

# Package ‘Superpower’

September 3, 2020

**Title** Simulation-Based Power Analysis for Factorial Designs

**Version** 0.1.0

**Description** Functions to perform simulations of ANOVA designs of up to three factors. Calculates the observed power and average observed effect size for all main effects and interactions in the ANOVA, and all simple comparisons between conditions. Includes functions for analytic power calculations and additional helper functions that compute effect sizes for ANOVA designs, observed error rates in the simulations, and functions to plot power curves. Please see Lakens, D., & Caldwell, A. R. (2019). “Simulation-Based Power-Analysis for Factorial ANOVA Designs”. <doi:10.31234/osf.io/baxsf>.

**URL** <https://aaroncaldwell.us/SuperpowerBook/>

**BugReports** <https://github.com/arcaldwell49/Superpower/issues>

**License** MIT + file LICENSE

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.1.1

**Imports** mvtnorm, MASS, afex, emmeans, ggplot2, gridExtra, reshape2, stats, dplyr, magrittr, tidyselect, Hmisc

**Suggests** knitr, rmarkdown, pwr, testthat, covr, jmvcore

**VignetteBuilder** knitr

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2020-09-03 14:52:10 UTC

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alpha_standardized	<i>Compute standardized alpha level based on unstandardized alpha level and the number of observations N.</i>
--------------------	---

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### Description

Compute standardized alpha level based on unstandardized alpha level and the number of observations N.

### Usage

```
alpha_standardized(alpha, N, standardize_N = 100)
```

### Arguments

alpha	The unstandardized alpha level (e.g., 0.05), independent of the sample size.
N	The number of observations (e.g., the sample size) in the dataset
standardize_N	The number of observations (e.g., the sample size) you want to use to standardize the alpha level for. Defaults to 100 (base on Good, 1982).

### References

Good, I. J. (1982). C140. Standardized tail-area probabilities. *Journal of Statistical Computation and Simulation*, 16(1), 65–66. <<https://doi.org/10.1080/00949658208810607>>

**Examples**

```
## Check it yields .05 for N = 100:
alpha_standardized(alpha = 0.05, N = 100)
## Check it yields .05 for N = 200:
alpha_standardized(alpha = 0.07071068, N = 200)
## Which alpha should we use with N = 200?
alpha_standardized(alpha = 0.05, N = 200)
## You can change the standardization N, repeating the example above:
alpha_standardized(alpha = 0.05, N = 100, standardize_N = 200)
```

---

ANOVA_compromise	<i>Justify your alpha level by minimizing or balancing Type 1 and Type 2 error rates for ANOVAs.</i>
------------------	--

---

**Description**

Justify your alpha level by minimizing or balancing Type 1 and Type 2 error rates for ANOVAs.

**Usage**

```
ANOVA_compromise(
  design_result,
  correction = Superpower_options("correction"),
  emm = Superpower_options("emm"),
  emm_model = Superpower_options("emm_model"),
  contrast_type = Superpower_options("contrast_type"),
  emm_comp,
  costT1T2 = 1,
  priorH1H0 = 1,
  error = "minimal",
  liberal_lambda = Superpower_options("liberal_lambda")
)
```

**Arguments**

design_result	Output from the ANOVA_design function
correction	Set a correction of violations of sphericity. This can be set to "none", "GG" Greenhouse-Geisser, and "HF" Huynh-Feldt
emm	Set to FALSE to not perform analysis of estimated marginal means
emm_model	Set model type ("multivariate", or "univariate") for estimated marginal means
contrast_type	Select the type of comparison for the estimated marginal means. Default is pairwise. See ?emmeans::'contrast-methods' for more details on acceptable methods.
emm_comp	Set the comparisons for estimated marginal means comparisons. This is a factor name (a), combination of factor names (a+b), or for simple effects a   sign is needed (alb)

costT1T2	Relative cost of Type 1 errors vs. Type 2 errors.
priorH1H0	How much more likely a-priori is H1 than H0? Default is 1: equally likely.
error	Either "minimal" to minimize error rates, or "balance" to balance error rates.
liberal_lambda	Logical indicator of whether to use the liberal ( $\text{cohen\_f}^2 * (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen\_f}^2 * \text{den\_df}$ ) calculation of the noncentrality (lambda) parameter estimate. Default is FALSE.

### Value

Returns dataframe with simulation data (power and effect sizes!), optimal alpha level, obtained beta error rate (1-power/100), and objective (see below for details). If NA is obtained in a alpha/beta/objective columns this indicates there is no effect for this particular comparison. Also returns alpha-beta compromise plots for all comparisons. Note: Cohen's  $f = \sqrt{\text{pes}/(1-\text{pes})}$  and the noncentrality parameter is  $= f^2 * \text{df}(\text{error})$

"aov\_comp" A dataframe of ANOVA-level results.

"aov\_plotlist" List of plots for ANOVA-level effects

"manova\_comp" A dataframe of MANOVA-level results.

"manova\_plotlist" List of plots for MANOVA-level effects.

"emmeans\_comp" A dataframe of ANOVA-level results.

