length  $N$  indicating which estimates of  $\theta$  are converged (FALSE) or not converged (TRUE).
- arclength:** The length in bits of the test information curve.
- alfine:** A mesh of 101 equally spaced positions along the test information curve.
- Qvec\_al:** The positions of the five marker percentages on the test information curve.
- theta\_al:** A vector of length  $N$  containing the positions of each examinee or respondent on the test information curve.

---

Quantshort\_U

*Test data for 24 math calculation questions from the SweSAT Quantitative data.*

---

### Description

These data are for a randomly selected subset of 1000 examinees.

### Usage

Quantshort\_U

### Format

A matrix object with 1000 rows and 24 columns. The integers indicate which answer was chosen for each question by the examinee associated with the row.

---

scoreDensity                      *Compute and plot a score density histogram and and curve.*

---

### Description

The tasks of function `theta.density()` and plotting the density are combined. The score density is plotted both as a histogram and as a smooth curve. All the score types may be plotted: sum scores, expected test scores, percentile score index values, and locations on the test information or scale curve. The plot is output as a `ggplot2` plot object, which is actually plotted using the `print` command.

### Usage

```
scoreDensity(scrvec, srrng=c(0,100), ndensbasis=15, ttlstr=NULL, pltmax=0)
```

### Arguments

|                         |  |
|-------------------------|--|
| <code>scrvec</code>     | A vector of strictly increasing bin boundary values, with the first at the lowest plotting value and the last at the upper boundary. The number of bins in the histogram is one less than the number of <code>bndry</code> values. |
| <code>srrng</code>      | A vector of length 2 containing lower and upper boundaries on scores, which defaults to <code>c(0,100)</code> .  |
| <code>ndensbasis</code> | The number of spline basis functions to be used to represent the smooth density curve.   |
| <code>ttlstr</code>     | A string object used as a title for the plot. Defaults to none.  |
| <code>pltmax</code>     | An upper limit on the vertical axis for plotting. Defaults to the maximum curve value.   |

### Value

A `ggplot2` plot object `dens.plot` that can be displayed using command `print(dens.plot)`.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

### See Also

[thetafun](#), [theta2arclen](#), [testscore](#), [theta.distn](#)

## Examples

```
# Example 1. Display probability density curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
Qvec <- Quantshort_parList$Qvec
# plot the density for the score indices within interval c(0,100)
theta_int <- theta[0 < theta & theta < 100]
oldpar <- par(no.readonly=TRUE)
scoreDensity(theta_int)
par(oldpar)
```

---

|                  |   |
|------------------|---|
| scorePerformance | <i>Calculate mean squared error and bias for a set of score index values from simulated data.</i> |
|------------------|---|

---

## Description

After the simulated data matrices have been analyzed, prepare the objects necessary for the performance plots produced by functions `RMSEbias1.plot` and `RMSEbias2.plot`.

## Usage

```
scorePerformance(dataList, simList)
```

## Arguments

**dataList** A list that contains the objects needed to analyse the test or rating scale with the following fields:

- U**: A matrix of response data with  $N$  rows and  $n$  columns where  $N$  is the number of examinees or respondents and  $n$  is the number of items. Entries in the matrices are the indices of the options chosen. Column  $i$  of  $U$  is expected to contain only the integers  $1, \dots, \text{noption}$ .
- optList**: A list vector containing the numerical score values assigned to the options for this question.
- key**: If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length  $n$  containing the indices the right answers. Otherwise, it is `NULL`.
- WfdPar**: An `fdPar` object for the defining the surprisal curves.
- noption**: A numeric vector of length  $n$  containing the numbers of options for each item.
- nbin**: The number of bins for binning the data.
- srrng**: A vector of length 2 containing the limits of observed sum scores.
- scrfine**: A fine mesh of test score values for plotting.
- scrvec**: A vector of length  $N$  containing the examinee or respondent sum scores.
- itemvec**: A vector of length  $n$  containing the question or item sum scores.

**percntrnk:** A vector length N containing the sum score percentile ranks.

**thetaQnt:** A numeric vector of length  $2 \cdot \text{nbin} + 1$  containing the bin boundaries alternating with the bin centers. These are initially defined as `seq(0, 100, len=2*nbin+1)`.

**Wdim:** The total dimension of the surprisal scores.

**PentMarkers:** The marker percentages for plotting: 5, 25, 50, 75 and 95.

simList A named list containing these objects:

**sumscr:** A matrix with row dimension `ntheta`, the number of population score index values and column dimension `nsample`, the number of simulated samples.

**theta:** An `ntheta` by `nsample` of estimated score index values.

**mu:** An `ntheta` by `nsample` of estimated expected score values.

**al:** An `ntheta` by `nsample` of estimated test information curve values.

**thepop:** A vector of population score index values.

**mupop:** A vector of expected scores computed from the population score index values.

**alpop:** A vector of test information values computed from the population score index values.

**n:** The number of questions.

**Qvec:** The five marker percentile values.

## Value

A named list containing these objects:

**sumscr:** A matrix with row dimension `ntheta`, the number of population score index values and column dimension `nsample`, the number of simulated samples.

**theta:** An `ntheta` by `nsample` matrix of estimated score index values.

**mu:** An `ntheta` by `nsample` matrix of estimated expected score values.

**al:** An `ntheta` by `nsample` matrix of estimated test information curve values.

**thepop:** A vector of population score index values.

**mupop:** A vector of expected scores computed from the population score index values.

**alpop:** A vector of test information values computed from the population score index values.

**n:** The number of questions.

**Qvec:** The five marker percentile values.

## References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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## See Also

[dataSimulation](#)

---

|     |   |
|-----|---|
| SDS | <i>The Symptom Distress Scale data.</i> |
|-----|---|

---

**Description**

The SDS is a rating scale with 13 questions and scores 0, 1, 2, 3 and 4.

**Usage**

```
data("SDS")
```

**Format**

A text file with 473 rows, each containing a string of 13 characters.

---

|              |   |
|--------------|---|
| SDS_dataList | <i>List of objects essential for an analysis of the Symptom Distress Scale.</i> |
|--------------|---|

---

**Description**

The data are for 473 respondents to the Symptom Distress Scale. Each question has rating scores 0, 1, 2, 3, and 4.