"emm\_plotlist" List of plots for estimated marginal means contrasts.

alpha = alpha or Type 1 error that minimizes or balances combined error rates  
 beta = beta or Type 2 error that minimizes or balances combined error rates  
 objective = value that is the result of the minimization, either 0 (for balance) or the combined weighted error rates

### References

too be added

### Examples

```
## Not run:
design_result <- ANOVA_design(design = "3b*2w",
  n = 6,
  mu = c(1, 2, 2, 3, 3, 4),
  sd = 3,
  plot = FALSE)
example = ANOVA_compromise(design_result, emm = TRUE, emm_comp = "a")

## End(Not run)
```

---

ANOVA_design	<i>Design function used to specify the parameters to be used in simulations</i>
--------------	---

---

### Description

Design function used to specify the parameters to be used in simulations

### Usage

```
ANOVA_design(
  design,
  n,
  mu,
  sd,
  r = 0,
  labelnames = NULL,
  plot = Superpower_options("plot")
)
```

### Arguments

design	String specifying the ANOVA design.
n	Sample size in each condition
mu	Vector specifying mean for each condition
sd	standard deviation for all conditions (or a vector specifying the sd for each condition)
r	Correlation between dependent variables (single value or matrix)
labelnames	Optional vector to specifying factor and condition names (recommended, if not used factors and levels are indicated by letters and numbers)
plot	Should means plot be printed (defaults to TRUE)

### Value

Returns single list with simulated data, design, design list, factor names, formulas for ANOVA, means, sd, correlation, sample size per condition, correlation matrix, covariance matrix, design string, labelnames, labelnameslist, factor names, meansplot

"dataframe" A sample dataframe of what data could look like given the proposed parameters.

"design" aov The design string, e.g. "2b\*2w".

"design\_list" The list of variables in the design.

"frm1" The first formula created for this design.

"frm2" The second formula created for this design.

"mu" Vector of means.

"sd" Vector of standard deviations.  
 "r" Common correlation coefficient.  
 "n" Sample size per cell. Can be entered as a single value or list of sample sizes for each condition.  
 If unequal n is entered then the design can only be passed onto ANOVA\_power.  
 "cor\_mat" The correlation matrix.  
 "sigmatrix" The variance-covariance matrix.  
 "design\_factors" Total number of within-subjects factors.  
 "labelnames" List of the label names.  
 "labelnameslist" Secondary list of labelnames  
 "factornames" List of the factor titles.  
 "meansplot" Plot of the experimental design.

### Warnings

Varying the sd or r (e.g., entering multiple values) violates assumptions of homoscedascity and sphericity respectively

### Examples

```
## Set up a within design with 2 factors, each with 2 levels,
## with correlation between observations of 0.8,
## 40 participants (who do all conditions), and standard deviation of 2
## with a mean pattern of 1, 0, 1, 0, conditions labeled 'condition' and
## 'voice', with names for levels of "cheerful", "sad", and "human", "robot"
ANOVA_design(design = "2w*2w", n = 40, mu = c(1, 0, 1, 0), sd = 2, r = 0.8,
  labelnames = c("condition", "cheerful", "sad", "voice", "human", "robot"))
```

---

ANOVA\_exact

*Simulates an exact dataset (mu, sd, and r represent empirical, not population, mean and covariance matrix) from the design to calculate power*

---

### Description

Simulates an exact dataset (mu, sd, and r represent empirical, not population, mean and covariance matrix) from the design to calculate power

### Usage

```
ANOVA_exact(
  design_result,
  correction = Superpower_options("correction"),
  alpha_level = Superpower_options("alpha_level"),
  verbose = Superpower_options("verbose"),
  emm = Superpower_options("emm"),
```

```

    emm_model = Superpower_options("emm_model"),
    contrast_type = Superpower_options("contrast_type"),
    liberal_lambda = Superpower_options("liberal_lambda"),
    emm_comp
  )

ANOVA_exact2(
  design_result,
  correction = Superpower_options("correction"),
  alpha_level = Superpower_options("alpha_level"),
  verbose = Superpower_options("verbose"),
  emm = Superpower_options("emm"),
  emm_model = Superpower_options("emm_model"),
  contrast_type = Superpower_options("contrast_type"),
  emm_comp,
  liberal_lambda = Superpower_options("liberal_lambda")
)

```

### Arguments

<code>design_result</code>	Output from the ANOVA_design function
<code>correction</code>	Set a correction of violations of sphericity. This can be set to "none", "GG" Greenhouse-Geisser, and "HF" Huynh-Feldt
<code>alpha_level</code>	Alpha level used to determine statistical significance
<code>verbose</code>	Set to FALSE to not print results (default = TRUE)
<code>emm</code>	Set to FALSE to not perform analysis of estimated marginal means
<code>emm_model</code>	Set model type ("multivariate", or "univariate") for estimated marginal means
<code>contrast_type</code>	Select the type of comparison for the estimated marginal means. Default is pairwise. See ?emmeans::'contrast-methods' for more details on acceptable methods.
<code>liberal_lambda</code>	Logical indicator of whether to use the liberal ( $\text{cohen\_f}^2 \cdot (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen\_f}^2 \cdot \text{den\_df}$ ) calculation of the noncentrality (lambda) parameter estimate. Default is FALSE.
<code>emm_comp</code>	Set the comparisons for estimated marginal means comparisons. This is a factor name (a), combination of factor names (a+b), or for simple effects a   sign is needed (alb)

### Value

Returns dataframe with simulation data (power and effect sizes!), anova results and simple effect results, plot of exact data, and alpha\_level. Note: Cohen's  $f = \sqrt{\text{pes}/(1-\text{pes})}$  and the noncentrality parameter is  $f^2 \cdot \text{df}(\text{error})$

"dataframe" A dataframe of the simulation result.

"aov\_result" aov object returned from [aov\\_car](#).

"aov\_result" emmeans object returned from [emmeans](#).

"main\_result" The power analysis results for ANOVA level effects.

"pc\_results" The power analysis results for the pairwise (t-test) comparisons.

"emm\_results" The power analysis results of the pairwise comparison results.

"manova\_results" Default is "NULL". If a within-subjects factor is included, then the power of the multivariate (i.e. MANOVA) analyses will be provided.

"alpha\_level" The alpha level, significance cut-off, used for the power analysis.

"method" Record of the function used to produce the simulation

"plot" A plot of the dataframe from the simulation; should closely match the meansplot in [ANOVA\\_design](#)

### Functions

- ANOVA\_exact2: An extension of ANOVA\_exact that uses the effect sizes calculated from very large sample size empirical simulation. This allows for small sample sizes, where ANOVA\_exact cannot, while still accurately estimating power. However, model objects (emmeans and aov) are not included as output, and pairwise (t-test) results are not currently supported.

### Warnings

Varying the sd or r (e.g., entering multiple values) violates assumptions of homoscedasticity and sphericity respectively

### Examples

```
## Set up a within design with 2 factors, each with 2 levels,
## with correlation between observations of 0.8,
## 40 participants (who do all conditions), and standard deviation of 2
## with a mean pattern of 1, 0, 1, 0, conditions labeled 'condition' and
## 'voice', with names for levels of "cheerful", "sad", and "human", "robot"
design_result <- ANOVA_design(design = "2w*2w", n = 40, mu = c(1, 0, 1, 0),
  sd = 2, r = 0.8, labelnames = c("condition", "cheerful",
  "sad", "voice", "human", "robot"))
exact_result <- ANOVA_exact(design_result, alpha_level = 0.05)
```

---

ANOVA\_power

*Simulation function used to estimate power*

---

### Description

Simulation function used to estimate power



**Usage**

```
ANOVA_power(
  design_result,
  alpha_level = Superpower_options("alpha_level"),
  correction = Superpower_options("correction"),
  p_adjust = "none",
  nsims = 1000,
  seed = NULL,
  verbose = Superpower_options("verbose"),
  emm = Superpower_options("emm"),
  emm_model = Superpower_options("emm_model"),
  contrast_type = Superpower_options("contrast_type"),
  emm_p_adjust = "none",
  emm_comp = NULL
)
```

**Arguments**

<code>design_result</code>	Output from the ANOVA_design function
<code>alpha_level</code>	Alpha level used to determine statistical significance
<code>correction</code>	Set a correction of violations of sphericity. This can be set to "none", "GG" Greenhouse-Geisser, and "HF" Huynh-Feldt
<code>p_adjust</code>	Correction for multiple comparisons. This will adjust p values for ANOVA/MANOVA level effects; see ?p.adjust for options
<code>nsims</code>	number of simulations to perform
<code>seed</code>	Set seed for reproducible results
<code>verbose</code>	Set to FALSE to not print results (default = TRUE)
<code>emm</code>	Set to FALSE to not perform analysis of estimated marginal means
<code>emm_model</code>	Set model type ("multivariate", or "univariate") for estimated marginal means
<code>contrast_type</code>	Select the type of comparison for the estimated marginal means. Default is pairwise. See ?emmeans::'contrast-methods' for more details on acceptable methods.
<code>emm_p_adjust</code>	Correction for multiple comparisons; default is "none". See ?summary.emmGrid for more details on acceptable methods.
<code>emm_comp</code>	Set the comparisons for estimated marginal means comparisons. This is a factor name (a), combination of factor names (a+b), or for simple effects a   sign is needed (alb)

**Value**

Returns dataframe with simulation data (p-values and effect sizes), anova results (type 3 sums of squares) and simple effect results, and plots of p-value distribution.

"sim\_data" Output from every iteration of the simulation

"main\_result" The power analysis results for ANOVA effects.

"pc\_results" The power analysis results for pairwise comparisons.

"manova\_results" Default is "NULL". If a within-subjects factor is included, then the power of the multivariate (i.e. MANOVA) analyses will be provided.

"emm\_results" The power analysis results of the estimated marginal means.

"plot1" Distribution of p-values from the ANOVA results.

"plot2" Distribution of p-values from the pairwise comparisons results.

"correction" The correction for sphericity applied to the simulation results.

"p\_adjust" The p-value adjustment applied to the simulation results for ANOVA/MANOVA omnibus tests and t-tests.

"emm\_p\_adjust" The p-value adjustment applied to the simulation results for the estimated marginal means.

"nsims" The number of simulations run.

"alpha\_level" The alpha level, significance cut-off, used for the power analysis.

"method" Record of the function used to produce the simulation

## References

too be added

## Examples

```
## Not run:
## Set up a within design with 2 factors, each with 2 levels,
## with correlation between observations of 0.8,
## 40 participants (who do all conditions), and standard deviation of 2
## with a mean pattern of 1, 0, 1, 0, conditions labeled 'condition' and
## 'voice', with names for levels of "cheerful", "sad", amd "human", "robot"
design_result <- ANOVA_design(design = "2w*2w", n = 40, mu = c(1, 0, 1, 0),
  sd = 2, r = 0.8, labelnames = c("condition", "cheerful",
  "sad", "voice", "human", "robot"))
power_result <- ANOVA_power(design_result, alpha_level = 0.05,
  p_adjust = "none", seed = 2019, nsims = 10)

## End(Not run)
```

---

design\_aov-methods      *Methods for design\_aov objects*

---

## Description

Methods defined for objects returned from the ANOVA\_design functions.