**Usage**

```
data("SDS_dataList")
```

**Format**

A named list.

**Details**

A named list with 15 members. See below for a description of each member.

**U:** An N by n matrix of integers indicating which option was chosen by one of N examinees for a question. The object should be in the matrix class and the contents should be integers. For any question the integers should be within the range 1 to the number of options.

**optList:** A list vector object of length equal to the number of questions. Each member of the list is a numeric vector of score values assigned to each option by the test designer. For multiple choice questions, these scores are usually 0 for wrong answers and 1 for the right answer. For rating scales they are often a sequence of signed integers indicating intensity of some experience.

**grbg:** A vector of length indicating which option for each item contains missing or illegal choice values. If 0, there is no such option.

- WfdPar:** A functional parameter object that is required to represent the surprisal curves. The number of basis functions should be small for smaller sizes and larger for large samples. For example, 7 for  $N \leq 500$ , 11 for  $N$  in  $[500, 2000]$ , 24 for  $N \geq 2000$ .
- logdensfd:** A functional data object used to represent the log density of the percentile score index values. The number of basis functions is often the same as used for the WfdPar object.
- noption:** An integer vector of length equal to the number of questions indicating the number of options for each question.
- nbin:** The number of bins used to contain the score index values. The number should ensure that each bin can hold at least 25 score values. For medium sized samples, 50 per bin is fine, and for large samples as many as are required to define the detail in the surprisal curves.
- key:** An integer vector of length equal to the number of questions and containing the right answer indices. This is not used for rating scales and can be NULL in that case.
- scrrng:** A vector of length 2 defining a range over which the sum and expected scores will be estimated.
- scrvec:** A vector of length  $N$  containing the sum scores for the examinees or respondents.
- percitrnk:** The percentile ranks for each of the examinees or respondents. This is the percentage of examinees with sum scores below that for an examinee. Ties are often broken by adding a small random quantity to each sum score before computing ranks.
- scrfine:** A fine mesh of score values used for plotting purposes, and running from `scrrng[1]` to `scrrng[2]`. Common number for mesh values are 51 or 101.
- scrtype:** If the question is of multiple choice, the value is 1, and if not, 0.
- indrng:** Defines the range of the score index. Usually this is `c(0,100)`.
- indfine:** A fine mesh of score index values used for plotting, and usually ranging from 0 to 100. The number of mesh values is commonly 51 or 101.

---

SDS\_infoList

*Arc length or information parameter list for 13 items in the Symptom Distress Scale.*


---

## Description

The data are for 473 respondents to the Symptom Distress Scale. Each question has options with rating scores 0, 1, 2, 3, and 4. The analysis results are 10 cycles of alternating between estimating surprisal curves and estimating percentile score index values.

The objects in list object `Quantshort_infoList` are required for plotting results over the arc length or information domain rather the score index domain. This domain is preferred because such plots are invariant with respect to changes in the score index domain. It also has a metric structure so that differences are comparable no matter where they fall within the information domain.

## Usage

```
SDS_infoList
```

**Format**

A named list containing eight objects.

**Value**

The object Quantshort\_parList is a named list with these members:

**arlength:** The total length of the information domain measured in M-bits, where M is the number of options for a question.

**Wfd.theta:** The log derivative functional data object defining a strictly increasing set of arc length values corresponding to set of score index values.

**arlengthvec:** A mesh of equally-spaced values of indefinite integrals of sum of norms of surprisal derivatives.

**theta\_al** The N arc length values corresponding to the N estimated score index values assigned to N examinees.

**Qvec\_al:** The arc length positions corresponding to the marker percentages 5, 25, 50, 75 and 95.

**Wfd.info:** The log derivative functional data object defining a strictly increasing set of score index values corresponding to a set of arc length values.

**thetavec:** A vector of score index values resulting from using function monfd with equally spaced arc length values and Wfd.info.

**Wdim:** The dimension of the over space containing the surprisal curves.

---

SDS\_key

*Key for Symptom Distress Scale.*

---

**Description**

NULL for scale data.

**Usage**

SDS\_key

SDS\_parList

*Parameter list for the Symptom Distress Scale.***Description**

The data are for 473 respondents to the Symptom Distress Scale. Each question has options with rating scores 0, 1, 2, 3, and 4. The analysis results are 10 cycles of alternating between estimating surprisal curves and estimating percentile score index values.

**Usage**

SDS\_parList

**Format**

A named list.

**Value**

The object SDS\_dataList is a list is a named list with these members:

**theta:** A vector of length N of estimated values of the percentile rank score index.

**thetaQnt:** A vector of length  $2 \cdot \text{nbin} + 1$  containing bin boundaries alternating with bin centres.

**WfdList:** A list vector of length equal to the number of questions. Each member contains the following eight results for the surprisal curves associated with a question:

- Wfd: A functional data object representing the M surprisal curves defined over the percentile rank range, where M is the number of options for that question.
- M: The number of option choices for the question.
- type: The type of question: 1 for multiple choice, 0 for rating scale.
- Pbin: A nbin by M matrix of proportions of examinees choosing each option for each bin.
- Wbin: A nbin by M matrix of surprisal values of examinees choosing each option for each bin.
- Pmatfine: A nfine by M matrix of proportions over a fine mesh of proportions of examinees choosing each option.
- Wmatfine: A nfine by M matrix of surprisal values over a fine mesh of values of examinees choosing each option.
- DWmatfine: A nfine by M matrix of the first derivative of surprisal values over a fine mesh of values of examinees choosing each option. These are referred to as the sensitivity values.

**logdensfd:** A functional data object representing the logarithm of the density of the percentile rank score index values.

**C:** The norming constant: the density function is  $\exp(\text{logdensfd})/C$ .

**densfine:** A fine mesh of probability density values of the percentile rank score index.

**denscdf:** A fine mesh of cumulative probability distribution values used for interpolating values.

- Qvec:** The score index values associated with the five marker percentages 5, 25, 50, 75 and 95.
- binctr:** A vector of length nbin containing the centres of the bins.
- bdry:** A vector of length nbin+1 containing the boundaries of the bins.
- freq:** An nbin by M matrix of frequencies with which options are chosen.
- Wmax:** A maximum surprisal value used for plotting purposes.
- Hval:** The value of the fitting criterion H for a single examinee or respondent.
- DHval:** The value of the first derivative of the fitting criterion H for a single examinee or respondent.
- D2Hval:** The value of the second derivative of the fitting criterion H for a single examinee or respondent.
- active:** A logical vector of length N indicating which estimates of theta are converged (FALSE) or not converged (TRUE).
- arclength:** The length in bits of the test information curve.
- alfine:** A mesh of 101 equally spaced positions along the test information curve.
- Qvec\_al:** The positions of the five marker percentages on the test information curve.
- theta\_al:** A vector of length N containing the positions of each examinee or respondent on the test information curve.