**Usage**

```
## S3 method for class 'design_aov'
print(x, ...)

## S3 method for class 'design_aov'
plot(x, ...)
```

**Arguments**

x                    object of class design\_aov as returned from ANOVA\_design

...                  further arguments passed through, see description of return value for details.  
[ANOVA\\_design](#).

**Value**

print Prints short summary of the study design created from ANOVA\_design function

plot Returns meansplot from created from the ANOVA\_design function

---

emmeans_power	<i>Compute power for <b>emmeans</b> contrasts</i>
---------------	---

---

**Description**

Computes power based on t value and degrees of freedom for contrasts. *Do not use to calculate "observed power" for empirical datasets (Hoenig & Heisey, 2001).*

**Usage**

```
emmeans_power(x, ...)

## S3 method for class 'emmGrid'
emmeans_power(x, ...)

## S3 method for class 'summary_em'
emmeans_power(x, ...)

## S3 method for class 'data.frame'
emmeans_power(
  x,
  alpha_level = Superpower_options("alpha_level"),
  liberal_lambda = Superpower_options("liberal_lambda"),
  ...
)
```

**Arguments**

x	emmGrid. Grid of contrasts to estimate power from.
...	Other arguments passed to the function if object is not already a emmGrid object.
alpha_level	Alpha level used to determine statistical significance
liberal_lambda	Logical indicator of whether to use the liberal ( $\text{cohen\_f}^2 \times (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen\_f}^2 \times \text{den\_df}$ ) calculation of the noncentrality (lambda) parameter estimate. Default is FALSE.

**Details**

Note that calculation of power is based on the F- and t-ratio assuming two-sided testing. Thus, the function does not honor adjustments of the testing procedure due to either one-sided testing (or two-one sided tests) or corrections for multiple comparisons via the `p.adjust` option in `emmeans`.

Power for one-sided tests can be calculated, if the means of the simulated dataset are consistent with the directional hypothesis, by doubling `alpha_level`. Similarly, power for Bonferroni-corrected contrasts can be calculated by adjusting `alpha_level` accordingly (see examples). ... Other arguments passed onto the function

**Value**

Returns dataframe with simulation data (power and effect sizes!), anova results and simple effect results, plot of exact data, and `alpha_level`. Note: Cohen's  $f = \sqrt{(\text{pes}/1 - \text{pes})}$  and the noncentrality parameter is  $f^2 \times \text{df}(\text{error})$

"dataframe" A dataframe of the simulation result.

"aov\_result" aov object returned from `aov_car`.

"aov\_result" emmeans object returned from `emmeans`.

"main\_result" The power analysis results for ANOVA level effects.

"pc\_results" The power analysis results for the pairwise (t-test) comparisons.

"emm\_results" The power analysis results of the pairwise comparison results.

"manova\_results" Default is "NULL". If a within-subjects factor is included, then the power of the multivariate (i.e. MANOVA) analyses will be provided.

"alpha\_level" The alpha level, significance cut-off, used for the power analysis.

"method" Record of the function used to produce the simulation

"plot" A plot of the dataframe from the simulation; should closely match the meansplot in `ANOVA_design`

**Author(s)**

Frederik Aust

**References**

Hoening, J. M., & Heisey, D. M. (2001). The Abuse of Power. *The American Statistician*, 55(1), 19–24. <https://doi.org/10.1198/000313001300339897>

**Examples**

```

## Not run:
# Set up a within design with 2 factors, each with 2 levels
design_result <- ANOVA_design(design = "2w*2w",
n = 40, mu = c(1, 0, 1, 0),
sd = 2, r = 0.8,
labelnames = c("condition", "cheerful",
"sad", "voice", "human", "robot"))

exact_result <- ANOVA_exact(design_result,
alpha_level = 0.05, verbose = FALSE,
emm = TRUE, contrast_type = "pairwise")

# Power for pairwise contrasts
exact_result$emm_results

# Corresponding emmeans contrasts
exact_result$emmeans$contrasts

# Manually recalculate power
emmmeans_power(exact_result$emmeans$contrasts,
alpha_level = 0.05)

# Calculate power for Bonferroni-adjusted pairwise comparisons
n_contrasts <- nrow(as.data.frame(exact_result$emmeans$contrasts))
emmmeans_power(exact_result$emmeans$contrasts,
alpha_level = 0.05 / n_contrasts)

# Calculate power for one-sided custom contrasts
exact_result$emmeans$emmeans
custom_contrast <- contrast(exact_result$emmeans$emmeans,
list(robot_vs_sad_human = c(0, 1, -0.5, -0.5)))
emmmeans_power(custom_contrast,
alpha_level = 0.05 * 2)

# Calculate power for follow-up ANOVA
follow_up <- joint_tests(exact_result$emmeans$emmeans,
by = "condition")
emmmeans_power(follow_up,
alpha_level = 0.05 / 2)
emmmeans_power(emmeans(exact_result$emmeans$emmeans,
pairwise ~ voice | condition)$contrasts,
alpha_level = 0.05 / 2)

## End(Not run)

```

---

mu\_from\_ES

*Convenience function to calculate the means for between designs with one factor (One-Way ANOVA). Can be used to determine the means that should yield a specified effect sizes (expressed in Cohen's f).*

---

**Description**

Convenience function to calculate the means for between designs with one factor (One-Way ANOVA). Can be used to determine the means that should yield a specified effect sizes (expressed in Cohen's  $f$ ).

**Usage**

```
mu_from_ES(K, ES)
```

**Arguments**

K	Number of groups (2, 3, or 4)
ES	Effect size (eta-squared)

**Value**

Returns vector of means

**References**

Albers, C., & Lakens, D. (2018). When power analyses based on pilot data are biased: Inaccurate effect size estimators and follow-up bias. *Journal of Experimental Social Psychology*, 74, 187–195. <https://doi.org/10.1016/j.jesp.2017.09.004>

**Examples**

```
## Medium effect size (eta-squared), 2 groups
ES <- 0.0588
K <- 2
mu_from_ES(K = K, ES = ES)
```

---

optimal\_alpha

*Justify your alpha level by minimizing or balancing Type 1 and Type 2 error rates.*

---

**Description**

Justify your alpha level by minimizing or balancing Type 1 and Type 2 error rates.

**Usage**

```
optimal_alpha(
  power_function,
  costT1T2 = 1,
  priorH1H0 = 1,
  error = "minimal",
  plot = Superpower_options("plot")
)
```

**Arguments**

power_function	Function that outputs the power, calculated with an analytic function.
costT1T2	Relative cost of Type 1 errors vs. Type 2 errors.
priorH1H0	How much more likely a-priori is H1 than H0?
error	Either "minimal" to minimize error rates, or "balance" to balance error rate
plot	When set to TRUE, automatically outputs a plot of alpha (x-axis) and beta (y-axis) error rates

**Value**

alpha = alpha or Type 1 error that minimizes or balances combined error rates  
 beta = beta or Type 2 error that minimizes or balances combined error rates  
 objective = value that is the result of the minimization, either 0 (for balance) or the combined weighted error rates

**References**

too be added

**Examples**

```
## Optimize power for a independent t-test, smallest effect of interest
## d = 0.5, 100 participants per condition
res <- optimal_alpha(power_function = "pwr::pwr.t.test(d = 0.5, n = 100,
sig.level = x, type = 'two.sample', alternative = 'two.sided')$power")
res$alpha
res$beta
```

---

plot\_power

*Convenience function to plot power across a range of sample sizes.*

---

**Description**

Convenience function to plot power across a range of sample sizes.

**Usage**

```
plot_power(
  design_result,
  alpha_level = Superpower_options("alpha_level"),
  min_n = 7,
  max_n = 100,
  desired_power = 90,
  plot = Superpower_options("plot"),
  emm = Superpower_options("emm"),
  emm_model = Superpower_options("emm_model"),
  contrast_type = Superpower_options("contrast_type"),
```

```

    emm_comp,
    verbose = Superpower_options("verbose"),
    exact2 = FALSE,
    liberal_lambda = Superpower_options("liberal_lambda")
  )

```

### Arguments

design_result	Output from the ANOVA_design function
alpha_level	Alpha level used to determine statistical significance
min_n	Minimum sample size in power curve. Cannot be less than or equal to the product of factors. E.g., if design = "2b*2b" then min_n must be at least 5 ( $2^2+1=5$ )
max_n	Maximum sample size in power curve.
desired_power	Desired power (e.g., 80, 90). N per group will be highlighted to achieve this desired power in the plot. Defaults to 90.
plot	Should power plot be printed automatically (defaults to TRUE)
emm	Set to FALSE to not perform analysis of estimated marginal means
emm_model	Set model type ("multivariate", or "univariate") for estimated marginal means
contrast_type	Select the type of comparison for the estimated marginal means
emm_comp	Set the comparisons for estimated marginal means comparisons. This is a factor name (a), combination of factor names (a+b), or for simple effects a   sign is needed (alb)
verbose	Set to FALSE to not print results (default = TRUE)
exact2	Logical indicator for which ANOVA_exact function (ANOVA_exact or ANOVA_exact2) to use in the plots. Default is FALSE which uses ANOVA_exact which has sample size limitations.
liberal_lambda	Logical indicator of whether to use the liberal ( $\text{cohen\_f}^2 * (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen\_f}^2 * \text{den\_df}$ ) calculation of the noncentrality (lambda) parameter estimate. Default is FALSE.

### Value

Returns plot with power curves for the ANOVA, and a dataframe with the summary data.

"plot\_ANOVA" Plot of power curves from ANOVA results.

"plot\_MANOVA" Plot of power curves from MANOVA results. Returns NULL if no within-subject factors.

"plot\_emm" Plot of power curves from MANOVA results. Returns NULL if emm = FALSE.

"anova\_n" Achieved Power and Sample Size for ANOVA-level effects.

"manova\_n" Achieved Power and Sample Size for MANOVA-level effects.

"emm\_n" Achieved Power and Sample Size for estimated marginal means.

"power\_df" The tabulated ANOVA power results.

"power\_df\_manova" The tabulated MANOVA power results. Returns NULL if no within-subject factors.



"power\_df\_emm" The tabulated Estimated Marginal Means power results. Returns NULL if emm = FALSE.

"effect\_sizes" Effect sizes (partial eta-squared) from ANOVA results.

"effect\_sizes\_manova" Effect sizes (Pillai's Trace) from MANOVA results. Returns NULL if no within-subject factors.

"effect\_sizes\_emm" Effect sizes (cohen's f) estimated marginal means results. Returns NULL if emm = FALSE.