---

SDS\_U

*Test data for Symptom Distress Scale.*


---

### Description

The integers indicate which answer was chosen for each question by the examinee associated with the row.

### Usage

SDS\_U

### Format

A vector object with 473 rows and 13 columns.

---

Sensitivity.plot      *Plots all the sensitivity curves for selected items or questions.*

---

### Description

A sensitivity curve for an option is the first derivative of the corresponding surprisal curve. Its values can be positive or negative, and the size of the departure from zero at any point on the curve is the amount information contributed by that curve to locating the value of an examinee or respondent on the score index continuum.

### Usage

```
Sensitivity.plot(scrfine, WfdList, Qvec, dataList, plotindex=1:n,
                plorange=c(min(scrfine),max(scrfine)),
                key=NULL, titlestr=NULL, saveplot=FALSE, width=c(-0.2,0.2),
                ttsiz=NULL, axisttl=NULL, axistxt=NULL, lgdlab=NULL)
```

### Arguments

|          |  |
|----------|--|
| scrfine  | A vector of length <i>n</i> fine (usually 101) containing equally spaced points spanning the <i>plorange</i> . Used for plotting.  |
| WfdList  | A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <i>WfdList</i> is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd</b> : A functional data object containing the <i>M</i> surprisal curves for a question.<br><b>M</b> : The number of options.<br><b>Pbin</b> : A matrix containing proportions at each bin.<br><b>Wbin</b> : A matrix containing surprisal values at each bin.<br><b>Pmatfine</b> : A matrix of probabilities over a fine mesh.<br><b>Wmatfine</b> : A matrix of surprisal values over a fine mesh.<br><b>DWmatfine</b> : A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine</b> : A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| Qvec     | The values of the five marker percentiles.   |
| dataList | A list that contains the objects needed to analyse the test or rating scale with the following fields:<br><b>U</b> : A matrix of response data with <i>N</i> rows and <i>n</i> columns where <i>N</i> is the number of examinees or respondents and <i>n</i> is the number of items. Entries in the matrices are the indices of the options chosen. Column <i>i</i> of <i>U</i> is expected to contain only the integers 1,..., <i>n</i> option.<br><b>optList</b> : A list vector containing the numerical score values assigned to the options for this question.  |

|           |  |
|-----------|--|
|           | <b>key:</b> If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length $n$ containing the indices the right answers. Otherwise, it is NULL. |
|           | <b>WfdPar:</b> An fdPar object for the defining the surprisal curves.  |
|           | <b>noption:</b> A numeric vector of length $n$ containing the numbers of options for each item.  |
|           | <b>nbin:</b> The number of bins for binning the data.  |
|           | <b>scrrng:</b> A vector of length 2 containing the limits of observed sum scores.  |
|           | <b>scrfine:</b> A fine mesh of test score values for plotting.   |
|           | <b>servec:</b> A vector of length $N$ containing the examinee or respondent sum scores.  |
|           | <b>itemvec:</b> A vector of length $n$ containing the question or item sum scores.   |
|           | <b>percntrnk:</b> A vector length $N$ containing the sum score percentile ranks.   |
|           | <b>thetaQnt:</b> A numeric vector of length $2*nbin + 1$ containing the bin boundaries alternating with the bin centers. These are initially defined as <code>seq(0,100,len=2*nbin+1)</code> .   |
|           | <b>Wdim:</b> The total dimension of the surprisal scores.  |
|           | <b>PentMarkers:</b> The marker percentages for plotting: 5, 25, 50, 75 and 95.   |
| plotindex | A set of integers specifying the numbers of the items or questions to be displayed.  |
| plorange  | A vector of length 2 containing the plot boundaries within or over the score index interval $c(0,100)$ .   |
| key       | A integer vector of indices of right answers. If the data are rating scales, this can be NULL.   |
| titlestr  | A title string for plots.  |
| saveplot  | A logical value indicating whether the plot should be saved to a pdf file.   |
| width     | A vector of length 2 defining the lower and upper limits on the ordinate for the plots.  |
| ttlsz     | Title font size.   |
| axisttl   | Axis title font size.  |
| axistxt   | Axis text(tick label) font size.   |
| lgdlab    | Legend label font size.  |

### Details

Sensitivity curves for each question indexed in the `index` argument. A request for a keystroke is made for each question.

### Value

A list vector is returned which is of the length of argument `plotindex`. Each member of the vector is a `gg` or `ggplot` object for the associated `plotindex` value. Each plot can be displayed using the `print` command. The plots of item power are produced as a side value even if no output object is specified in the call to the function.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[Power.plot](#), [Entropy.plot](#), [ICC.plot](#)

**Examples**

```
# Example 1. Display the option sensitivity curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
WfdList <- Quantshort_parList$WfdList
Qvec <- Quantshort_parList$Qvec
scrfine <- seq(0,100,len=101)
oldpar <- par(no.readonly=TRUE)
Sensitivity.plot(scrfine, WfdList, Qvec, Quantshort_dataList,
                plotindex=1)
par(oldpar)
# Example 2. Display the option sensitivity curves for the
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".
```

---

testscore

*Compute the expected test score by substituting probability of choices for indicator variable 0-1 values. Binary items assumed coded as two choice items.*

---

**Description**

Compute the expected test score by substituting probability of choices for indicator variable 0-1 values. Binary items assumed coded as two choice items.

**Usage**

```
testscore(theta, WfdList, optList)
```

**Arguments**

|         |   |
|---------|---|
| theta   | Initial values for score indices in the interval [0,100]. A vector of size N.   |
| WfdList | A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of WfdList is a named list containing information computed during the analysis. These named list in each member contains these objects:<br><b>Wfd:</b> A functional data object containing the M surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| optList | A numbered list of length n. Each member contains the weights assigned to each option for that item or question.  |

**Value**

A vector of test score values.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[scoreDensity](#)

**Examples**

```
# Example 1. Compute expected sum score values for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
mu <- testscore(theta, WfdList, Quantshort_dataList$optList)
par(c(1,1))
```

```

hist(mu,11)
# Example 2. Compute expected sum score values for the
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".

```

---

TG\_density.fd

---

*Compute a Probability Density Function*


---

## Description

Like the regular S-PLUS function density, this function computes a probability density function for a sample of values of a random variable. However, in this case the density function is defined by a functional parameter object logdensfdPar along with a normalizing constant C.

The density function  $p(\text{thetadens})$  has the form  $p(\text{thetadens}) = C \exp[W(\text{thetadens})]$  where function  $W(\text{thetadens})$  is defined by the functional data object logdensfdPar.

## Usage

```

## S3 method for class 'fd'
TG_density(thetadens, logdensfdPar, conv=0.0001, iterlim=20,
           active=1:nbasis, dbglev=0)

```

## Arguments

|              |   |
|--------------|---|
| thetadens    | a set observations, which may be one of two forms: <ol style="list-style-type: none"> <li>1. a vector of observations <math>\text{\\$thetadens}_i</math></li> <li>2. a two-column matrix, with the observations <math>\text{\\$thetadens}_i</math> in the first column, and frequencies <math>\text{\\$f}_i</math> in the second.</li> </ol> <p>The first option corresponds to all <math>\text{\\$f}_i = 1</math>.</p> |
| logdensfdPar | a functional parameter object specifying the initial value, basis object, roughness penalty and smoothing parameter defining function $W(t)$ .  |
| conv         | a positive constant defining the convergence criterion.   |
| iterlim      | the maximum number of iterations allowed.   |
| active       | a logical vector of length equal to the number of coefficients defining Wfdobj. If an entry is TRUE, the corresponding coefficient is estimated, and if FALSE, it is held at the value defining the argument Wfdobj. Normally the first coefficient is set to 0 and not estimated, since it is assumed that $W(0) = 0$ .  |
| dbglev       | either 0, 1, or 2. This controls the amount information printed out on each iteration, with 0 implying no output, 1 intermediate output level, and 2 full output. If levels 1 and 2 are used, it is helpful to turn off the output buffering option in S-PLUS.  |

## Details

The goal of the function is provide a smooth density function estimate that approaches some target density by an amount that is controlled by the linear differential operator `Lfdobj` and the penalty parameter. For example, if the second derivative of  $W(t)$  is penalized heavily, this will force the function to approach a straight line, which in turn will force the density function itself to be nearly normal or Gaussian. Similarly, to each textbook density function there corresponds a  $W(t)$ , and to each of these in turn their corresponds a linear differential operator that will, when apply to  $W(t)$ , produce zero as a result. To plot the density function or to evaluate it, evaluate `Wfdobj`, exponentiate the resulting vector, and then divide by the normalizing constant `C`.

## Value

a named list of length 4 containing:

|                       |  |
|-----------------------|--|
| <code>Wfdobj</code>   | a functional data object defining function $W(\text{thetadens})$ that that optimizes the fit to the data of the monotone function that it defines.   |
| <code>C</code>        | the normalizing constant.  |
| <code>Flist</code>    | a named list containing three results for the final converged solution: (1) <b>f</b> : the optimal function value being minimized, (2) <b>grad</b> : the gradient vector at the optimal solution, and (3) <b>norm</b> : the norm of the gradient vector at the optimal solution. |
| <code>iternum</code>  | the number of iterations.  |
| <code>iterhist</code> | a <code>iternum+1</code> by 5 matrix containing the iteration history.   |

## See Also

[intensity.fd](#)

## Examples

```
# set up range for density
rangeval <- c(-3,3)
# set up some standard normal data
thetadens <- rnorm(50)
# make sure values within the range
thetadens[thetadens < -3] <- -2.99
thetadens[thetadens > 3] <- 2.99
# set up basis for W(thetadens)
basisobj <- create.bspline.basis(rangeval, 11)
# set up initial value for Wfdobj
Wfd0 <- fd(matrix(0,11,1), basisobj)
logdensfdPar <- fdPar(Wfd0)
# estimate density
denslist <- TG_density.fd(thetadens, logdensfdPar)
# plot density
thetadensval <- seq(-3,3,.2)
wval <- eval.fd(thetadensval, denslist$Wfdobj)
pval <- exp(wval)/denslist$C
oldpar <- par(no.readonly=TRUE)
```

```
on.exit(oldpar)
plot(thetadensval, pval, type="l", ylim=c(0,0.4))
points(thetadens,rep(0,50))
```

---

|             |                              |
|-------------|------------------------------|
| theta.distn | <i>Compute score density</i> |
|-------------|------------------------------|

---

### Description

Computes the cumulated density for distribution function, the probability density function, and the log probability density function as fd objects by spline smoothing of the score values thetadens using the basis object logdensbasis. The norming constant C is also output.

The score values may score index values theta, expected test score values mu, or arc length locations on the test information or scale curve. The argument functional data object logdensfd should have a range that is appropriate for the score values being represented: For score indices, [0,100], for expected test scores, the range of observed or expected scores; and for test information curve locations in the interval [0,arclength].

### Usage

```
theta.distn(thetadens, logdensbasis, pvec=c(0.05, 0.25, 0.50, 0.75, 0.95),
           nfine = 101)
```

### Arguments

|              |  |
|--------------|--|
| thetadens    | A vector of score index, test score, or arc length values. In the score index case, these are usually only the values in the interior of the interval [0,100].             |
| logdensbasis | A functional basis object for representing the log density function. The argument may also be a functional parameter object (fdPar) or a functional basis object (Wbasis). |
| pvec         | A vector length NL containing the marker percentages.  |
| nfine        | The number of values in a fine grid, default as 101.   |

### Value

A named list containing:

**cdf\_fd:** An fd object for the cumulative probability function.

**pdf\_fd:** An fd object for the probability density function. values over the fine mesh.

logdensfd: A functional data object (fd) representing the log of the probability function for input theta.