## References

too be added

## Examples

```
## Not run:
design_result <- ANOVA_design(design = "3b",
                             n = 20,
                             mu = c(0,0,0.3),
                             sd = 1,
                             labelnames = c("condition",
                                             "cheerful", "neutral", "sad"))

plot_power(design_result, min_n = 50, max_n = 70, desired_power = 90)

## End(Not run)
```

---

power.ftest

*Power Calculations for an F-test*

---

## Description

Compute power of test or determine parameters to obtain target power. Inspired by the pwr.f2.test function in the pwr package, but allows for varying noncentrality parameter estimates for a more liberal (default in pwr.f2.test) or conservative (default in this function) estimates (see Aberson, Chapter 5, pg 72).

## Usage

```
power.ftest(
  num_df = NULL,
  den_df = NULL,
  cohen_f = NULL,
  alpha_level = Superpower_options("alpha_level"),
  beta_level = NULL,
  liberal_lambda = Superpower_options("liberal_lambda")
)
```

**Arguments**

num_df	degrees of freedom for numerator
den_df	degrees of freedom for denominator
cohen_f	Cohen's f effect size. Note: this is the sqrt(f2) if you are used to using pwr.f2.test
alpha_level	Alpha level used to determine statistical significance.
beta_level	Type II error probability (power/100-1)
liberal_lambda	Logical indicator of whether to use the liberal ( $\text{cohen\_f}^2 * (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen\_f}^2 * \text{den\_df}$ ) calculation of the noncentrality (lambda) parameter estimate. Default is FALSE.

**Value**

num\_df = degrees of freedom for numerator, den\_df = degrees of freedom for denominator, cohen\_f = Cohen's f effect size, alpha\_level = Type 1 error probability, beta\_level = Type 2 error probability, power = Power of test ( $1 - \text{beta\_level} * 100$ ) lambda = Noncentrality parameter estimate (default =  $\text{cohen\_f}^2 * \text{den\_df}$ , liberal =  $\text{cohen\_f}^2 * (\text{num\_df} + \text{den\_df})$ )

**References**

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale, NJ: Lawrence Erlbaum. Aberson, C. (2019). Applied Power Analysis for the Behavioral Sciences (2nd ed.). New York, NY: Routledge.

**Examples**

```
design_result <- ANOVA_design(design = "2b",
  n = 65,
  mu = c(0, .5),
  sd = 1,
  plot = FALSE)
x1 = ANOVA_exact2(design_result, verbose = FALSE)
ex = power.ftest(num_df = x1$anova_table$num_df,
  den_df = x1$anova_table$den_df,
  cohen_f = x1$main_result$cohen_f,
  alpha_level = 0.05,
  liberal_lambda = FALSE)
```

---

power\_oneway\_between *Analytic power calculation for one-way between designs.*

---

**Description**

Analytic power calculation for one-way between designs.

**Usage**

```
power_oneway_between(design_result, alpha_level = 0.05)
```

**Arguments**

design\_result    Output from the ANOVA\_design function  
 alpha\_level    Alpha level used to determine statistical significance

**Value**

mu = means  
 sigma = standard deviation  
 n = sample size  
 alpha\_level = alpha level  
 Cohen\_f = Cohen f  
 f\_2 = Cohen's  $f^2$   
 lambda = lambda  
 F\_critical = Critical F-value  
 power = power  
 df1 = degrees of freedom for the effect  
 df2 = degrees of freedom of the error  
 eta\_p\_2 = partial eta-squared  
 mean\_mat = matrix of the means

**References**

too be added

**Examples**

```
## Set up a within design with one factor with 2 levels,
## 40 participants (woh do all conditions), and standard deviation of 2
## with a mean pattern of 1, 0, 1, conditions labeled 'condition'
## with names for levels of "cheerful", "neutral", "sad"
design_result <- ANOVA_design(design = "3b", n = 40, mu = c(1, 0, 1),
  sd = 2, labelnames = c("condition", "cheerful", "neutral", "sad"))
power_result <- power_oweway_between(design_result, alpha_level = 0.05)
```

---

power\_oweway\_within    *Analytic power calculation for one-way within designs.*

---

**Description**

Analytic power calculation for one-way within designs.

**Usage**

```
power_oweway_within(design_result, alpha_level = 0.05)
```

**Arguments**

`design_result` Output from the `ANOVA_design` function  
`alpha_level` Alpha level used to determine statistical significance

**Value**

`mu` = means  
`sigma` = standard deviation  
`n` = sample size  
`alpha_level` = alpha level  
`Cohen_f` = Cohen's  $f$   
`f_2` = Cohen's  $f$  squared  
`lambda` = lambda  
`F_critical` = Critical F-value  
`power` = power  
`df1` = degrees of freedom for the effect  
`df2` = degrees of freedom of the error  
`eta_p_2` = partial eta-squared  
`mean_mat` = matrix of the means

**References**

too be added

**Examples**

```
## Set up a within design with 3 factors,  
## with correlation between observations of 0.8,  
## 40 participants (who do all conditions), and standard deviation of 2  
## with a mean pattern of 1, 0, 1, conditions labeled 'condition' and  
## 'voice', with names for levels of "cheerful", "neutral", "sad".  
design_result <- ANOVA_design(design = "3w", n = 40, r = 0.8,  
  mu = c(1, 0, 1), sd = 2,  
  labelnames = c("condition", "cheerful", "neutral", "sad"))  
power_result <- power_oneway_within(design_result, alpha_level = 0.05)
```

---

power\_standardized\_alpha

*Optimizing function to achieve desired power based on a standardized alpha level.*

---

## Description

Because the standardized alpha depends on the sample size (N), and the power depends on the sample size, deciding upon the sample size to achieve a desired power requires an iterative procedure. Increasing the sample size reduces the standardized alpha, which requires an increase in the sample size for the power analysis, which reduces the standardized alpha. This function takes a power analysis function that outputs the power as a function of the desired power, the alpha level, as a function of N(x).