C: The normalization constant for computing the probability density function with the command `densityfd = exp(logdensfd)/C`.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[thetafun](#), [theta2arclen](#), [testscore](#), [scoreDensity](#)

**Examples**

```
# Example 1. Display the item power curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# Assemble information for estimating theta density
indfine <- seq(0,100,len=101)
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
N <- length(theta)
# Define the density for only interior theta values
inside <- theta > 0 & theta < 100
logdensbasis <- Quantshort_parList$logdensfd$basis
theta.distnList <- theta.distn(theta[inside], logdensbasis)
theta.densfine <- eval.fd(indfine, theta.distnList$pdf_fd)
# Add number of values at each boundary
thetazero <- length(theta[theta == 0])
thetacent <- length(theta[theta == 100])
# Plot both the interior density and the boundary proportions
oldpar <- par(no.readonly=TRUE)
on.exit(oldpar)
plot(indfine, theta.densfine, type="l", lwd=2, ylim=c(0,0.025),
      xlab="Percentile Index", ylab="Density")
lines(c( 0,100), c(1/100,1/100), lty=2)
lines(c( 0, 0), c(0,thetazero/N), lty=1, lwd=4)
lines(c(100,100), c(0,thetacent/N), lty=1, lwd=4)
```

**Description**

The one-dimensional psychometric model defines a space curve within the vector space defined by the total collection of option surprisal curves. This curve is a valuable resource since positions along the curve are defined in bits and positions on the curve are subject to the same strict properties that apply to physical measurements.

Function `theta2arclen` is required to convert objects defined over the score index continuum  $c(0, 100)$  to the same objects over the arc length continuum  $c(0, \text{arclength})$ , and also vice versa. Since the arc length or information continuum is along a space curve that is invariant under strictly monotone transformations of the score index `theta`, and is also a metric, it is an ideal choice for the abscissa in all plots.

**Usage**

```
theta2arclen(theta, Qvec, WfdList, binctr, itemindex=1:n, plotrng=c(0,100), shortwrtd)
```

**Arguments**

|                        |  |
|------------------------|--|
| <code>theta</code>     | A vector of score index, test score, or arc length values, one for each examinee or respondent.  |
| <code>Qvec</code>      | A vector of locations of the five marker percentages.  |
| <code>WfdList</code>   | A numbered list object produced by a <code>TestGardener</code> analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <code>WfdList</code> is a named list containing information computed during the analysis. These named lists contain these objects:<br><br><b>Wfd:</b> A functional data object containing the $M$ surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| <code>binctr</code>    | A vector of locations of the bin centers.  |
| <code>itemindex</code> | A vector containing the indices of the items to be used.   |
| <code>plotrng</code>   | A vector of length 2 containing the starting score index and end score index values of the range to be plotted.  |
| <code>shortwrtd</code> | If <code>TRUE</code> only vectors <code>arclength</code> and <code>arclengtvec</code> are returned in order to speed up the computation within cycles in function <code>Analyze</code> where only these objects are required. The default is <code>FALSE</code> .  |

**Value**

A named list object containing these results of the analysis:

**arclength** The length of the test information or scale curve.

**arclengthvec** Positions on the test information or scale curve corresponding to a fine mesh of score index values (typically 101 values between 0 and 100).

**arclengthfd** Functional data object representing the relation between the score index abscissa and the arclength or information ordinate.

**theta\_al** A vector of positions on the test information or scale curve corresponding to the input score index values in argument theta.

**Qvec\_al** Values in arc length of the five marker percentages.

**binctr\_al** Values in arc length of the bin centers.

**Wfd.info** A functional data object representing the relation between the arclength or information abscissa and the score index ordinate.

**Wdim.index** The dimension of the overspace, which equal to sum of the number of options in the items specified in itemindex.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[Wpca.plot](#)

**Examples**

```
# Example 1. Display the arc length curve for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
indfine      <- seq(0,100,len=101)
WfdList      <- Quantshort_parList$WfdList
theta        <- Quantshort_parList$theta
Qvec         <- Quantshort_parList$Qvec
binctr       <- Quantshort_parList$binctr
arclenList   <- theta2arclen(theta, Qvec, WfdList, binctr)
names(arclenList)
oldpar <- par(no.readonly=TRUE)
ArcLength.plot(arclenList$arclength, arclenList$arclengthvec)
# Example 2. Display the arc length curve for the
```

```
# Symptom Distress Scale with 13 items and 473 respondents
# Proceed as above changing "Quant" to "SDS".
par(oldpar)
```

---

|          |                               |
|----------|-------------------------------|
| thetafun | <i>Compute optimal scores</i> |
|----------|-------------------------------|

---

## Description

The percentile score index values are estimated for each person. The estimates minimize the negative log likelihoods, which are a type of surprisal. The main optimization method is a safe-guarded Newton-Raphson method.

For any iteration the method uses only those scores that are within the interior of the interval [0,100] or at a boundary with a first derivative that would take a step into the interior, and have second derivative values exceeding the value of argument `crit`. Consequently the number of values being optimized decrease on each iteration, and iterations cease when either all values meet the convergence criterion or are optimized on a boundary, or when the number of iterations reaches `itermax`. At that point, if there are any interior scores still associated with either non-positive second derivatives or values that exceed `crit`, the minimizing value along a fine mesh is used.

If `itdisp` is positive, the number of values to be estimated are printed for each iteration.

## Usage

```
thetafun(theta, WfdList, U, itermax = 20, crit = 0.001,
         itdisp = FALSE)
```

## Arguments

- |                      |  |
|----------------------|--|
| <code>theta</code>   | A vector of size N containing initial values for score indices in the interval [0,100].  |
| <code>WfdList</code> | <p>A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <code>WfdList</code> is a named list containing information computed during the analysis. The named list in each member contains these objects:</p> <ul style="list-style-type: none"> <li>• <code>Wfd</code>: A functional data object containing the M surprisal curves for a question.</li> <li>• <code>M</code>: The number of options.</li> <li>• <code>Pbin</code>: A matrix containing proportions at each bin.</li> <li>• <code>Wbin</code>: A matrix containing surprisal values at each bin.</li> <li>• <code>Pmatfine</code>: A matrix of probabilities over a fine mesh.</li> <li>• <code>Wmatfine</code>: A matrix of surprisal values over a fine mesh.</li> <li>• <code>DWmatfine</code>: A matrix of the values of the first derivative of surprisal curves over fine mesh.</li> <li>• <code>D2Wmatfine</code>: A matrix of the values of the second derivative of surprisal curves over fine mesh.</li> </ul> |

|         |  |
|---------|--|
| U       | A matrix number of rows equal to the number of examinees or respondents, and number of columns equal to number of items. The values in the matrix are indices of choices made by each respondent to each question. |
| itermax | Maximum number of iterations for computing the optimal theta values. Default is 20.  |
| crit    | Criterion for convergence of optimization. Default is 1e-8.  |
| itdisp  | If TRUE, results are displayed for each iteration.   |