## Usage

```
power_standardized_alpha(
  power_function,
  alpha = 0.05,
  power = 0.8,
  standardize_N = 100,
  verbose = Superpower_options("verbose")
)
```

## Arguments

power_function	Function that outputs the power, calculated with an analytic function.
alpha	The unstandardized alpha level (e.g., 0.05), independent of the sample size.
power	The desired power, i.e., the outcome of the power calculation you would like to achieve.
standardize_N	The sample size you want to use to standardize the alpha level for. Defaults to 100 (based on Good, 1982).
verbose	Set to FALSE to not print results (default = TRUE)

## Value

mean\_mat = matrix of the means

## References

Good, I. J. (1982). C140. Standardized tail-area probabilities. *Journal of Statistical Computation and Simulation*, 16(1), 65–66. <<https://doi.org/10.1080/00949658208810607>>

**Examples**

```
## Not run:
res <- power_standardized_alpha(power_function = "pwr::pwr.t.test(d = 0.3,
n = x, sig.level = a_stan, type = 'two.sample',
alternative = 'two.sided')$power", power = 0.9, alpha = 0.05)
res$N

## End(Not run)
```

---

power\_threeway\_between

*Analytic power calculation for three-way between designs.*

---

**Description**

Analytic power calculation for three-way between designs.

**Usage**

```
power_threeway_between(design_result, alpha_level = 0.05)
```

**Arguments**

design\_result    Output from the ANOVA\_design function  
alpha\_level     Alpha level used to determine statistical significance (default to 0.05)

**Value**

mu = means  
sigma = standard deviation  
n = sample size  
alpha\_level = alpha level  
Cohen\_f\_A = Cohen's f for main effect A  
Cohen\_f\_B = Cohen's f for main effect B  
Cohen\_f\_C = Cohen's f for main effect C  
Cohen\_f\_AB = Cohen's f for the A\*B interaction  
Cohen\_f\_AC = Cohen's f for the A\*C interaction  
Cohen\_f\_BC = Cohen's f for the B\*C interaction  
Cohen\_f\_ABC = Cohen's f for the A\*B\*C interaction  
f\_2\_A = Cohen's f squared for main effect A  
f\_2\_B = Cohen's f squared for main effect B  
f\_2\_C = Cohen's f squared for main effect C

f\_2\_AB = Cohen's f squared for A\*B interaction  
f\_2\_AC = Cohen's f squared for A\*C interaction  
f\_2\_BC = Cohen's f squared for B\*C interaction  
f\_2\_ABC = Cohen's f squared for A\*B\*C interaction  
lambda\_A = lambda for main effect A  
lambda\_B = lambda for main effect B  
lambda\_C = lambda for main effect C  
lambda\_AB = lambda for A\*B interaction  
lambda\_AC = lambda for A\*C interaction  
lambda\_BC = lambda for B\*C interaction  
lambda\_ABC = lambda for A\*B\*C interaction  
critical\_F\_A = critical F-value for main effect A  
critical\_F\_B = critical F-value for main effect B  
critical\_F\_C = critical F-value for main effect C  
critical\_F\_AB = critical F-value for A\*B interaction  
critical\_F\_AC = critical F-value for A\*C interaction  
critical\_F\_BC = critical F-value for B\*C interaction  
critical\_F\_ABC = critical F-value for A\*B\*C interaction  
power\_A = power for main effect A  
power\_B = power for main effect B  
power\_C = power for main effect C  
power\_AB = power for A\*B interaction  
power\_AC = power for A\*C interaction  
power\_BC = power for B\*C interaction  
power\_ABC = power for A\*B\*C interaction  
df\_A = degrees of freedom for main effect A  
df\_B = degrees of freedom for main effect B  
df\_C = degrees of freedom for main effect C  
df\_AB = degrees of freedom for A\*B interaction  
df\_AC = degrees of freedom for A\*C interaction  
df\_BC = degrees of freedom for B\*C interaction  
df\_ABC = degrees of freedom for A\*B\*C interaction  
df\_error = degrees of freedom for error term  
eta\_p\_2\_A = partial eta-squared for main effect A  
eta\_p\_2\_B = partial eta-squared for main effect B  
eta\_p\_2\_C = partial eta-squared for main effect C  
eta\_p\_2\_AB = partial eta-squared for A\*B interaction

eta\_p\_2\_AC = partial eta-squared for A\*C interaction  
 eta\_p\_2\_BC = partial eta-squared for B\*C interaction  
 eta\_p\_2\_ABC = partial eta-squared for A\*B\*C interaction  
 mean\_mat = matrix of the means

## References

to be added

## Examples

```
design_result <- ANOVA_design(design = "2b*2b*2b", n = 40,
  mu = c(1, 0, 1, 0, 0, 1, 1, 0), sd = 2,
  labelnames = c("condition", "cheerful", "sad",
    "voice", "human", "robot", "color", "green", "red"))
power_result <- power_threeway_between(design_result, alpha_level = 0.05)
```

---

power\_twoway\_between *Analytic power calculation for two-way between designs.*

---

## Description

Analytic power calculation for two-way between designs.