**Value**

A named list with these members:

**theta\_out:** A vector of optimized score index value.

**Hval:** The negative log likelihood criterion.

**DHval:** The first derivative of the negative likelihood.

**D2Hval:** The second derivative of the negative likelihood.

**iter:** The number iterations used.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[theta.distn](#), [Hfun](#), [DHfun](#), [theta2arclen](#), [testscore](#), [scoreDensity](#)

---

thetasearch

*Ensure that estimated score index is global*

---

**Description**

Multiple minima are found quite often in the data fitting function that is minimized using function `thetafun`, and in roughly 10 percent of the estimates there is a minimum that is lower than that detected. The function searches a mesh of 101 points for minima, computes the fitting function at the minima, and assigns the location of the global minimum as the replacement theta if the location differs by more than 0.5 from the value identified by `thetafun`. The function values and their first two derivatives are also replaced.

**Usage**

```
thetasearch(WfdList, U, theta, Hval, DHval, D2Hval, thetaird=1:N)
```

**Arguments**

|          |  |
|----------|--|
| WfdList  | A list vector containing specifications of surprisal curves for each item. |
| U        | An N by n matrix containing indices of chosen items for each test taker.   |
| theta    | A vector containing all the score index values.                            |
| Hval     | A vector containing the N function values.                                 |
| DHval    | A vector containing the N first derivative values.                         |
| D2Hval   | A vector containing the N second derivative values.                        |
| thetaird | A vector containing indices of values to be processed.                     |

**Value**

A named list object containing objects produced from analyzing the simulations, one set for each simulation:

**theta:** A vector containing all the score index values including those that are altered.

**Hval:** A vector containing the N function values included those that are altered.

**DHval:** A vector containing the N first derivative values included those that are altered.

**D2Hval:** A vector containing the N second derivative values included those that are altered.

**changeindex:** Indices of the theta values that are altered

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

<http://testgardener.azurewebsites.net>

**See Also**

[thetafun](#)

### Examples

```
# Search for values of theta that are not at the global minimum of the
# fitting function and replace them as well as their function and
# derivative values associated with the fine grid value nearest the
# the global minimum.
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
Hval <- Quantshort_parList$Hval
DHval <- Quantshort_parList$DHval
D2Hval <- Quantshort_parList$D2Hval
U <- Quantshort_dataList$U
Result <- thetasearch(WfdList, U, theta, Hval, DHval, D2Hval, thetaind=1:1000)
changeindex <- Result$changeindex
print(paste("Number changed =",length(changeindex)))
change <- theta[changeindex] - Result$theta[changeindex]
oldpar <- par(no.readonly=TRUE)
hist(change,101)
par(oldpar)
```

---

Ushort

*Test data for 24 math calculation questions from the SweSAT Quantitative data.*

---

### Description

These data are for a randomly selected subset of 1000 examinees.

### Usage

Ushort

### Format

A .txt file with 1000 rows each containing 24 integers in string format. The integers indicate which answer was chosen for each question by the examinee associated with the row.

### Details

The code above inputs the contents of the file using the scan function into a single character vector of length 24,000. The strings are converted to integers by the third command, and the integer vector is then reformatted into a 1000 by 24 matrix containing choice indices. The subsequent analysis of these data is described in detail in the vignette SweSATQuantitativeShort.

---

 Usimulate

*Simulate a test or scale data matrix.*


---

### Description

Used in `dataSimulation`, this function sets up an  $N$  by  $n$  matrix of index values that specify the index of the option chosen by an examinee or respondent for a specific question.

### Usage

```
Usimulate(theta.pop, WfdList)
```

### Arguments

|                        |   |
|------------------------|---|
| <code>theta.pop</code> | A vector containing population score index values at which data are to be simulated.  |
| <code>WfdList</code>   | A numbered list object produced by a <code>TestGardener</code> analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <code>WfdList</code> is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd:</b> A functional data object containing the $M$ surprisal curves $f$ . or a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |

### Details

For each question and each examinee a vector of random multinomial integer values is generated using the probability transforms of the surprisal curves and the examinee's score index value.

### Value

An  $N$  by  $n$  matrix of integer index values.

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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---

Wbinsmth

*Estimate the option probability and surprisal curves.*


---

### Description

The surprisal curves for each item are fit to the surprisal transforms of choice probabilities for each of a set of bins of current performance values `theta`. The error sums of squares are minimized by the surprisal optimization `smooth.surp` in the `fda` package. The output is a list vector of length `n` containing the functional data objects defining the curves.

### Usage

```
Wbinsmth(theta, dataList, WfdList=dataList$WfdList,
          thetaQnt=seq(0,100, len=2*nbin+1), wtvec=matrix(1,n,1),
          iterlim=20, conv=1e-4, dbglev=0)
```