## Usage

```
power_twoway_between(design_result, alpha_level = 0.05)
```

## Arguments

design\_result    Output from the ANOVA\_design function  
 alpha\_level    Alpha level used to determine statistical significance

## Value

mu = means  
 sigma = standard deviation  
 n = sample size  
 alpha\_level = alpha level  
 Cohen\_f\_A = Cohen's f for main effect A  
 Cohen\_f\_B = Cohen's f for main effect B  
 Cohen\_f\_AB = Cohen's f for the A\*B interaction  
 f\_2\_A = Cohen's f squared for main effect A  
 f\_2\_B = Cohen's f squared for main effect B



f\_2\_AB = Cohen's f squared for A\*B interaction  
 lambda\_A = lambda for main effect A  
 lambda\_B = lambda for main effect B  
 lambda\_AB = lambda for A\*B interaction  
 critical\_F\_A = critical F-value for main effect A  
 critical\_F\_B = critical F-value for main effect B  
 critical\_F\_AB = critical F-value for A\*B interaction  
 power\_A = power for main effect A  
 power\_B = power for main effect B  
 power\_AB = power for A\*B interaction  
 df\_A = degrees of freedom for main effect A  
 df\_B = degrees of freedom for main effect B  
 df\_AB = degrees of freedom for A\*B interaction  
 df\_error = degrees of freedom for error term  
 eta\_p\_2\_A = partial eta-squared for main effect A  
 eta\_p\_2\_B = partial eta-squared for main effect B  
 eta\_p\_2\_AB = partial eta-squared for A\*B interaction  
 mean\_mat = matrix of the means

## References

too be added

## Examples

```

design_result <- ANOVA_design(design = "2b*2b", n = 40, mu = c(1, 0, 1, 0),
  sd = 2, labelnames = c("condition", "cheerful", "sad",
  "voice", "human", "robot"))
power_result <- power_twoway_between(design_result, alpha_level = 0.05)

```

---

p_standardized	<i>Compute standardized alpha level based on unstandardized alpha level and the number of observations N.</i>
----------------	---

---

## Description

Compute standardized alpha level based on unstandardized alpha level and the number of observations N.

## Usage

```
p_standardized(p, N, standardize_N = 100)
```

**Arguments**

p	The observed p-value.
N	The number of observations (e.g., the sample size) in the dataset
standardize_N	The number of observations (e.g., the sample size) you want to use to standardize the alpha level for. Defaults to 100 (based on Good, 1982).

**References**

Good, I. J. (1982). C140. Standardized tail-area probabilities. *Journal of Statistical Computation and Simulation*, 16(1), 65–66. <<https://doi.org/10.1080/00949658208810607>>

**Examples**

```
## Check it yields .05 for N = 100:
p_standardized(p = 0.05, N = 100)
## Check it yields .05 for N = 200, p = 0.03535534:
p_standardized(p = 0.03535534, N = 200)
## What is a standardized p-value for p = .05 and N = 200?
p_standardized(p = 0.05, N = 200)
## You can change the standardization N, repeating the example above:
p_standardized(p = 0.05, N = 100, standardize_N = 200)
```

---

sim\_result-methods      *Methods for sim\_result objects*

---

**Description**

Methods defined for objects returned from the ANOVA\_exact, ANOVA\_exact2, and ANOVA\_power functions.

**Usage**

```
## S3 method for class 'sim_result'
print(x, ...)

## S3 method for class 'sim_result'
plot(x, ...)
```

**Arguments**

x	object of class <code>sim_result</code> as returned from one of the simulation functions in <code>Superpower</code>
...	further arguments passed through, see description of return value for details. <a href="#">ANOVA_design</a> .

**Value**

`print` Prints short summary of the simulation result

`plot` Returns `meansplot` or a plot of the distribution of p-values depending on whether an exact or Monte Carlo simulation was performed

---

Superpower\_options      *Set/get global Superpower options*

---

**Description**

Global Superpower options are used, for example, by `ANOVA_exact` (et al.) and `ANOVA_power`. But can be changed in each functions directly using an argument (which has precedence over the global options).

**Usage**

```
Superpower_options(...)
```

**Arguments**

...      One of four: (1) nothing, then returns all options as a list; (2) a name of an option element, then returns its' value; (3) a name-value pair which sets the corresponding option to the new value (and returns nothing), (4) a list with option-value pairs which sets all the corresponding arguments. The example show all possible cases.

**Details**

The following arguments are currently set:

- `verbose` should verbose (printed results) be set to true? Default is TRUE.
- `emm` Option to perform analysis of estimated marginal means. Default is FALSE.
- `emm_model` Model type ("multivariate", or "univariate") for estimated marginal means. Default is "multivariate".
- `contrast_type` The type of comparison for the estimated marginal means. Default is "pairwise". See `?emmeans::contrast-methods` for more details on acceptable methods.
- `plot` Option to automatically print plots. Default is FALSE.
- `alpha_level` Alpha level used to determine statistical significance. Default is .05.
- `correction` Option to set a correction for sphericity violations. Default is no correction. This can be set to "none", "GG" Greenhouse-Geisser, and "HF" Huynh-Feldt
- `liberal_lambda` Option to set a logical indicator of whether to use the liberal ( $\text{cohen}_f^2 \cdot (\text{num\_df} + \text{den\_df})$ ) or conservative ( $\text{cohen}_f^2 \cdot \text{den\_df}$ ) calculation of the noncentrality ( $\lambda$ ) parameter estimate. Default is FALSE.

**Value**

depends on input, see above.

**Note**

All options are saved in the global R [options](#) with prefix Superpower .

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