### Arguments

- |                       |  |
|-----------------------|--|
| <code>theta</code>    | A vector of length <code>N</code> containing current values of score index percentile values.  |
| <code>dataList</code> | A list that contains the objects needed to analyse the test or rating scale with the following fields: <ul style="list-style-type: none"> <li><b>U:</b> A matrix of response data with <code>N</code> rows and <code>n</code> columns where <code>N</code> is the number of examinees or respondents and <code>n</code> is the number of items. Entries in the matrices are the indices of the options chosen. Column <code>i</code> of <code>U</code> is expected to contain only the integers <code>1, . . . , noption</code>.</li> <li><b>optList:</b> A list vector containing the numerical score values assigned to the options for this question.</li> <li><b>key:</b> If the data are from a test of the multiple choices type where the right answer is scored 1 and the wrong answers 0, this is a numeric vector of length <code>n</code> containing the indices the right answers. Otherwise, it is <code>NULL</code>.</li> <li><b>WfdPar:</b> An <code>fdPar</code> object for the defining the surprisal curves.</li> <li><b>noption:</b> A numeric vector of length <code>n</code> containing the numbers of options for each item.</li> <li><b>nbin:</b> The number of bins for binning the data.</li> <li><b>scrrng:</b> A vector of length 2 containing the limits of observed sum scores.</li> <li><b>scrfine:</b> A fine mesh of test score values for plotting.</li> <li><b>scrvec:</b> A vector of length <code>N</code> containing the examinee or respondent sum scores.</li> <li><b>itemvec:</b> A vector of length <code>n</code> containing the question or item sum scores.</li> <li><b>percntrnk:</b> A vector length <code>N</code> containing the sum score percentile ranks.</li> <li><b>thetaQnt:</b> A numeric vector of length <code>2*nbin + 1</code> containing the bin boundaries alternating with the bin centers. These are initially defined as <code>seq(0, 100, len=2*nbin+1)</code>.</li> <li><b>Wdim:</b> The total dimension of the surprisal scores.</li> <li><b>PcntMarkers:</b> The marker percentages for plotting: 5, 25, 50, 75 and 95.</li> </ul> |

|          |  |
|----------|--|
| WfdList  | <p>A numbered list object produced by a TestGardener analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of WfdList is a named list containing information computed during the analysis. These named lists contain these objects:</p> <p><b>Wfd:</b> A functional data object containing the <math>M</math> surprisal curves for a question.</p> <p><b>M:</b> The number of options.</p> <p><b>Pbin:</b> A matrix containing proportions at each bin.</p> <p><b>Wbin:</b> A matrix containing surprisal values at each bin.</p> <p><b>indfine:</b> A vector of length 101 containing equally spaced plotting points.</p> <p><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.</p> <p><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.</p> <p><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.</p> <p><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh.</p> <p>By default Wbinsmth uses the WfdList member of dataList, which is generated by the initialization with Wbinsmth.init within make.dataList. Usually this is what is required. However, WfdList may occasionally need to be entered from another source, and so included here as a separate argument.</p> |
| thetaQnt | A vector of length $2*n+1$ containing the sequence of bin boundary and bin centre values.  |
| wtvec    | A vector of length $n$ of weights on observations. Defaults to all ones.   |
| iterlim  | The maximum number of iterations used in optimizing surprisal curves. Defaults to 20.  |
| conv     | Convergence tolerance. Defaults to 0.0001.   |
| dbglev   | Level of output within Wbinsmth. If 0, no output, if 1 the error sum of squares and slope on each iterations, and if 2 or higher, results for each line search iteration with function lnsrch.   |

## Details

The function first bins the data in order to achieve rapid estimation of the option surprisal curves. The argument thetaQnt contains the sequence of bin boundaries separated by the bin centers, so that it is of length  $2*nbin + 1$  where nbin is the number of bins. These bin values are distributed over the percentile interval  $[0,100]$  so that the lowest boundary is 0 and highest 100. Prior to the call to Wbinsmth these boundaries are computed so that the numbers of values of theta falling in the bins are roughly equal. It is important that the number of bins be chosen so that the bins contain at least about 25 values.

After the values of theta are binned, the proportions that the bins are chosen for each question and each option are computed. Proportions of zero are given NA values.

The positive proportions are then converted to surprisal values where surprisal =  $-\log_M$  (proportion) where  $\log_M$  is the logarithm with base  $M$ , the number of options associated with a question. Bins with zero proportions are assigned a surprisal that is appropriately large in the sense of being in the range of the larger surprisal values associated with small but positive proportions.

The next step is to fit the surprisal values for each question by a functional data object that is smooth, passes as closely as possible to an option's surprisal values, and has values consistent with being a surprisal value. The function `smooth.surp()` is used for this purpose.

Finally the curves and other results for each question are saved in object `WfdList`, a list vector of length `n`, and the list vector is returned.

### Value

The optimized numbered list object produced by `Wbinsmth`. See above for its description.

### Author(s)

Juan Li and James Ramsay

### References

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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### See Also

[ICC.plot](#), [thetafun](#)

### Examples

```
# Example 1. Display the item probability and surprisal curves for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# estimate the initial surprisal curves
theta <- Quantshort_dataList$percncrnk
thetaQnt <- Quantshort_parList$thetaQnt
Qvec <- Quantshort_parList$Qvec
WfdResult <- Wbinsmth(theta, Quantshort_dataList)
WfdList <- WfdResult$WfdList
# plot the curves for the first question
binctr <- Quantshort_parList$binctr
scrfine <- seq(0,100,len=101)
ICC.plot(scrfine, WfdList, Quantshort_dataList, Qvec, binctr,
         plotindex=1, plorange=c(0,100))
# estimate the final surprisal curves
theta <- Quantshort_parList$theta
thetaQnt <- Quantshort_parList$thetaQnt
Qvec <- Quantshort_parList$Qvec
WfdList <- Quantshort_parList$WfdList
# plot the curves for the first question
ICC.plot(scrfine, WfdList, Quantshort_dataList, Qvec, binctr,
         plotindex=1, plorange=c(0,100))
# Example 2. Display the item probability and surprisal curves for the
# Symptom Distress Scale with 13 items and 473 respondents.
```

```
# Proceed as above changing "Quant" to "SDS"
```

---

|           |  |
|-----------|--|
| Wpca.plot | <i>Plot the test information or scale curve in either two or three dimensions.</i> |
|-----------|--|

---

### Description

A test or scale analysis produces a space curve that varies with in the space of possible option curves of dimension `Wdim`. Fortunately, it is usual that most of the shape variation in the curve is within only two or three dimensions, and these can be fixed by using functional principal components analysis.

### Usage

```
Wpca.plot(arclength, WfdList, Wdim, nharm=2, rotate=TRUE, dodge=1.003,
          titlestr=NULL, Display=TRUE)
```

### Arguments

|                        |   |
|------------------------|---|
| <code>arclength</code> | The total length of the test information or scale curve as computed by function <code>theta2arclen</code> .   |
| <code>WfdList</code>   | A numbered list object produced by a <code>TestGardener</code> analysis of a test. Its length is equal to the number of items in the test or questions in the scale. Each member of <code>WfdList</code> is a named list containing information computed during the analysis. These named lists contain these objects:<br><b>Wfd:</b> A functional data object containing the <code>M</code> surprisal curves for a question.<br><b>M:</b> The number of options.<br><b>Pbin:</b> A matrix containing proportions at each bin.<br><b>Wbin:</b> A matrix containing surprisal values at each bin.<br><b>Pmatfine:</b> A matrix of probabilities over a fine mesh.<br><b>Wmatfine:</b> A matrix of surprisal values over a fine mesh.<br><b>DWmatfine:</b> A matrix of the values of the first derivative of surprisal curves over fine mesh.<br><b>D2Wmatfine:</b> A matrix of the values of the second derivative of surprisal curves over fine mesh. |
| <code>Wdim</code>      | The total number of options in the test or scale.   |
| <code>nharm</code>     | The number of principal components of the test information or scale curve to be used to display the curve. Must be either 2 or 3.   |
| <code>rotate</code>    | If true, rotate principal components of the test information or scale curve to be used to display the curve to VARIMAX orientation.   |
| <code>dodge</code>     | A constant greater than 1 required by <code>ggplot2</code> . Defaults to 1.003.   |
| <code>titlestr</code>  | A string for the title of the plot. Defaults to NULL.   |
| <code>Display</code>   | A logical value that is TRUE if the test information manifold is to be displayed.   |

**Value**

A named list with these members:

|              |   |
|--------------|---|
| pcaplot      | If two dimensions or harmonics are specified, this is a gg or ggplot object that can be displayed using the print command. If three dimensions are specified, this is NULL. |
| harmvarmxfd  | Functional data objects for the principal components of the curve shape.  |
| varpropvarmx | Proportions of variance accounted for by the principal components   |

The principal components are VARIMAX rotated by default. The plot is displayed as a side value even if no output object is specified in the call to the function.

**Author(s)**

Juan Li and James Ramsay

**References**

Ramsay, J. O., Li J. and Wiberg, M. (2020) Full information optimal scoring. *Journal of Educational and Behavioral Statistics*, 45, 297-315.

Ramsay, J. O., Li J. and Wiberg, M. (2020) Better rating scale scores with information-based psychometrics. *Psych*, 2, 347-360.

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**Examples**

```
# Example 1. Display the test information curve for the
# short SweSAT multiple choice test with 24 items and 1000 examinees
# plot a two-dimension version of manifold curve
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
arclength <- Quantshort_parList$arclength
oldpar <- par(no.readonly=TRUE)
on.exit(oldpar)
Wpca.plotResults <- Wpca.plot(arclength, WfdList, Quantshort_dataList$Wdim)
varprop <- Wpca.plotResults$varpropvarmx
print("Proportions of variance accounted for and their sum:")
print(round(c(varprop,sum(varprop)),3))
# plot a three-dimension version of manifold curve
WfdList <- Quantshort_parList$WfdList
theta <- Quantshort_parList$theta
arclength <- Quantshort_parList$arclength
Wpca.plotResults <- Wpca.plot(arclength, WfdList, Quantshort_dataList$Wdim, nharm=3)
varprop <- Wpca.plotResults$varpropvarmx
print("Proportions of variance accounted for and their sum:")
print(round(c(varprop,sum(varprop)),3))
# Example 2. Display the test information curve for the
# Symptom Distress Scale with 13 items and 473 respondents.
# Proceed as above changing "Quant" to "SDS"
```

# Index

## \* datasets

keyshort, [24](#)  
Quantshort\_dataList, [31](#)  
Quantshort\_infoList, [32](#)  
Quantshort\_key, [33](#)  
Quantshort\_parList, [33](#)  
Quantshort\_U, [34](#)  
SDS\_dataList, [38](#)  
SDS\_infoList, [39](#)  
SDS\_key, [40](#)  
SDS\_parList, [41](#)  
SDS\_U, [42](#)  
Ushort, [56](#)

## \* smooth

TG\_density.fd, [47](#)

Analyze, [3](#), [27](#)

ArcLength.plot, [5](#)

dataSimulation, [5](#), [6](#), [37](#)

density\_plot, [8](#)

DHfun, [9](#), [18](#), [54](#)

entropies, [11](#)

Entropy.plot, [12](#), [12](#), [24](#), [30](#), [45](#)

Hcurve, [14](#)

Hfun, [10](#), [16](#), [17](#), [18](#), [54](#)

Hfuns.plot, [10](#), [14](#), [17](#), [17](#), [30](#)

ICC.fit, [18](#)

ICC.plot, [5](#), [14](#), [21](#), [21](#), [30](#), [45](#), [60](#)

intensity.fd, [48](#)

keyshort (keyshort), [24](#)

keyshort, [24](#)

make\_dataList, [5](#), [10](#), [17](#), [25](#)

mu.plot, [28](#)

Power.plot, [5](#), [14](#), [24](#), [29](#), [45](#)

Quantshort\_dataList, [31](#)

Quantshort\_infoList, [32](#)

Quantshort\_key, [33](#)

Quantshort\_parList, [33](#)

Quantshort\_U, [34](#)

scoreDensity, [5](#), [9](#), [29](#), [35](#), [46](#), [50](#), [54](#)

scorePerformance, [8](#), [36](#)

SDS, [38](#)

SDS\_dataList, [38](#)

SDS\_infoList, [39](#)

SDS\_key, [40](#)

SDS\_parList, [41](#)

SDS\_U, [42](#)

Sensitivity.plot, [5](#), [14](#), [24](#), [30](#), [43](#)

testscore, [5](#), [29](#), [35](#), [45](#), [50](#), [54](#)

TG\_density.fd, [47](#)

theta.distn, [5](#), [35](#), [49](#), [54](#)

theta2arclen, [5](#), [6](#), [35](#), [50](#), [50](#), [54](#)

thetafun, [5](#), [18](#), [21](#), [35](#), [50](#), [53](#), [55](#), [60](#)

thetasearch, [15](#), [54](#)

Ushort, [56](#)

Usimulate, [57](#)

usimulate (Usimulate), [57](#)

Wbinsmth, [5](#), [24](#), [58](#)

Wpca.plot, [5](#), [52](#), [61](#)